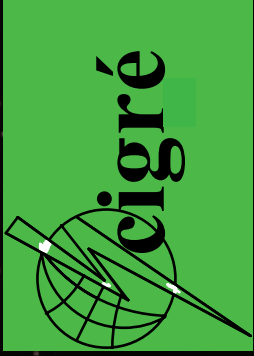


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Numerical Distance Protection Principles and Applications

Gerhard Ziegler
Gustav Steynberg

Numerical Distance Protection – Course program

Part 1: Fundamentals and operation principles	26-11	9:30-11:00 Break 11:30-13 Lunch
Part 2: Teleprotection using distance relays		14:30-15:30 Break
Part 3: Power swing blocking/tripping (out-of-step protection)		16:00-17:00
Part 4: Distance protection of parallel lines	27-11	8:00-9:30
Part 5: Distance protection of series-compensated lines		9:30-10:00 Break
Part 6: Distance protection of three-terminal and tapped lines		10:30-11:15
Part 7: Auto-reclosure (ARC)		11:15-11:45
Part 8: Setting of distance protection		11:45-13:00 Lunch
Part 9: Current and voltage transformer requirements		14:30-16:00
Part 10: Connection, commissioning and maintenance		16:30-17:00
Part 10: Distance protection in the transmission system	28-11	8:00-9:00
Part 12: International practices and recent trends		9:00-9:30
Part 13: Modern numerical relay design and integrated functions		9:30-10:00 Break
Part 14: Integration in Substation automation with IEC 61850		10:30-12:00
Final Discussion		12:00-13:00 End

Modern Relay Design and Integrated Functions

Power System Protection: Relay design

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Uniform Design Trend

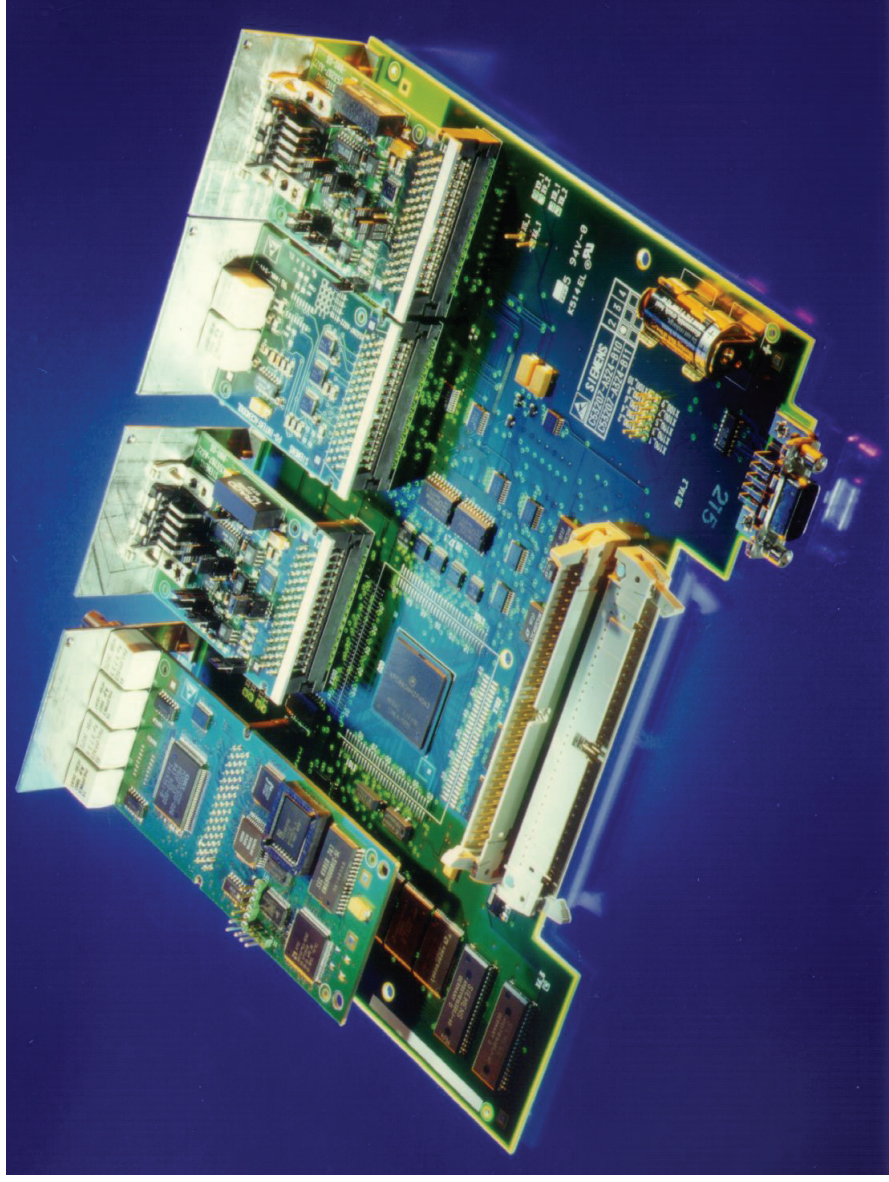


SIPROTEC4 Relay Series

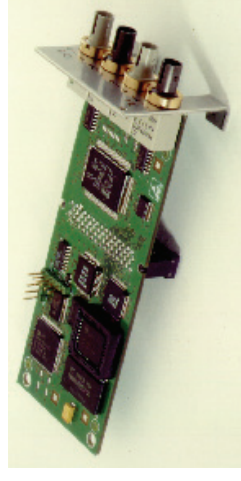
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Modern IED processing and communication board



**O.F.
Double
ring**



**Exchangeable
communication
modules**

**Wired
IEC61850
Ethernet
100 Mbit**



Development of processing hardware

Begin of delivery	Relay generation	Memories RAM/EPROM	Bus width	Clock frequency	Processing power
1992	SIPROTEC 3	256/512 k	16 bit	16 MHz	1.0 MIPS
2000	SIPROTEC 4	512k/4MB + 4MB D-RAM	32 bit	80 MHz	35 MIPS

SIPROTEC 4 Data acquisition

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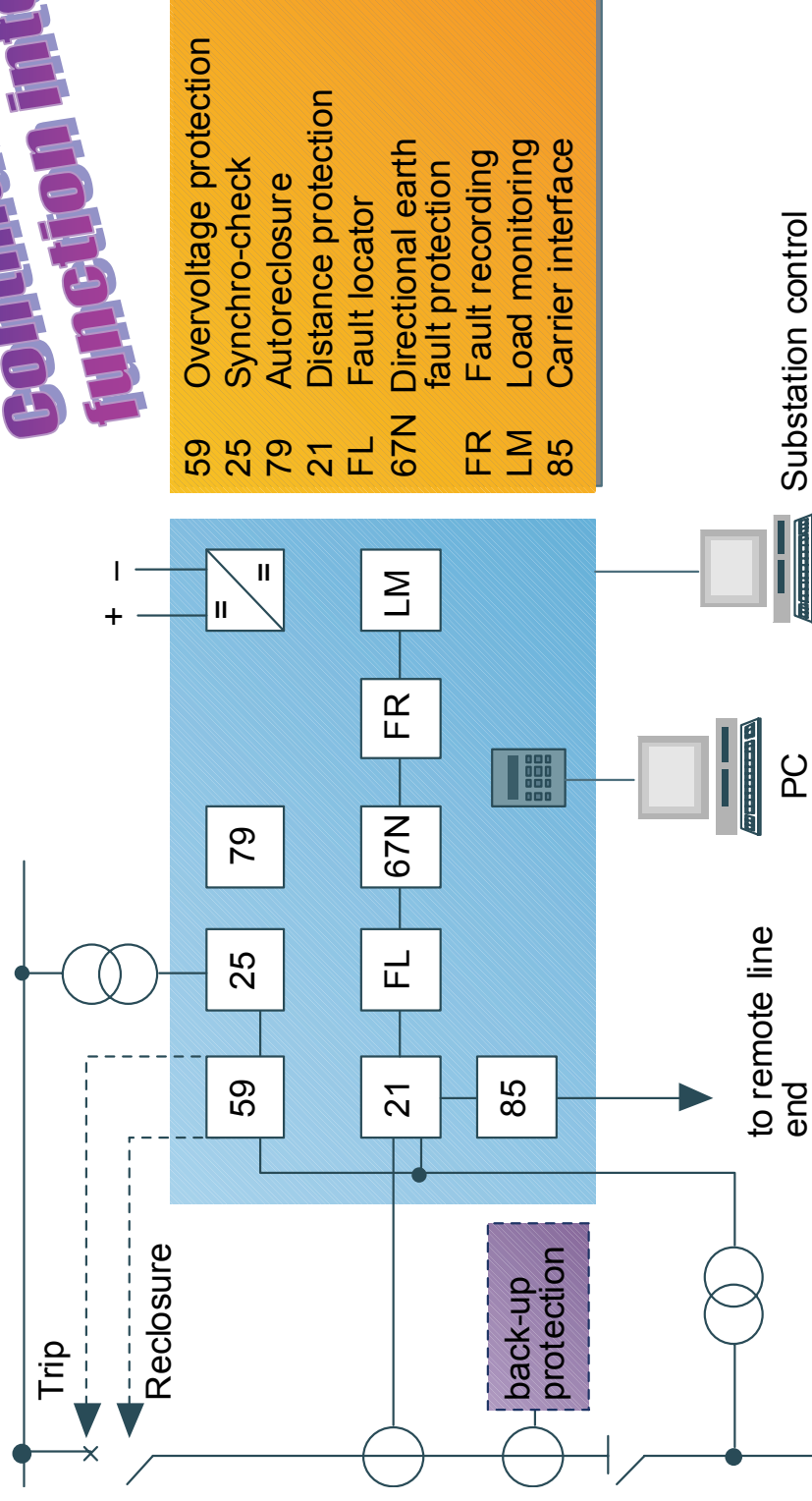
Sampling rate:	1000 Hz (1200 Hz with 60 Hz nominal frequency)
Samples per period:	20
Anti-aliasing filter:	500 Hz (600 Hz) limiting frequency
A/D-conversion:	16 bit, corresponding to 65536 steps
Measuring value storage:	15 s
Program language:	C/C++

Multifunction relays

Example: Line Protection

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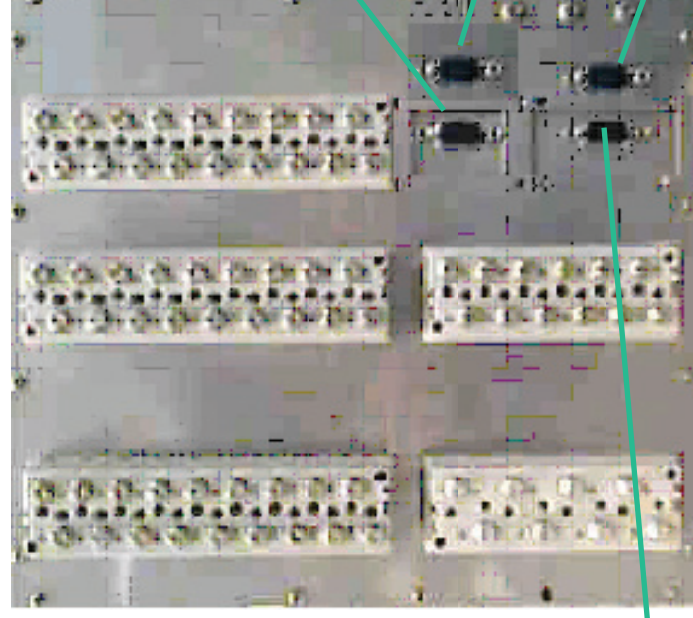
*continuing
function integration*



SIPROTEC 4

7SA6: Communication interfaces

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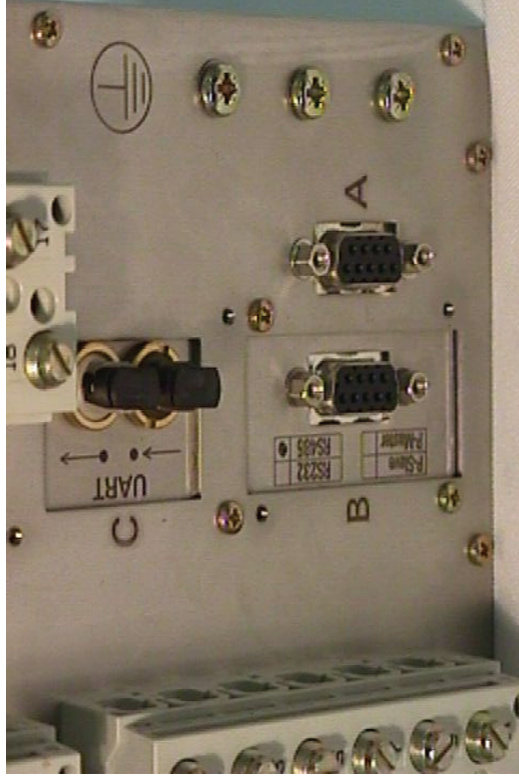
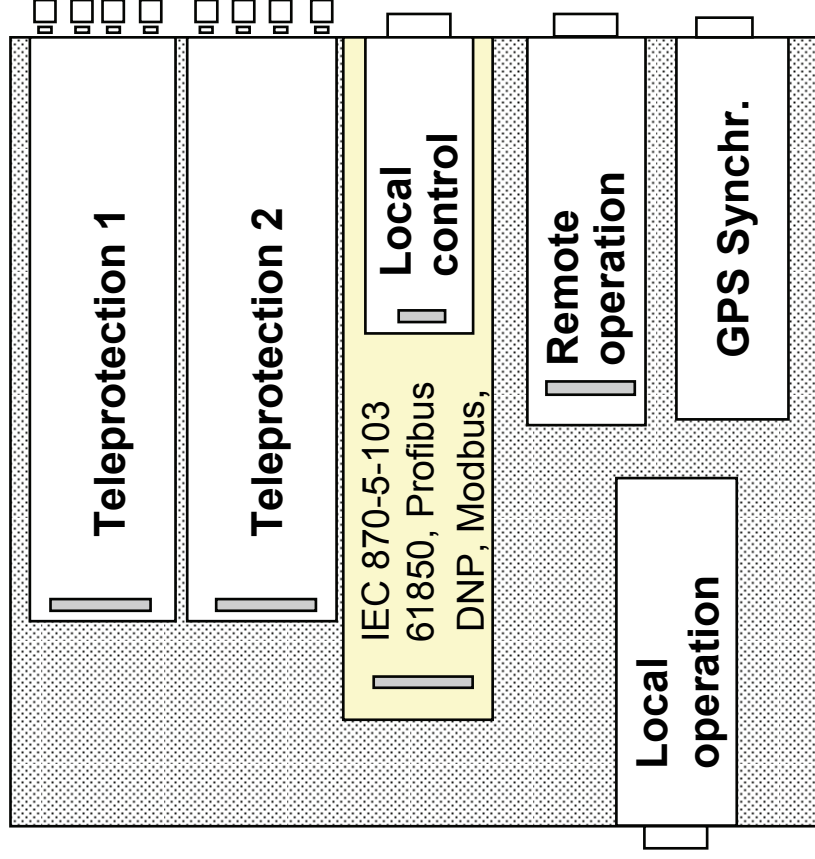
PC-interface,
front side
⇒ electric RS 232

Analog output 20 mA or
teleprotection interface
⇒ electric or optic

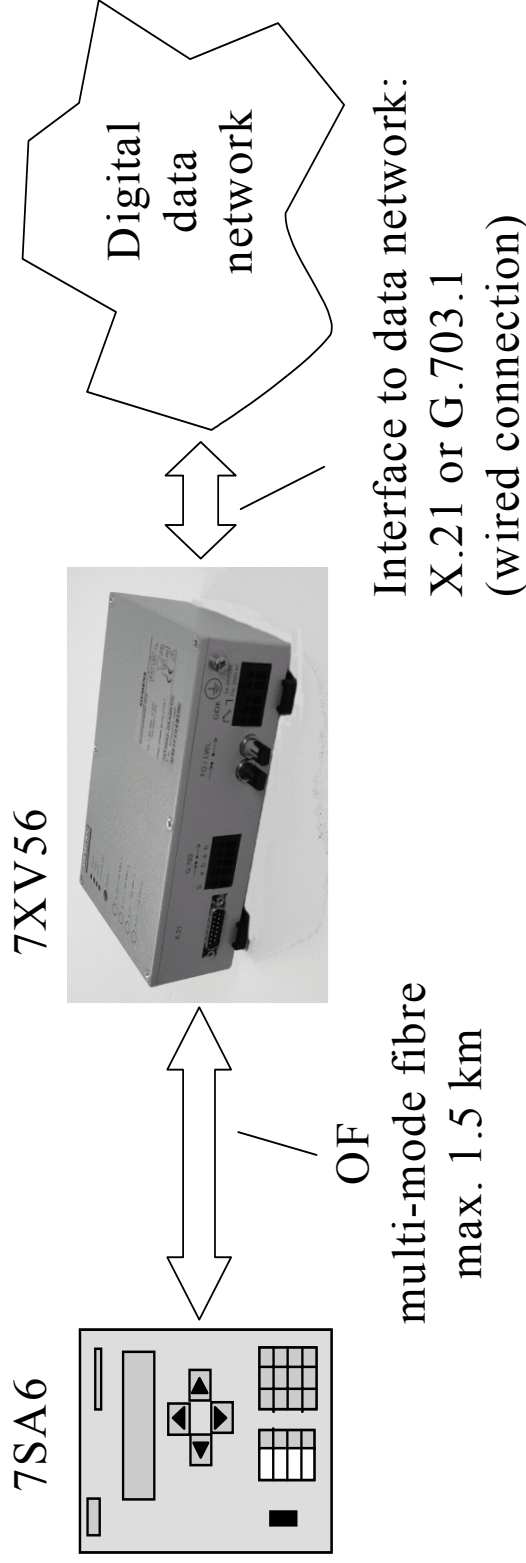
Service interface
⇒ electric RS232 / RS485
⇒ DIGSI 4 / modem

Time synchronisation
⇒ GPS (IREC-B)
⇒ or DCF-77

System interface
⇒ electric or optic
⇒ IEC60870-5-103, IEC61850, Profibus FMS, DNP3.0
or Modbus;
alternatively analog output 20 mA

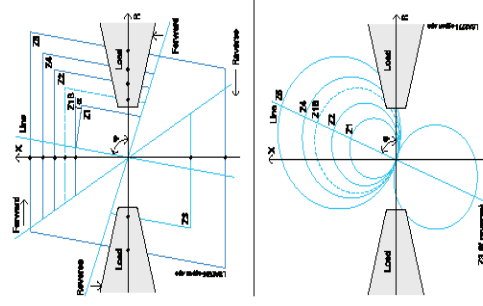


Modems for relay communication



21 & 87 Relay

United full scheme distance and differential protection



21



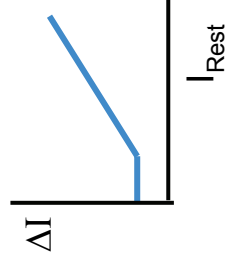
Copy of well
proven features

21, 21N
67N
68, 68T

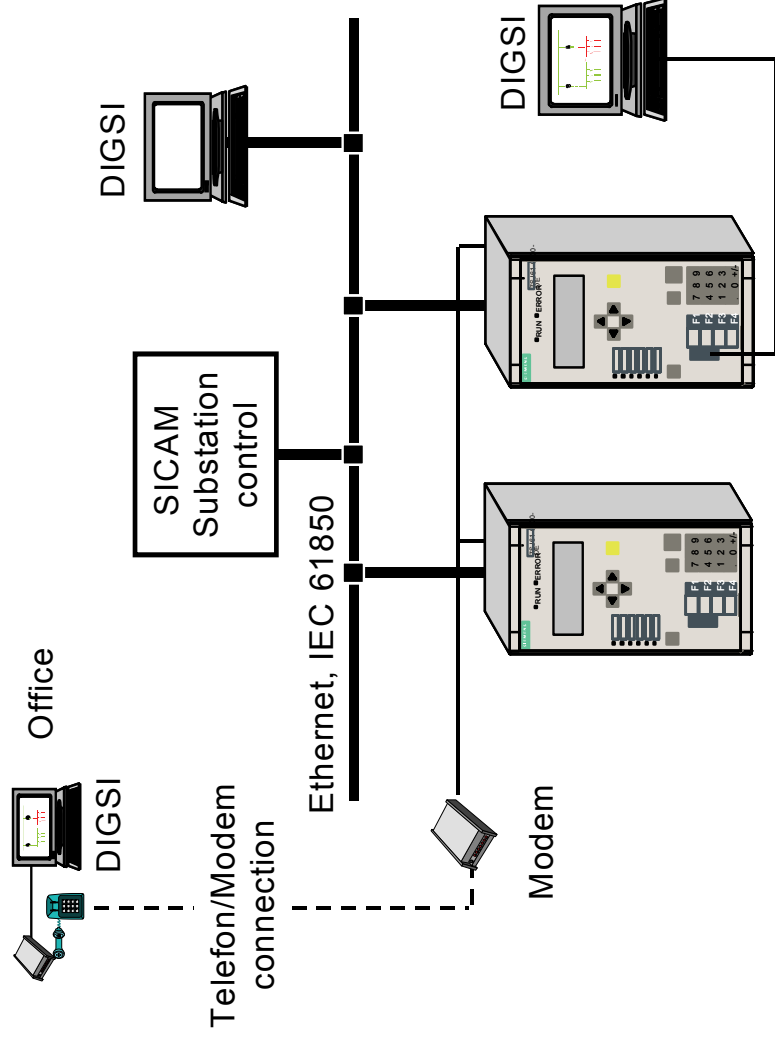
21 & 87



87



Modern Substation Automation



Software marshalling matrix



Parameter - Rangierung - Project 1 / Region North / 7SJ636 V4.0/7SJ636 V04.00.18

Information			Ziel																												
Nr	Dt	Lt	Ty	BA														LE													
				11	12	13	14	15	16	17	18	19	20	21	22	1	2	3	4	5	6	7	8	9	10	11	12	13	14	B	
Anlagendaten 1																													*		
Störschreibung																													*		
Anlagendaten 2																*													*		
U/AMZ	1721	>U/AMZ >> blk	EM																												
	1762	U/AMZ Anr L1	AM														G														
	1763	U/AMZ Anr L2	AM															G													
	1764	U/AMZ Anr L3	AM																G												
	1724	>U/AMZ IE>> blk	EM																												
	1765	U/AMZ Anr E	AM																G											*	
Messwertüberw.																				*											
Automatische VWE	2701	>AVWE ein	EM																			U									
	2781	AVWE aus	AM																												KC
	2782	AVWE ein	IE																												
	2851	AVWE EIN-Kom.	AM																												
Fehlerort																														*	
Ort/Modus																														*	
Schaltobjekte																															
		Q0 EIN/AUS	BR_D12																												KC
		Q0 EIN/AUS	DM																												
		Q1 EIN/AUS	BR_D2																												KC
		Q1 EIN/AUS	DM																												KC
		Q8 EIN/AUS	BR_D2																												KC

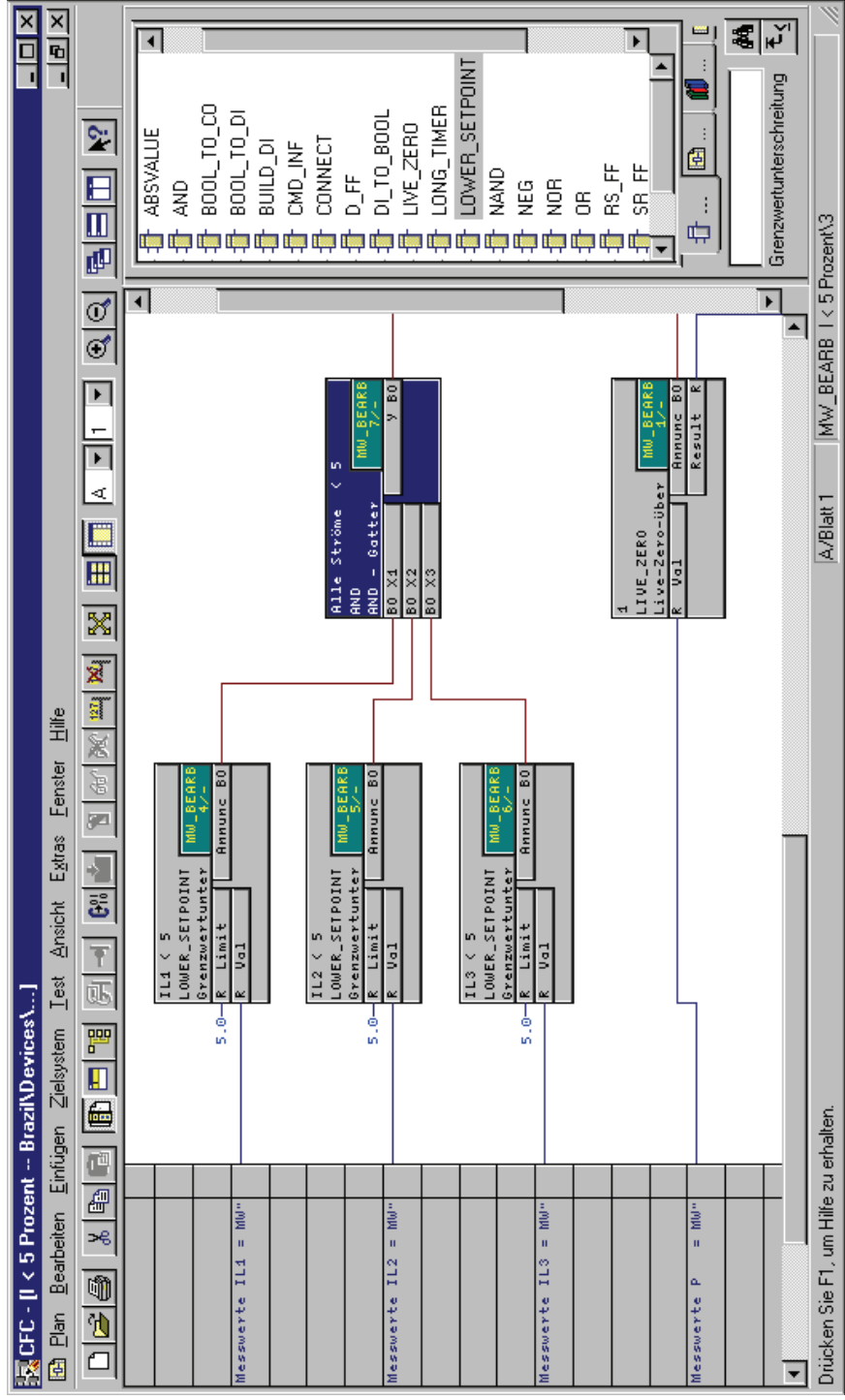
G (gespeichert)

U (ungespeichert)

(nicht rangiert)

PLC (Programmable logic control)

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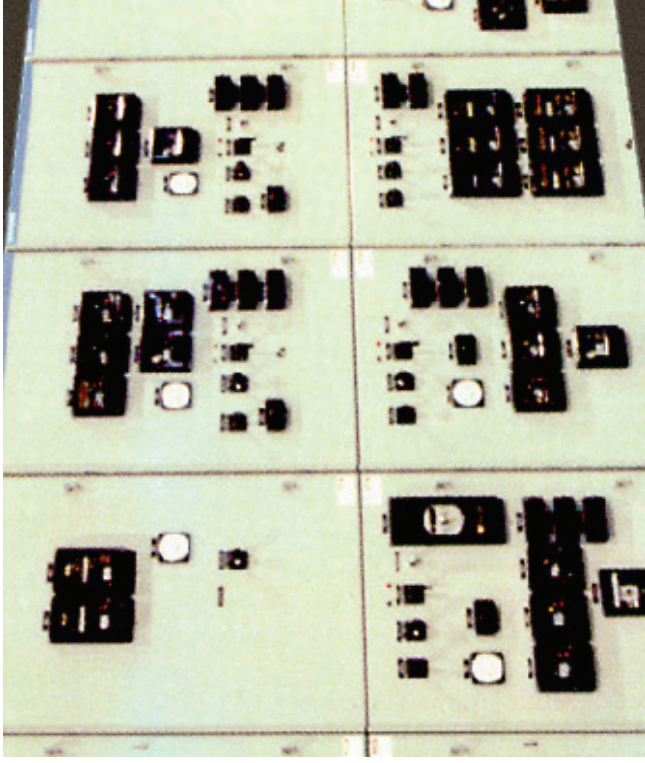


Distribution Switchgear Innovation

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One IED replaces a conglomeration of “black box” devices

Traditional panels with mechanical relays and control



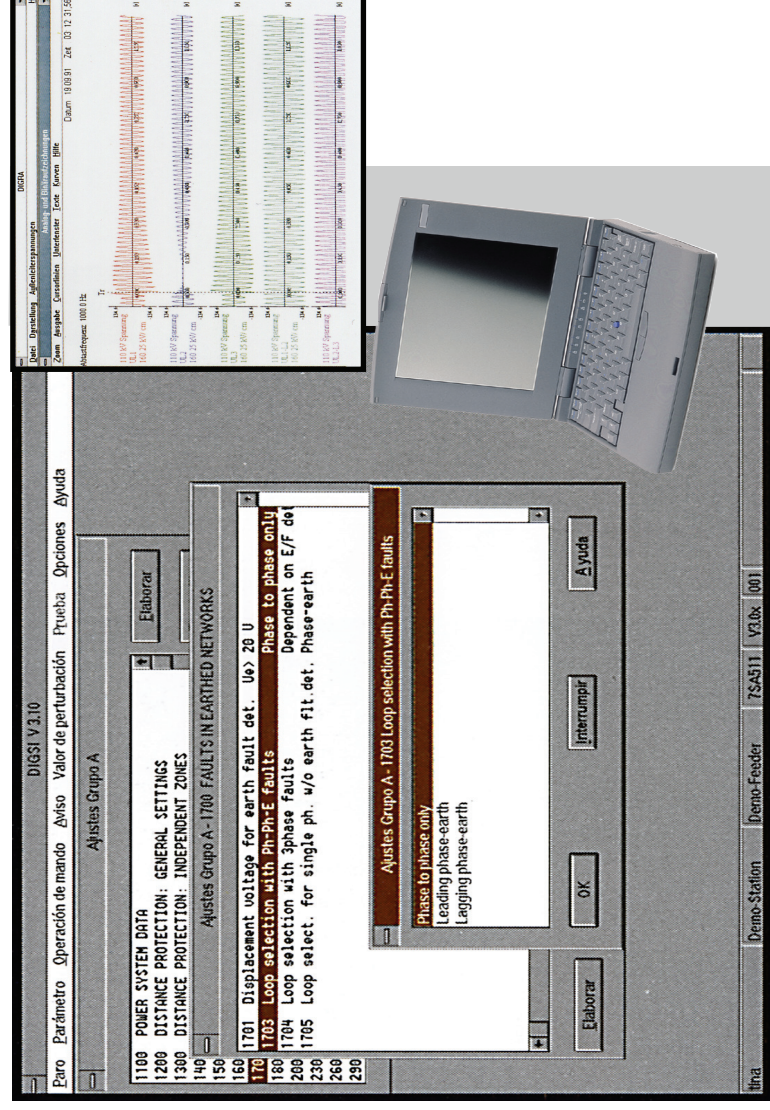
Modern panels with digital multifunction relay



State-of-the-art:

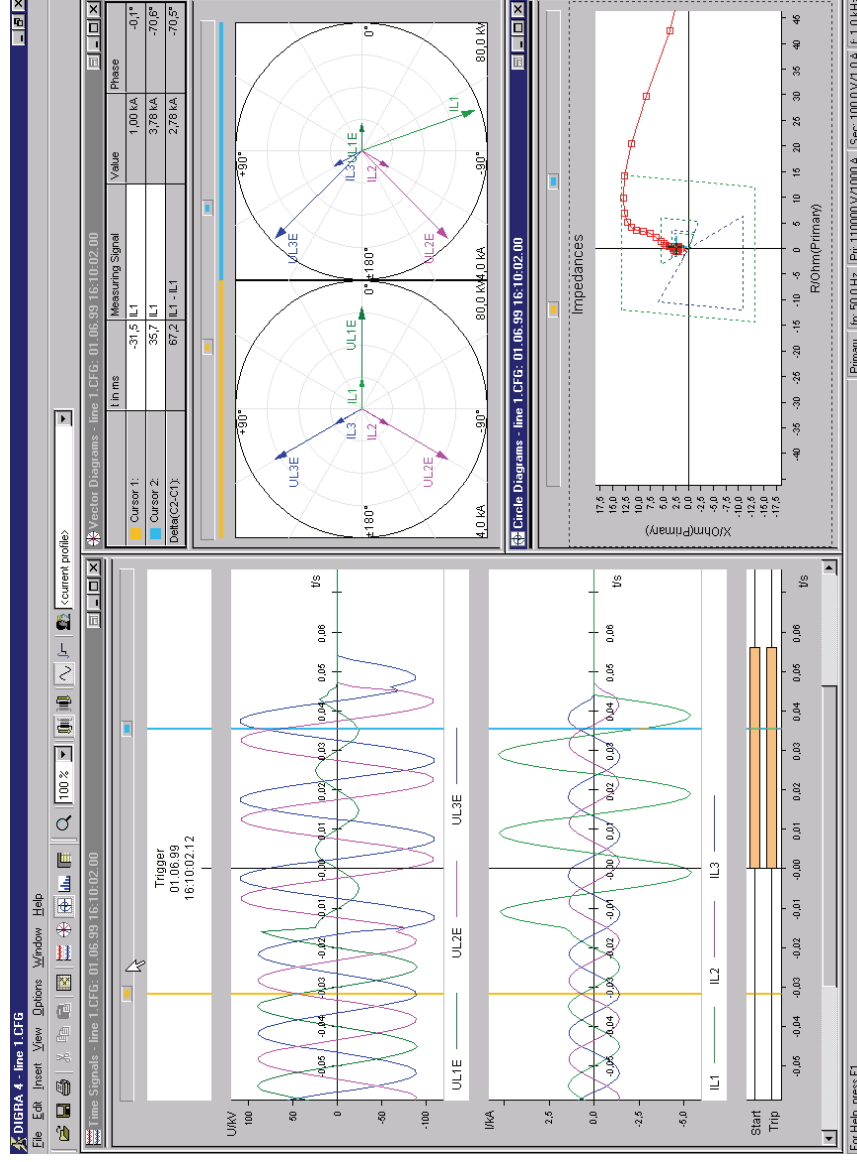
Windows Based Relay Operating Programs

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A New Quality of Fault Analysis

SIEMENS



Powerful PC Tools

Calculation of
phasors, components,
sequences,
impedances,
harmonics,
and more

Valuation of integrated functions in protection relays Utility survey, Germany 2003

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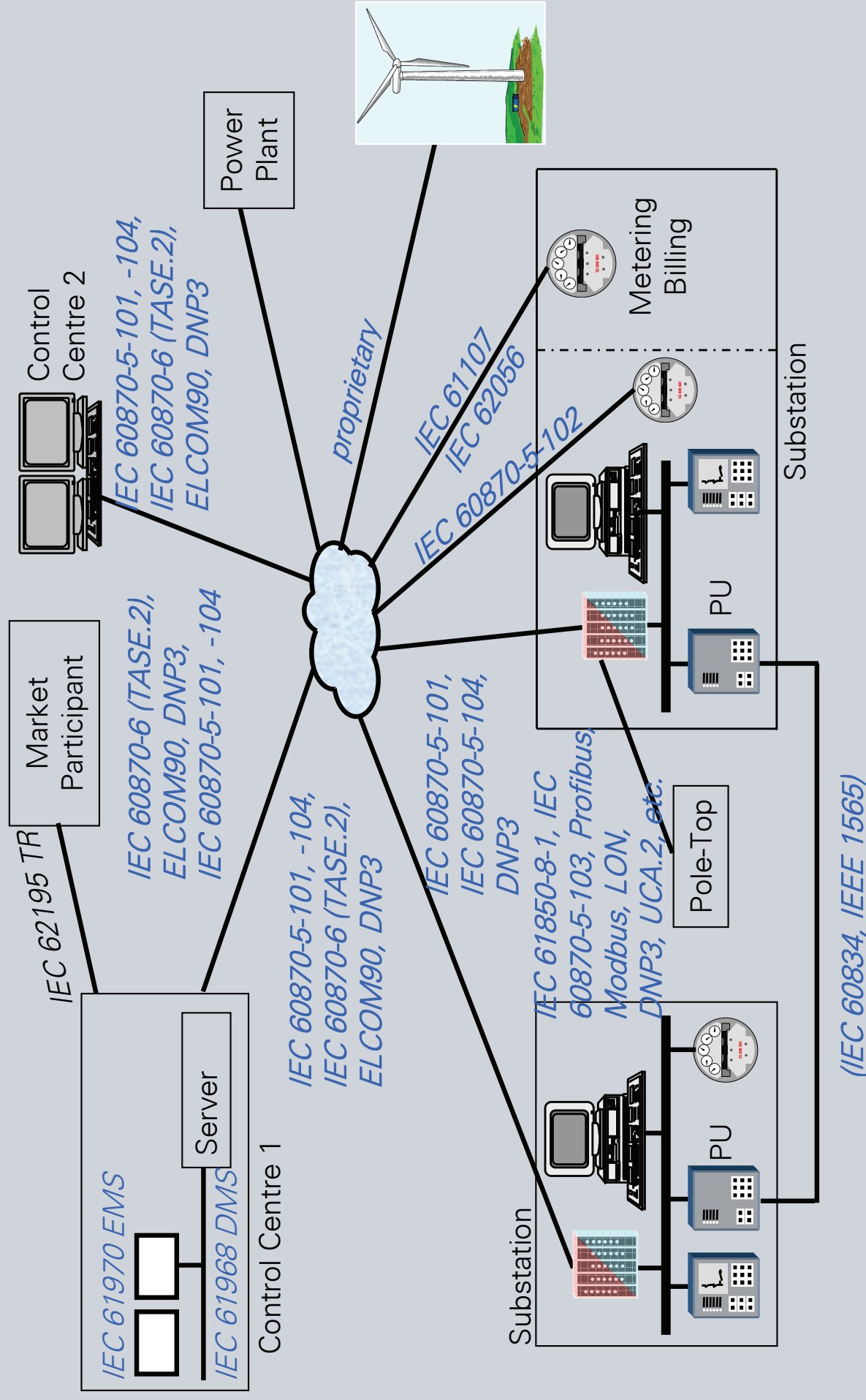
Integrated functions	Valuation:					
	0	1	2	3	4	5
Flexible setting					X	
Higher selectivity				X		
Shorter operating time			X			
Lower CT and VT requirements		X				
Integrated fault recording						X
Integrated load monitoring (U, I, P, f)		X				
Remote retrieval of fault records						X
Remote setting			X			
Self-monitoring						X
Remote diagnosis				X		
Programmable logic functions					X	
Free assignment of I/O interfaces						X

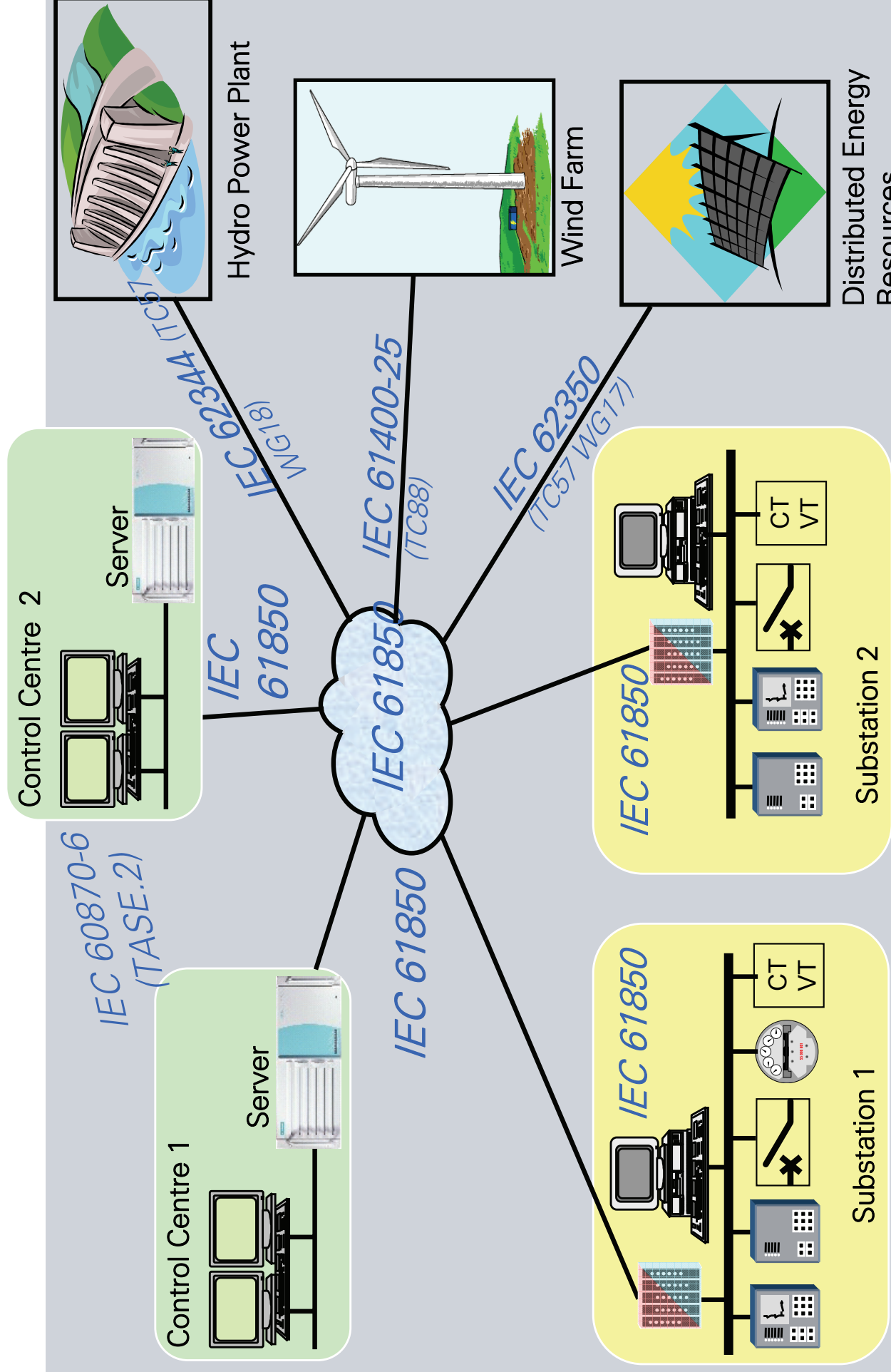
IEC 61850 - Basics and trends of numerical communication in substations

Power Transmission
and Distribution

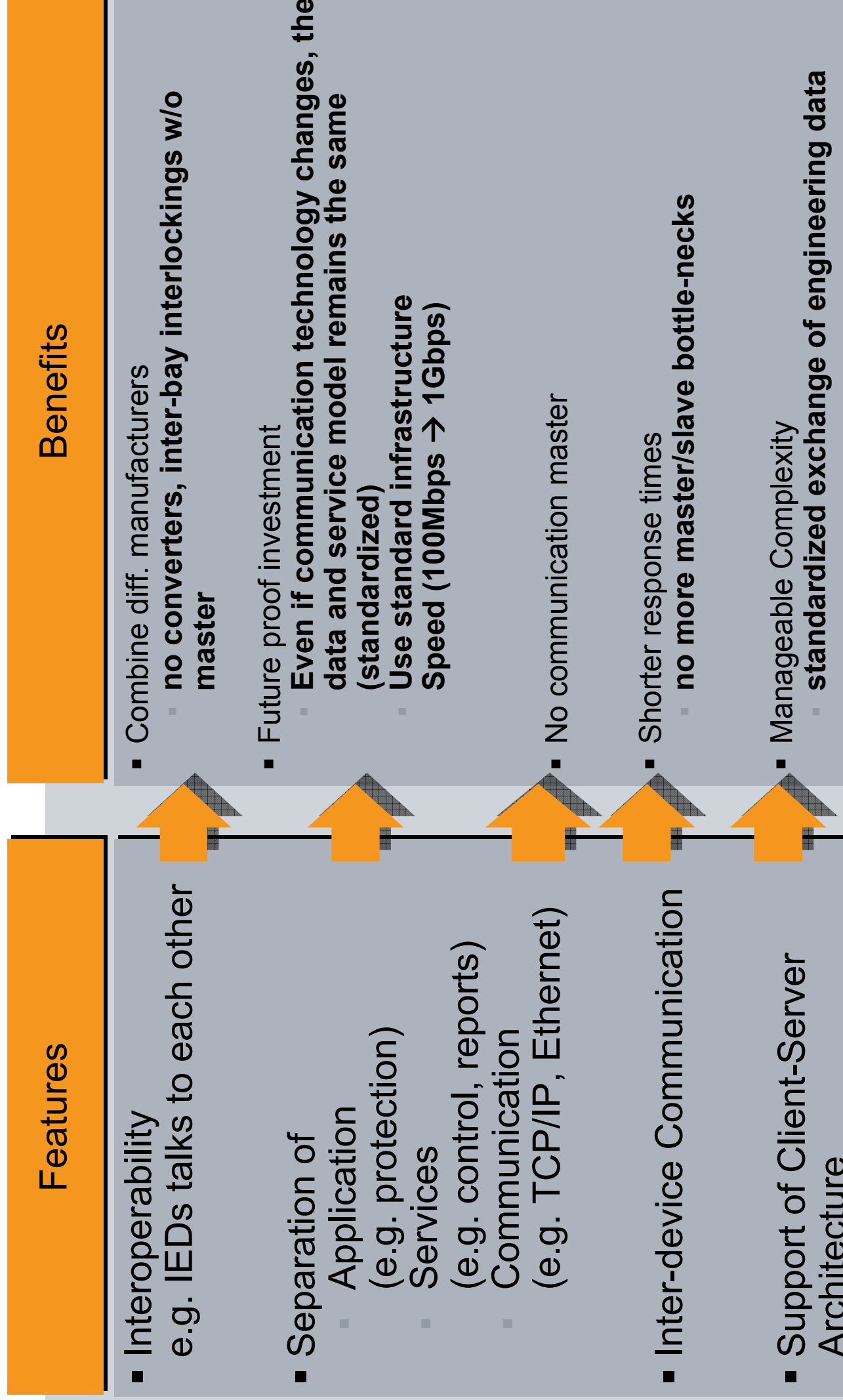


Today's Communication Standards within and outside of Substations





What's so special about IEC61850?



Interoperability ≠ Interchangeability

Interoperability

is the ability of two or more IEDs from the same vendor, or different vendors, to exchange information and uses that information for correct co-operation.

Interchangeability

ability to replace a device supplied by one manufacturer with a device supplied by another manufacturer, without making changes to the other elements in the system.

IEC 61850 Part 1

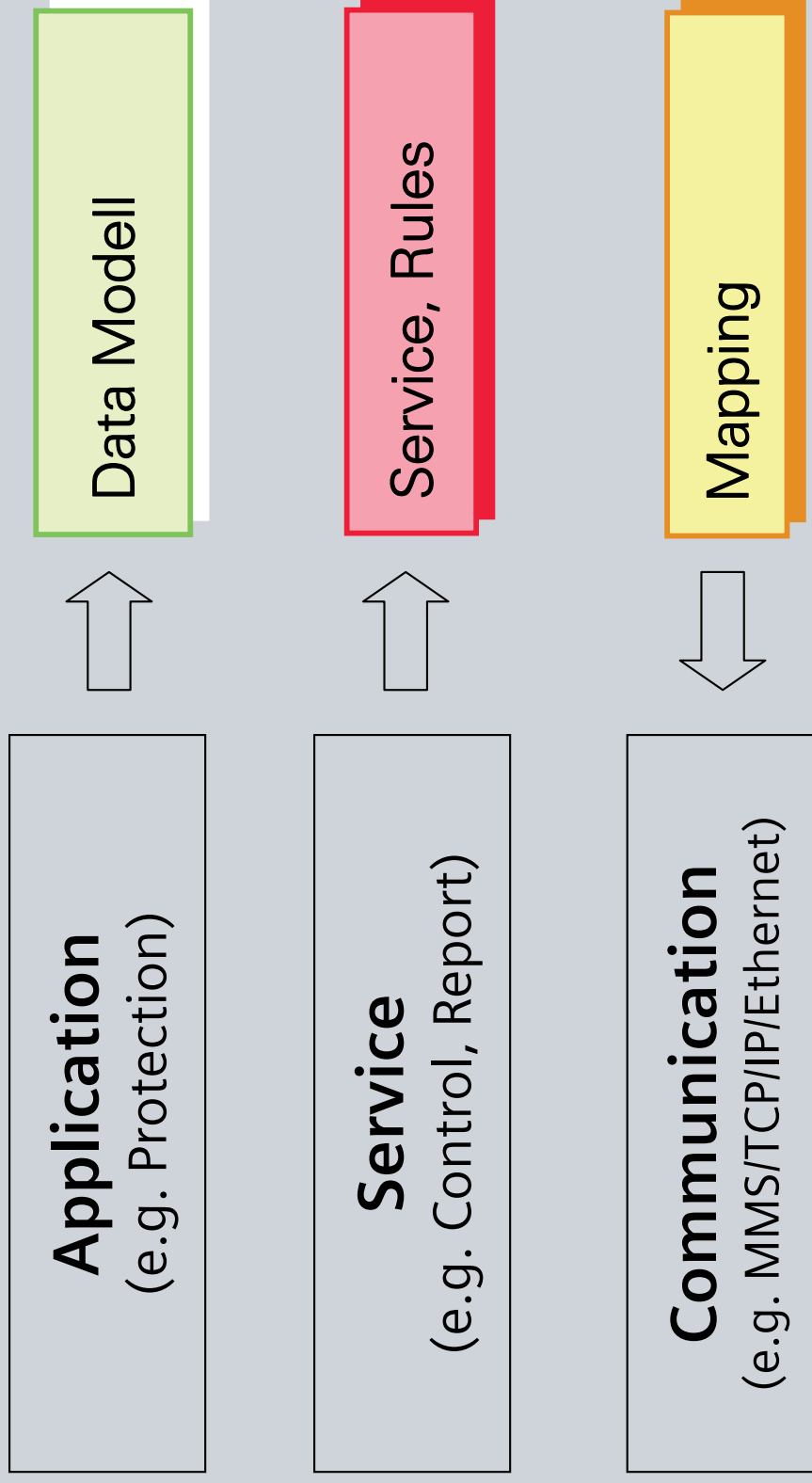
“Interchangeability is beyond this communication standard.”

What is needed for interoperability

- Data model
- Service model
- Mapping to a real protocol
- Communication medium
- Data exchange between engineering tools
- Conformance test

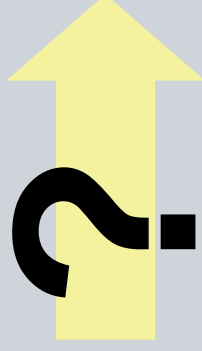
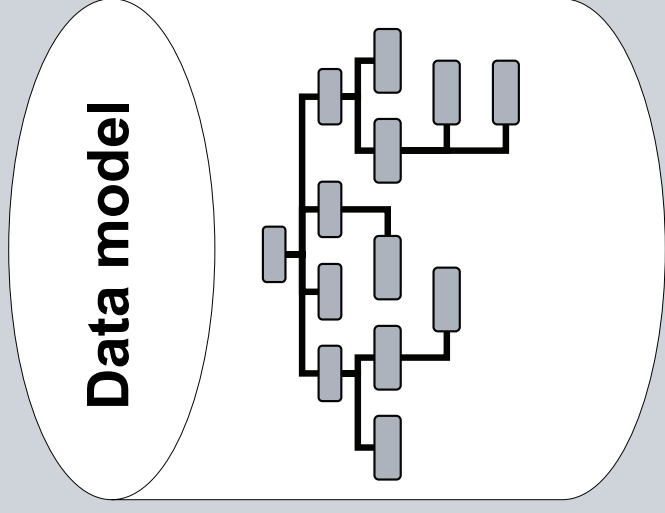
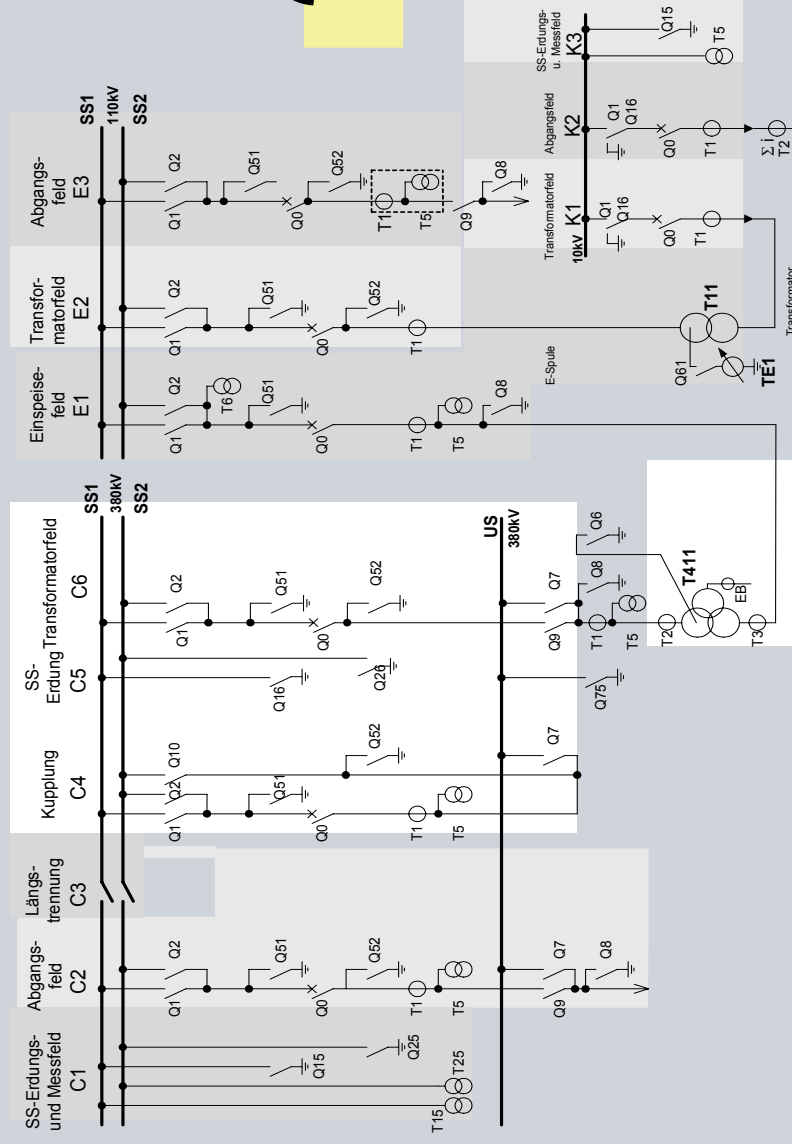
IEC 61850 standardized these needs

The idea behind IEC 61850: Separation

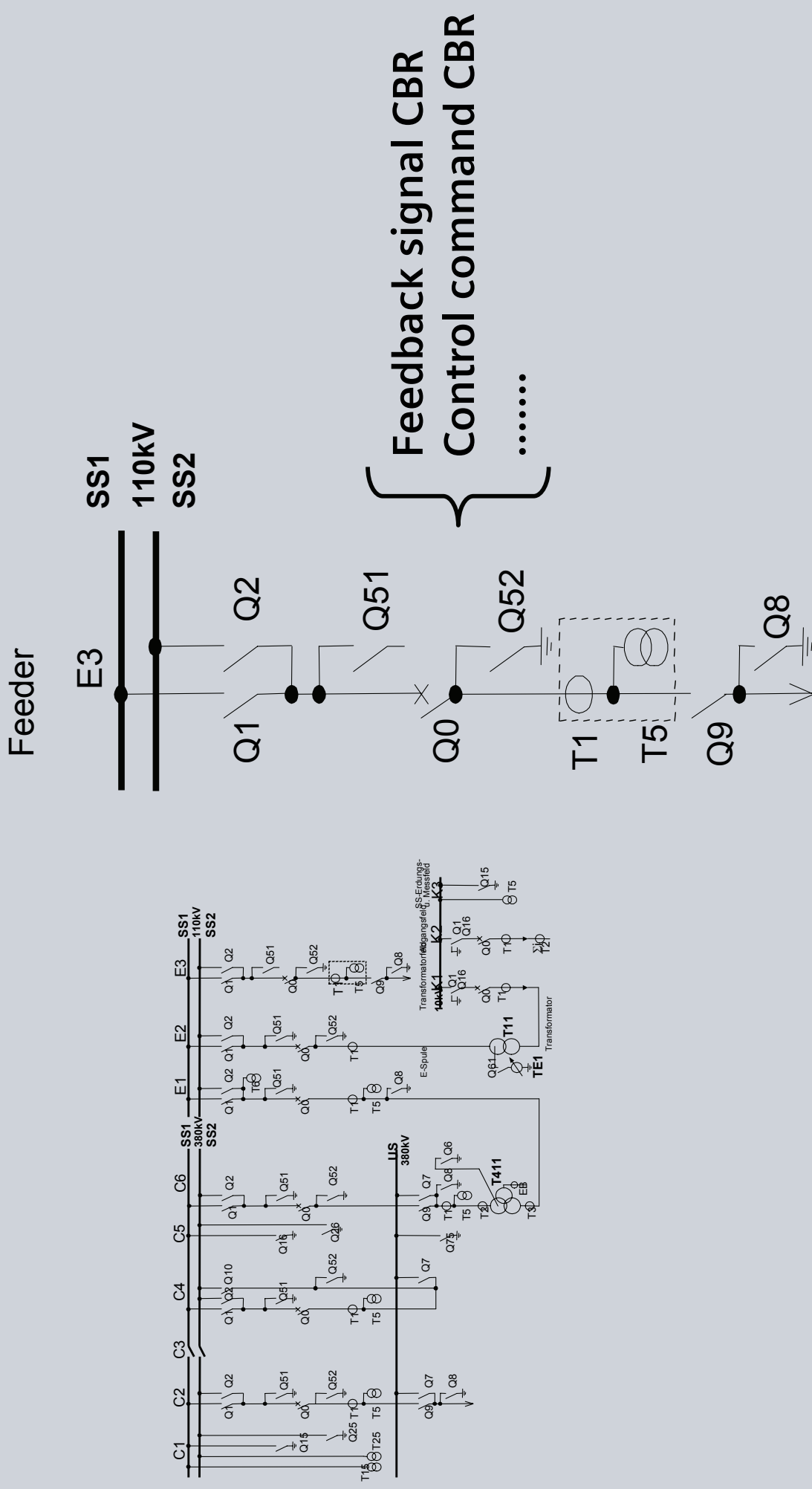


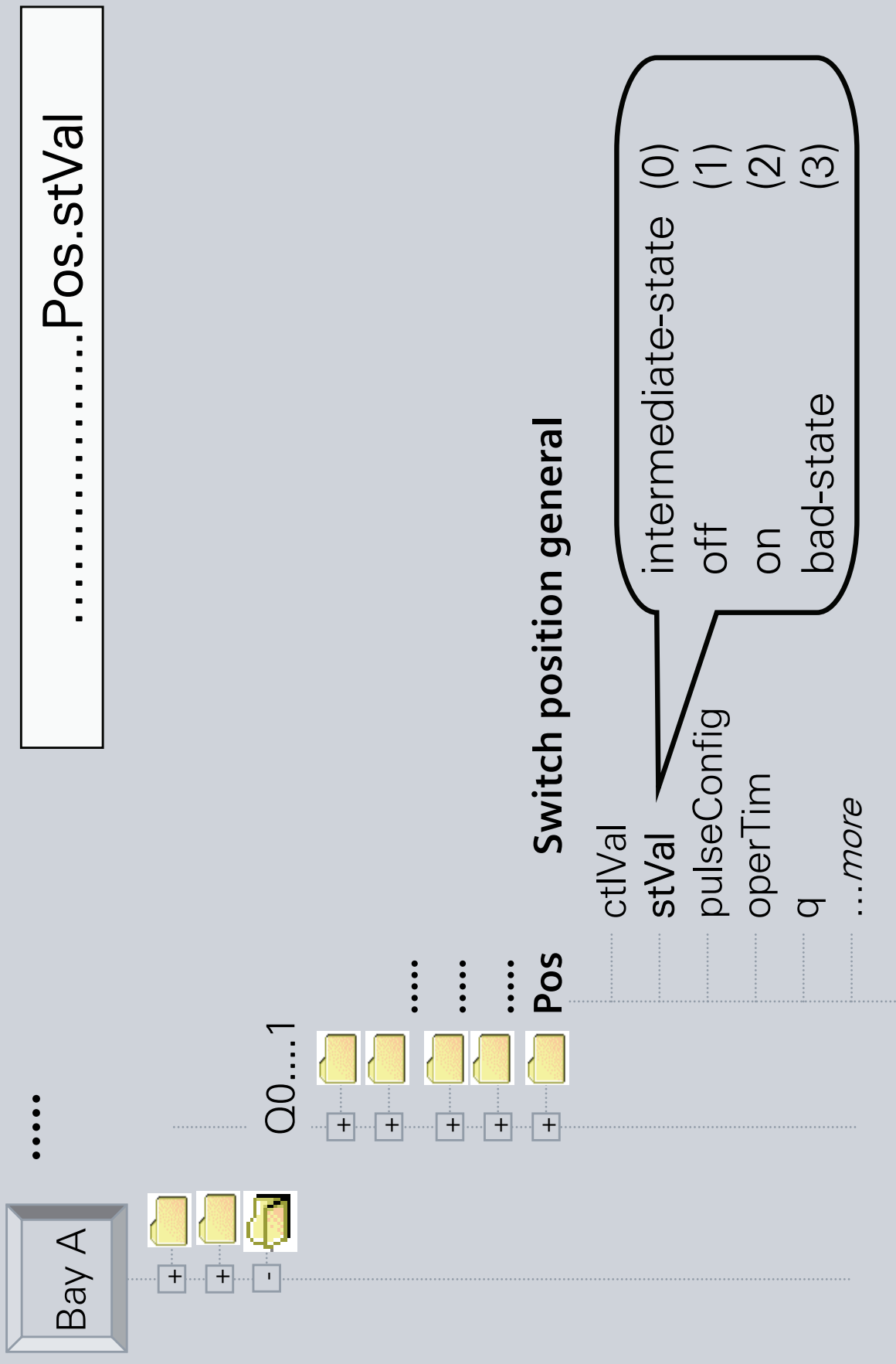
because Data did not change and will not change
but the communication technology will

Data model How are the data of switchgear and control modeled considering the functionality according to the IEC 61850?
How does this influence your data and specification?

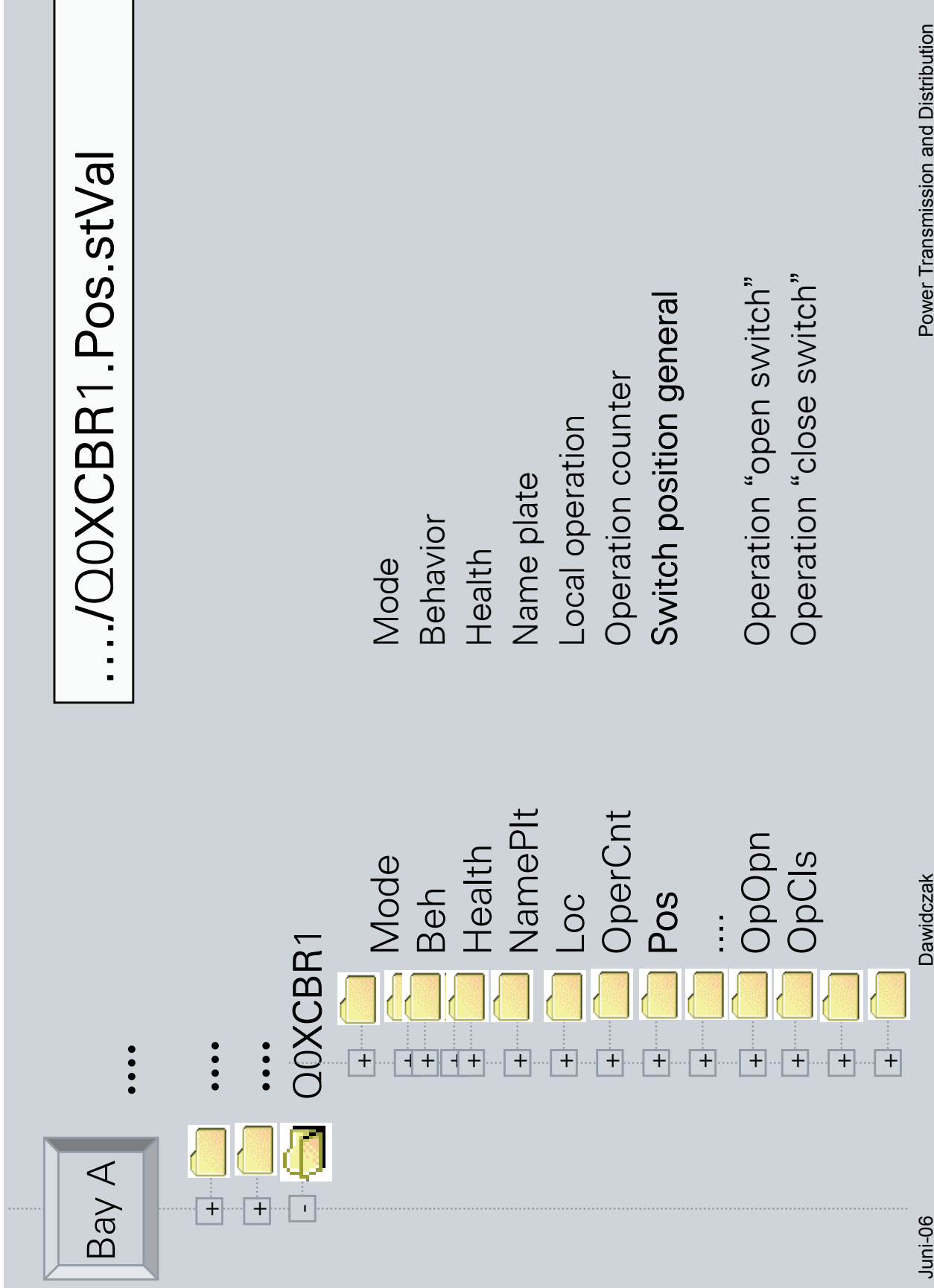


Basis of the data model

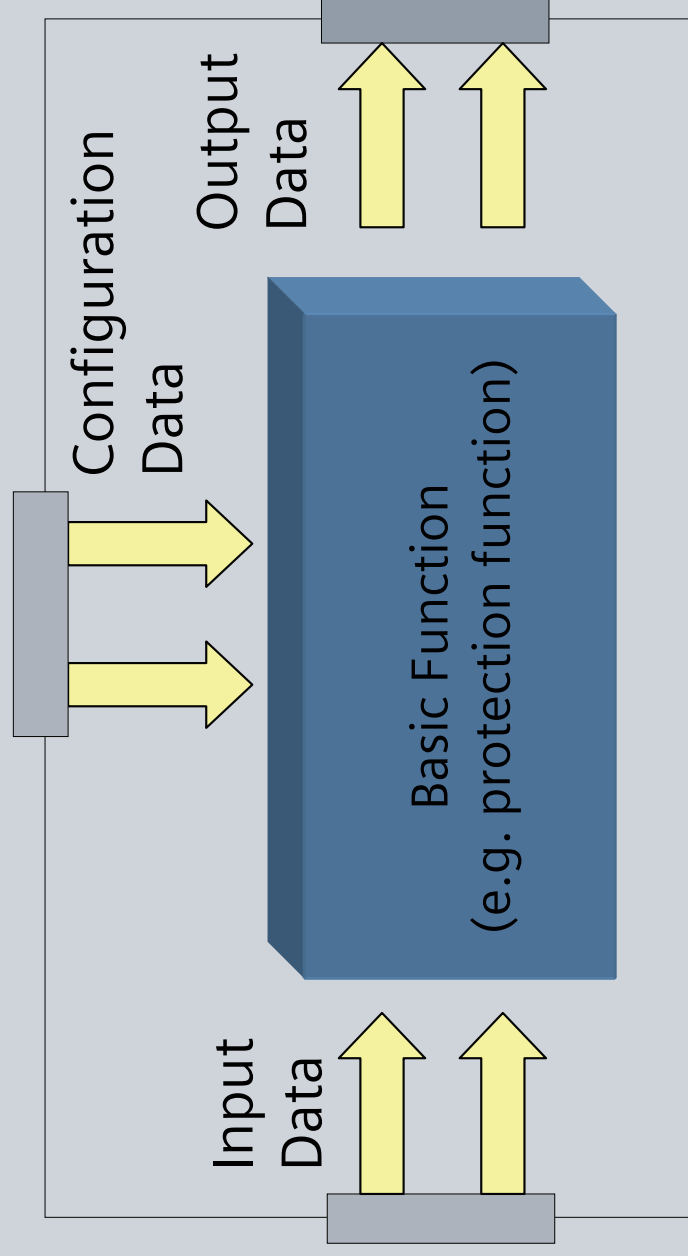




IEC 61850: Data Objects – Logical Node



Concept of a Logical Node



- Functions still remain vendor specific
- Data exchange becomes standardized

IEC 61850: Logical Node – Logical Device



Logical Node: There are about 90 classes

Group Indicator	Logical node groups
A	Automatic Control
C	Supervisory control
G	Generic Function References
I	Interfacing and Archiving
L	System Logical Nodes
M	Metering and Measurement
P	Protection functions
R	Protection related functions
S	Sensors
T	Instrument Transformer
X	Switchgear
Y	Power Transformer
Z	Further (power system) equipment

MMXU Measuring (Measurand unit)
 MMTR Metering
 MSQI Sequence and Imbalance
 MHAI Harmonics and Interharmonics
 MDIF Differential Measurements

PDIF Differential protection
 PTEF Transient Earth Fault
 PTOC Time overcurrent protection
 PDIS Distance protection
 ...more

SIMG Insulation medium meas unit
 SARC Monitoring and diagnostics for arcs
 SPDC Monitoring and diagnostics for partial discharge

XCBR Circuit Breaker
 XSWI Circuit Switch

Logical Node for Circuit Breaker - LN XCBR

IEC 61850-7-3

Mandatory /Optional

XCBR class			
Attribute Name	Attr. Type	Explanation	T M/O
LNName		Shall be inherited from Logical-Node Class (see IEC 61850-7-2)	
Data			
Common Logical Node Information			
		LN shall inherit all Mandatory Data from Common Logical Node Class	M
Loc	SPS	Local operation (local means without substation automation communication, hardwired direct control)	M
EEHealth	INS	External equipment health	O
EEName	DPL	External equipment name plate	O
OpCnt	INS	Operation counter	M
Controls			
Pos	DPC	Switch position	M
BlkOpn	SPC	Block opening	M
BlkCls	SPC	Block closing	M
ChaMotEna	SPC	Charger motor enabled	O
Metered Values			
SumSwARs	BCR	Sum of Switched Amperes, resetable	O
Status Information			
CBOPCap	INS	Circuit breaker operating capability	M
POWCap	INS	Point On Wave switching capability	O
MaxOpCap	INS	Circuit breaker operating capability when fully charged	O

Data: There are about 350 classes

Data Classes	Number
System information	13
Physical device inform.	11
Measurands	66
Metered values	14
Controllable Data	36
Status information	85
Settings	130
	355

Types: DPC, SPC, INC....

Pos – Switch position

TapChg – Change voltage (stop, higher, lower)

FanCtl – Fan control

More.....

Types: DPS, SPS, INS. ACT....

OP – Operate

Loc – Change voltage (stop, higher, lower)

OpCnt – Operation counter

More.....

They are assigned to 28 common data classes in Part 7-3, e.g. DPC, SPC....

Common data class - Controllable double point (DPC)

functional constraint

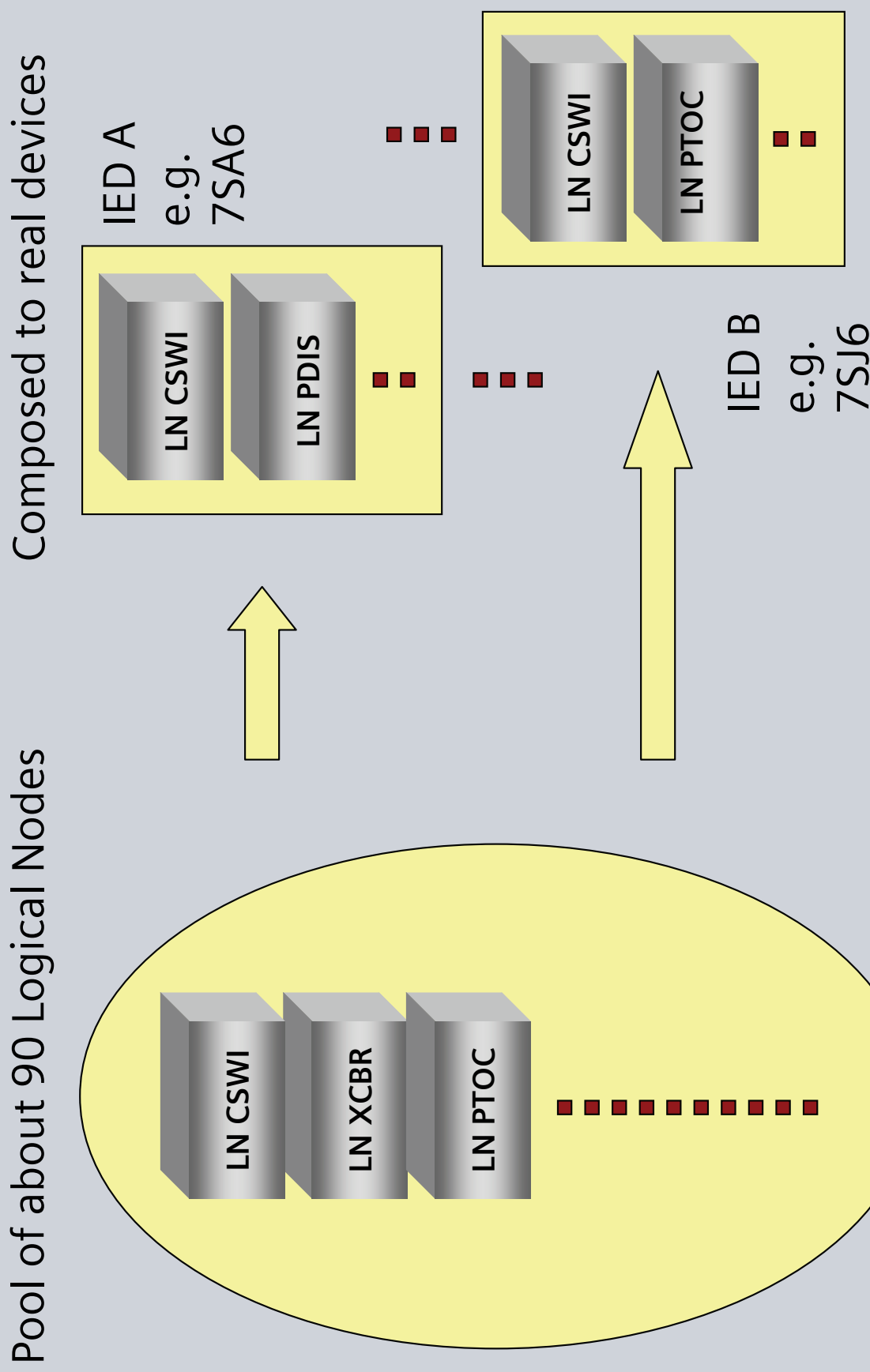
basic types

control value

status value

DPC class					
Attribute Name	Attribute Type	FC	TrgOp	Value/Value Range	M/O/C
DataSetName	Inherited from Data Class (see IEC 61850-7-2)				
DataAttribute					
control and status					
ctlVal	BOOLEAN	CO		off (FALSE) on (TRUE)	AC_CO_M
operTm	TimeStamp	CO			AC_CO_O
origin	Originator	CO, ST			AC_CO_O
ctlNum	INT8U	CO, ST		0..255	AC_CO_O
stVal	CODED ENUM	ST	dchg	intermediate-state off on bad-state	M
q	Quality	ST	qchg		M
t	TimeStamp	ST			M
stSeld	BOOLEAN	ST	dchg		AC_CO_O
substitution					
subEna	BOOLEAN	SV			PICS_SUBST
subVal	CODED ENUM	SV		intermediate-state off on bad-state	PICS_SUBST
subQ	Quality	SV			PICS_SUBST
subID	VISIBLE STRING64	SV			PICS_SUBST
configuration, description and extension					
pulseConfig	PulseConfig	CF			AC_CO_O
ctlModel	CtlModels	CF			M
sboTimeout	INT32U	CF			AC_CO_O
sboClass	SboClasses	CF			AC_CO_O
d	VISIBLE STRING255	DC		Text	O
dU	UNICODE STRING255	DC			O
cdcNs	VISIBLE STRING255	EX			AC_DLNDA_M
cdcName	VISIBLE STRING255	EX			AC_DLNDA_M
dataNs	VISIBLE STRING255	EX			AC_DLN_M

Vendors compose real protection and control devices

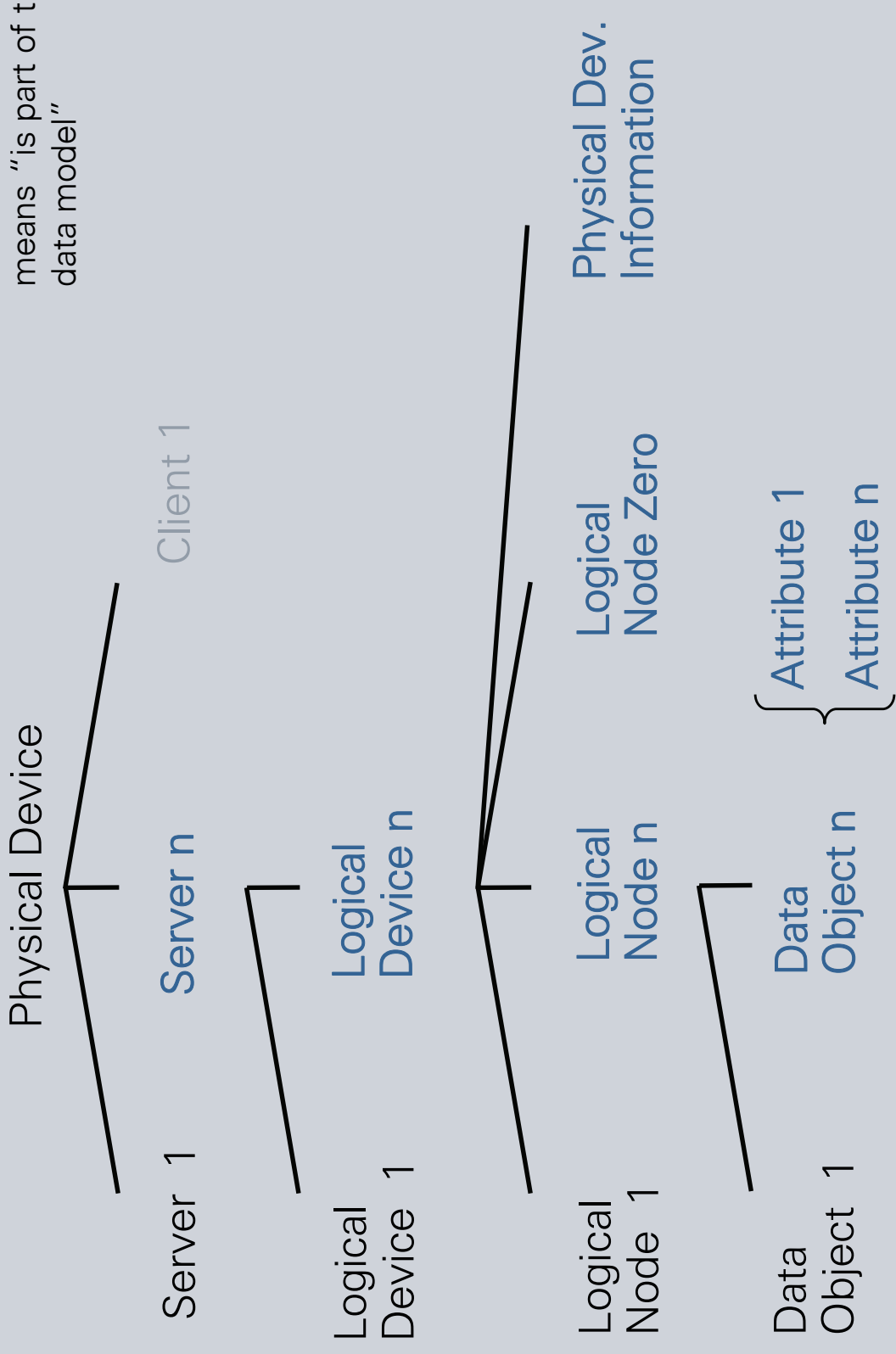


IEC 61850-7: Addressing “Circuit Breaker”



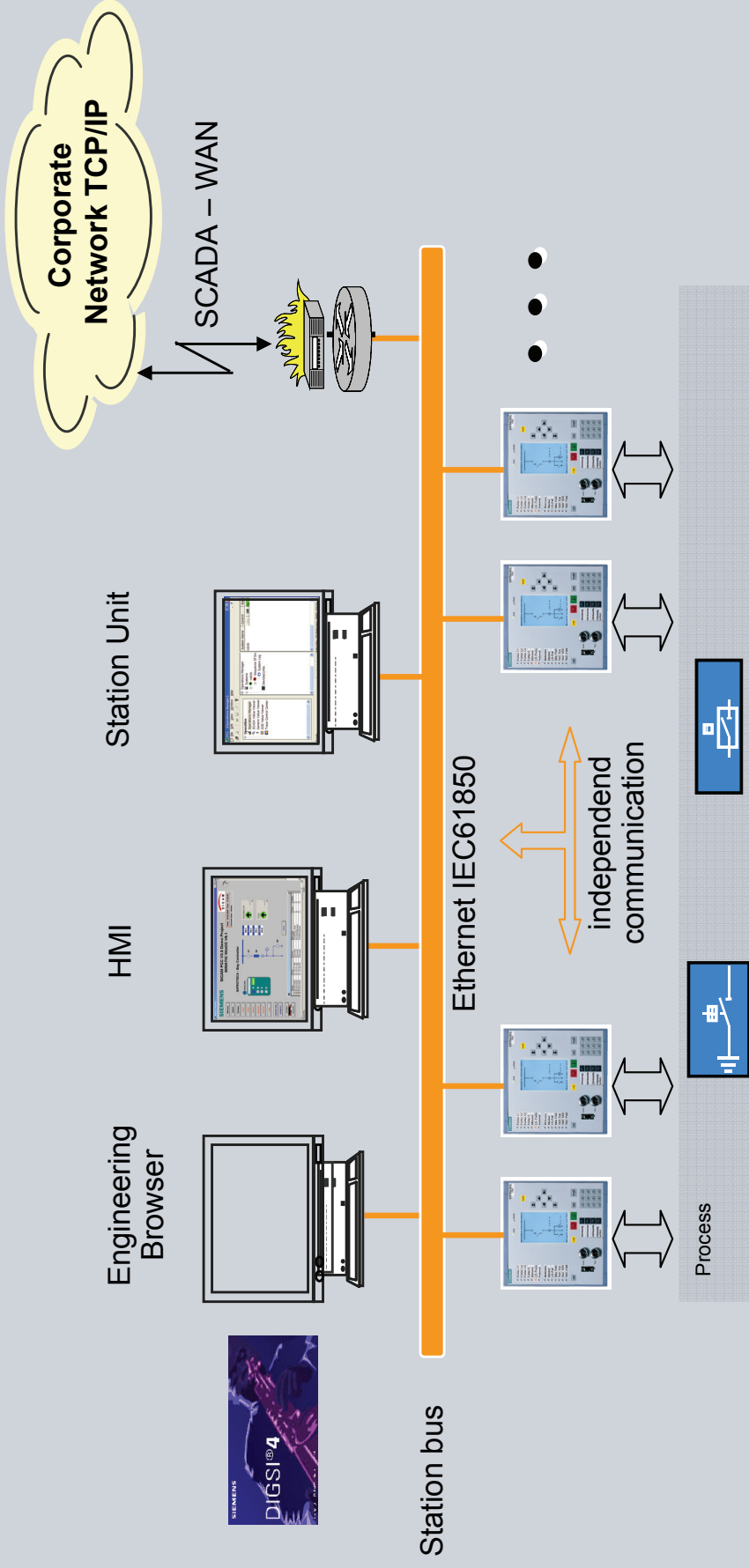
Hierarchy of the Data Model

blue coloured words means "is part of the data model"



distributed intelligence

- no more classic Master/Slave configuration and no bottle neck.
- Client / Server architecture
- Peer-to-peer (publisher / subscriber) architecture



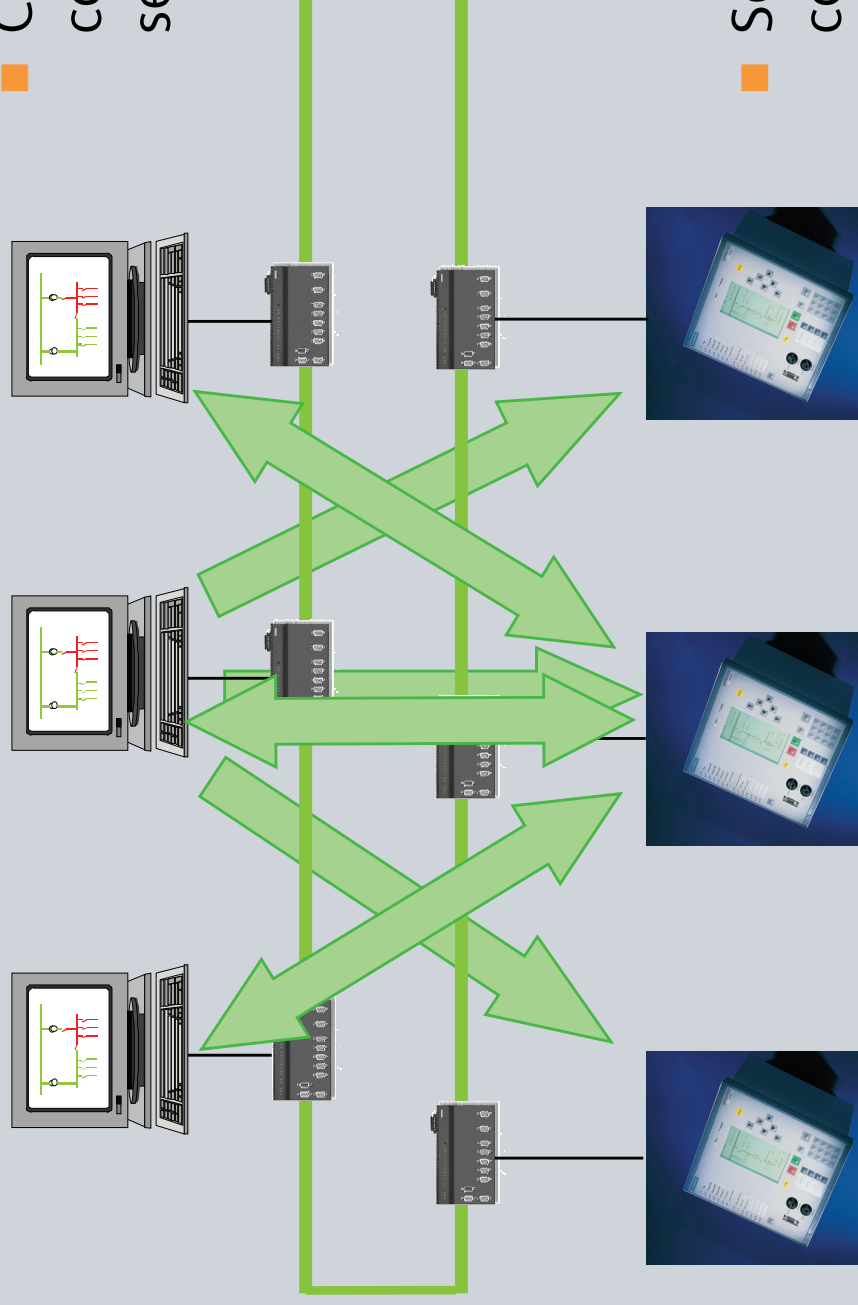
- Control
- Buffered and Unbuffered Information Report
- Logging
- GOOSE (for fast inter-device communication)
- Substitution
- Setting Group
- Sampled Value
- Time Synchronisation (SNTP)
- File Transfer (MMS-File Transfer, FTP)

GOOSE –Generic Object Oriented Substation Event

Client / Server architecture

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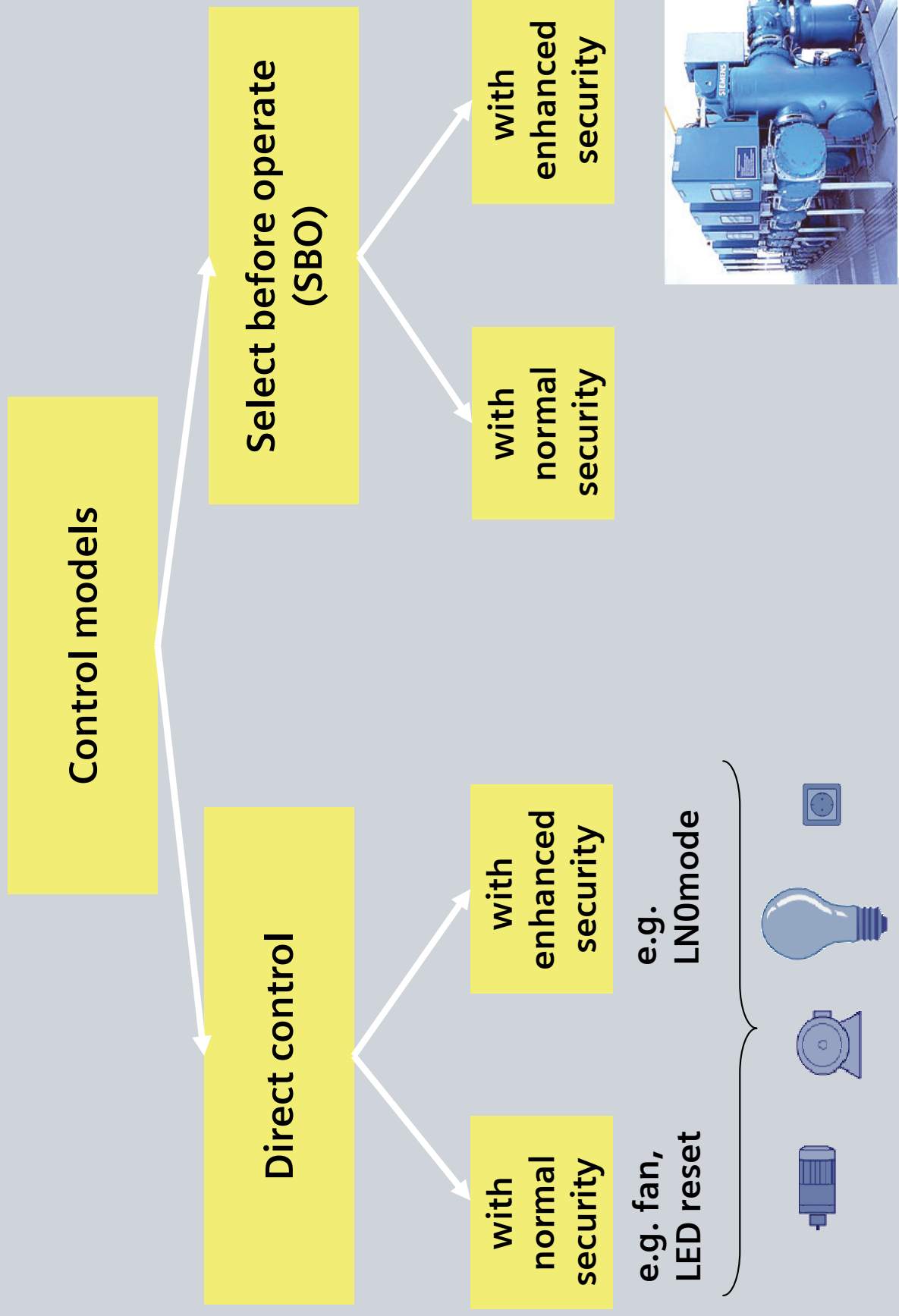
- Client keeps connection to several servers.



- Server supports connection to several clients simultaneously.

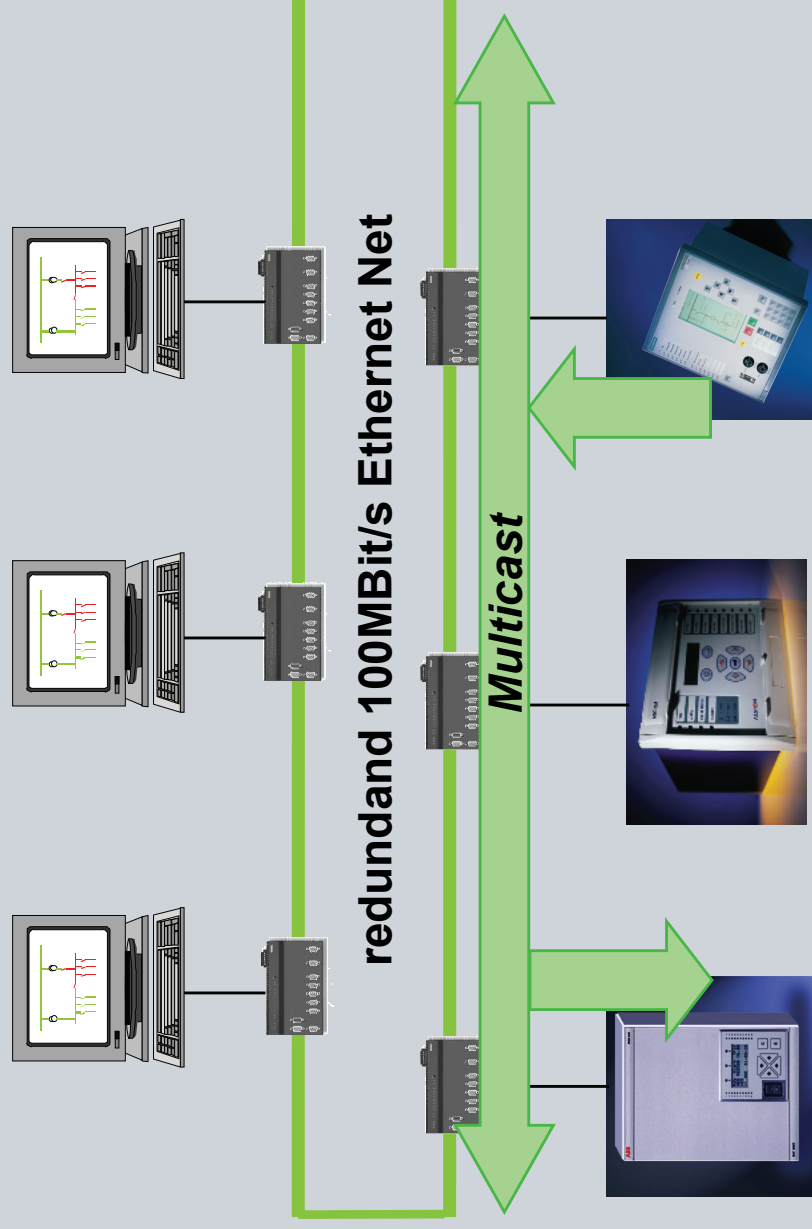
- Report is more efficient than polling
- Report is transmitting data based on a condition being met: change of state, value, quality attribute, time-out

Control models in IEC 61850



Fast Inter-Device Communication (GOOSE)

A device sends the published information by multicast .
A subscriber receives this message.



IEC 61850 – GOOSE principle

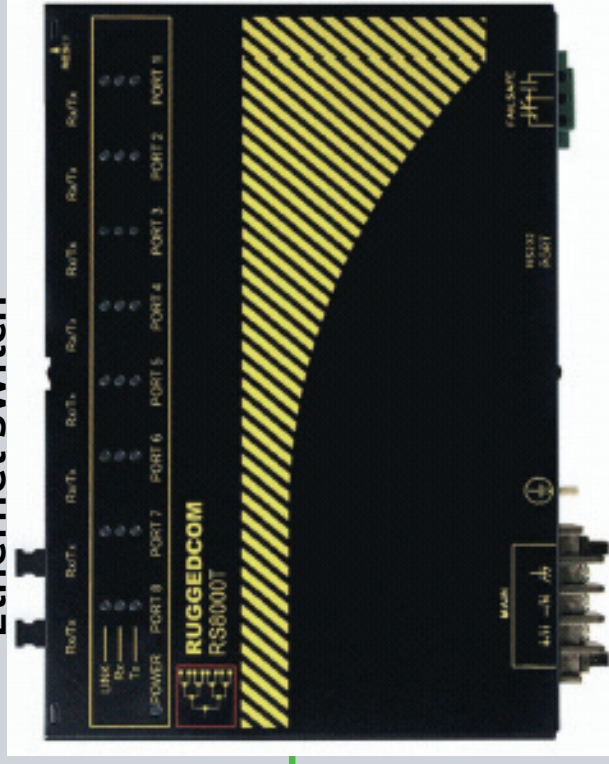
Prioritization (tagging) of GOOSE-Telegrams

Ethernet Switch

fast

GOOSE

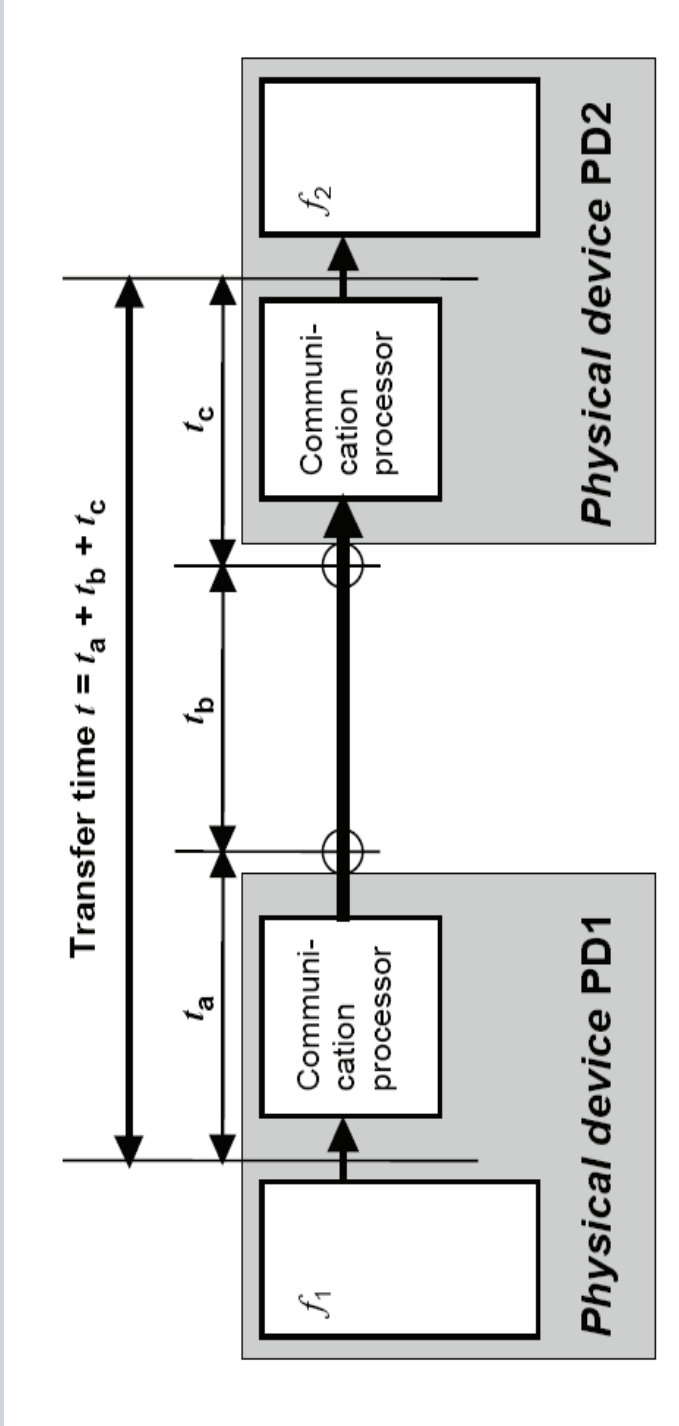
Normal Telegrams



Only IEC 61850 uses the possibilities of the modern 100 MBIT-Ethernet.

Not UCA2.0, **not** DNP, **not** T104 !

Transfer time in IEC 61850-5

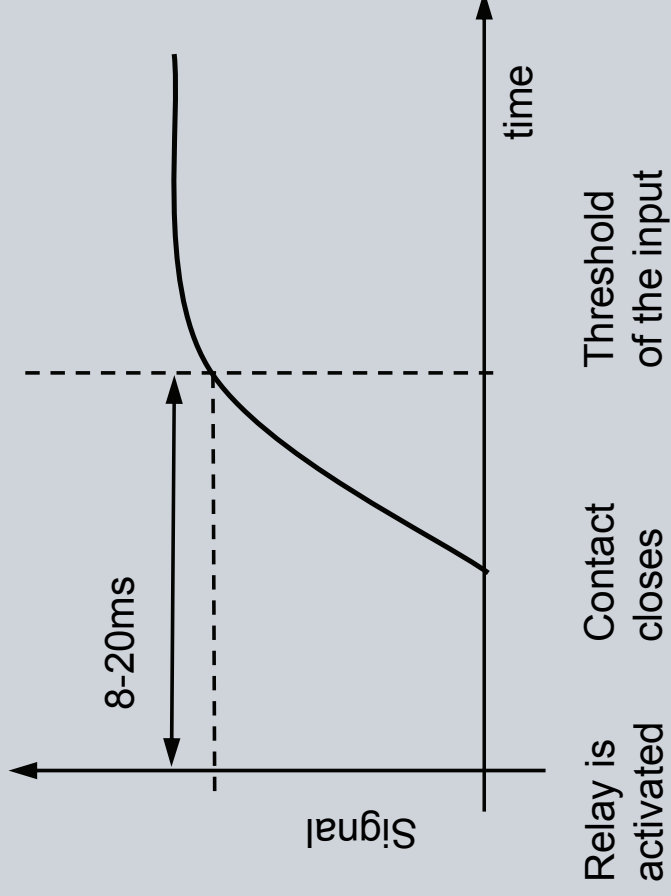


(from IEC 61850-5)

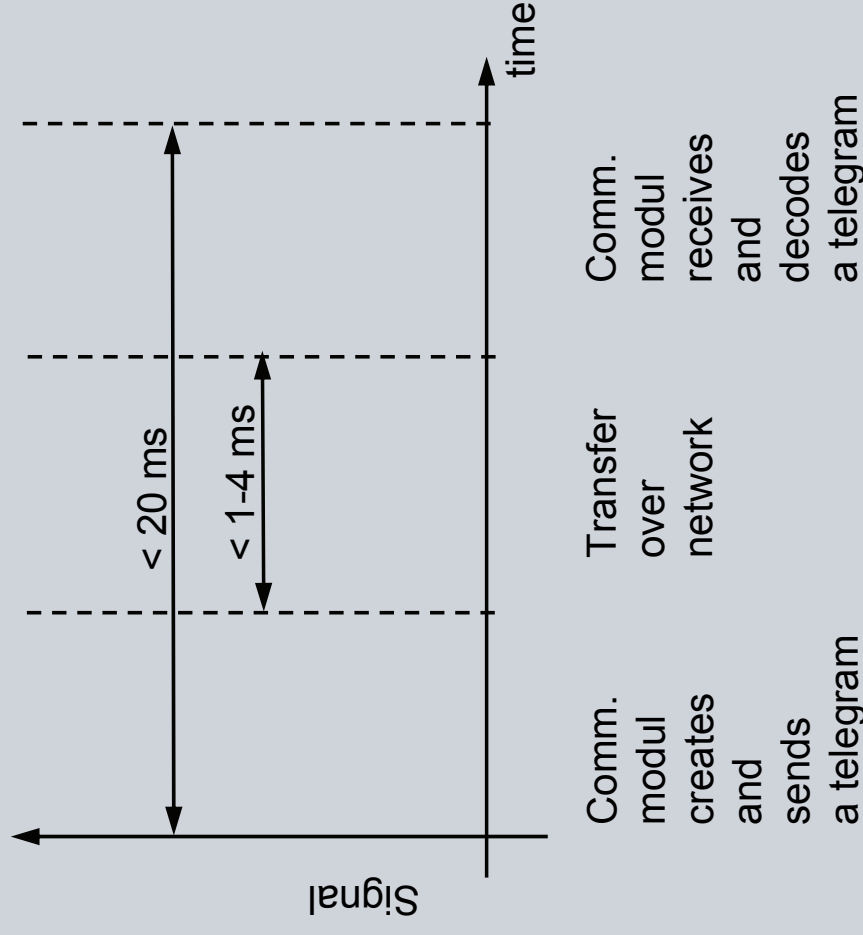
	Fast messages Trip others		Medium speed messages	Low speed messages
Distribution (P1)	10ms	100ms	100ms	500ms
Transmission (P2/P3)	3ms	20ms		

Hardwired signal transmission between bays

Output- / Input Signal (schematic)



Use of GOOSE with prioritizing and multicast filtering (principle)

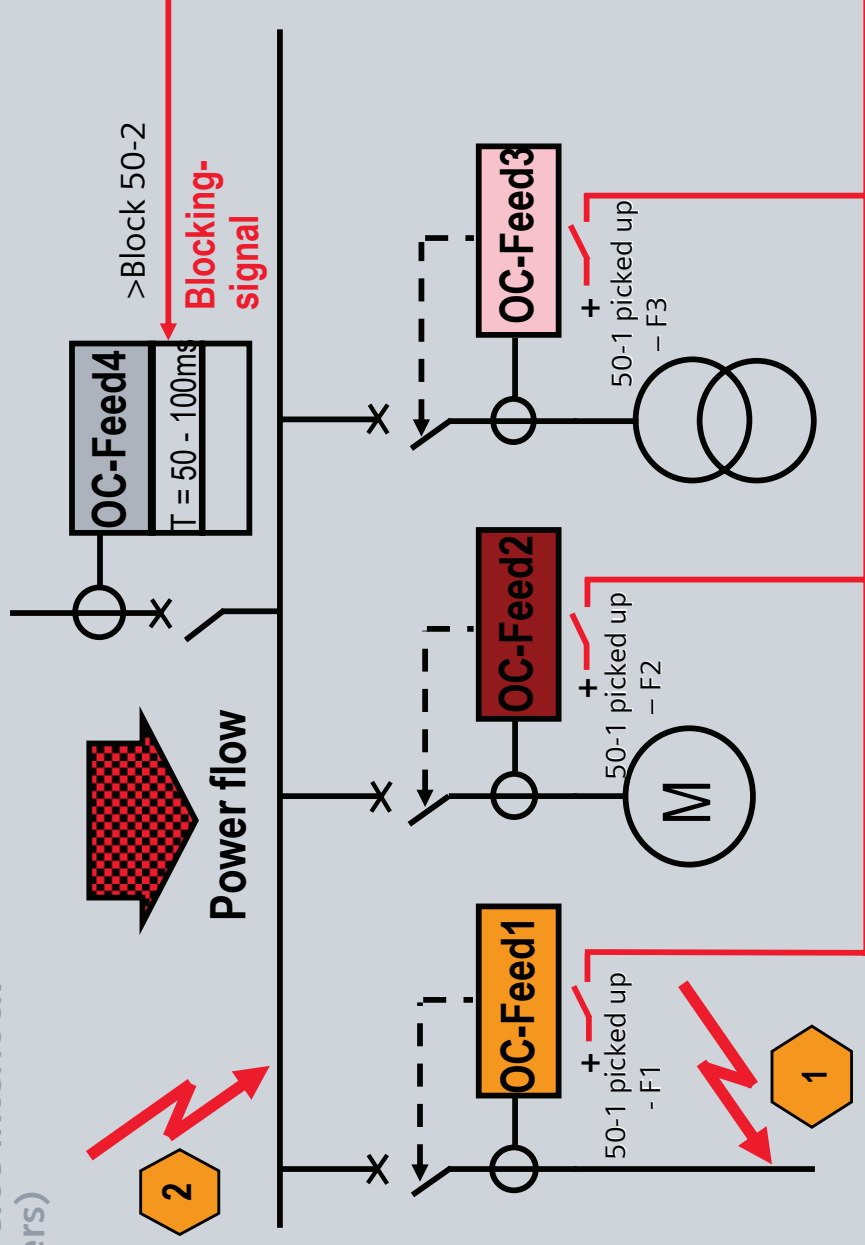


Example for IEC 61850–GOOSE

Principle of reverse interlock

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Principle of reverse interlock
(ANSI – numbers)



1

Overcurrent protection of outgoing feeders blocks the 50-2 stage ($I > I_{set}$) of the overcurrent protection of the incoming feeder (OC-Feed4) with the pick-up signal of OC-functions 50-1 ($I > I_{set}$).

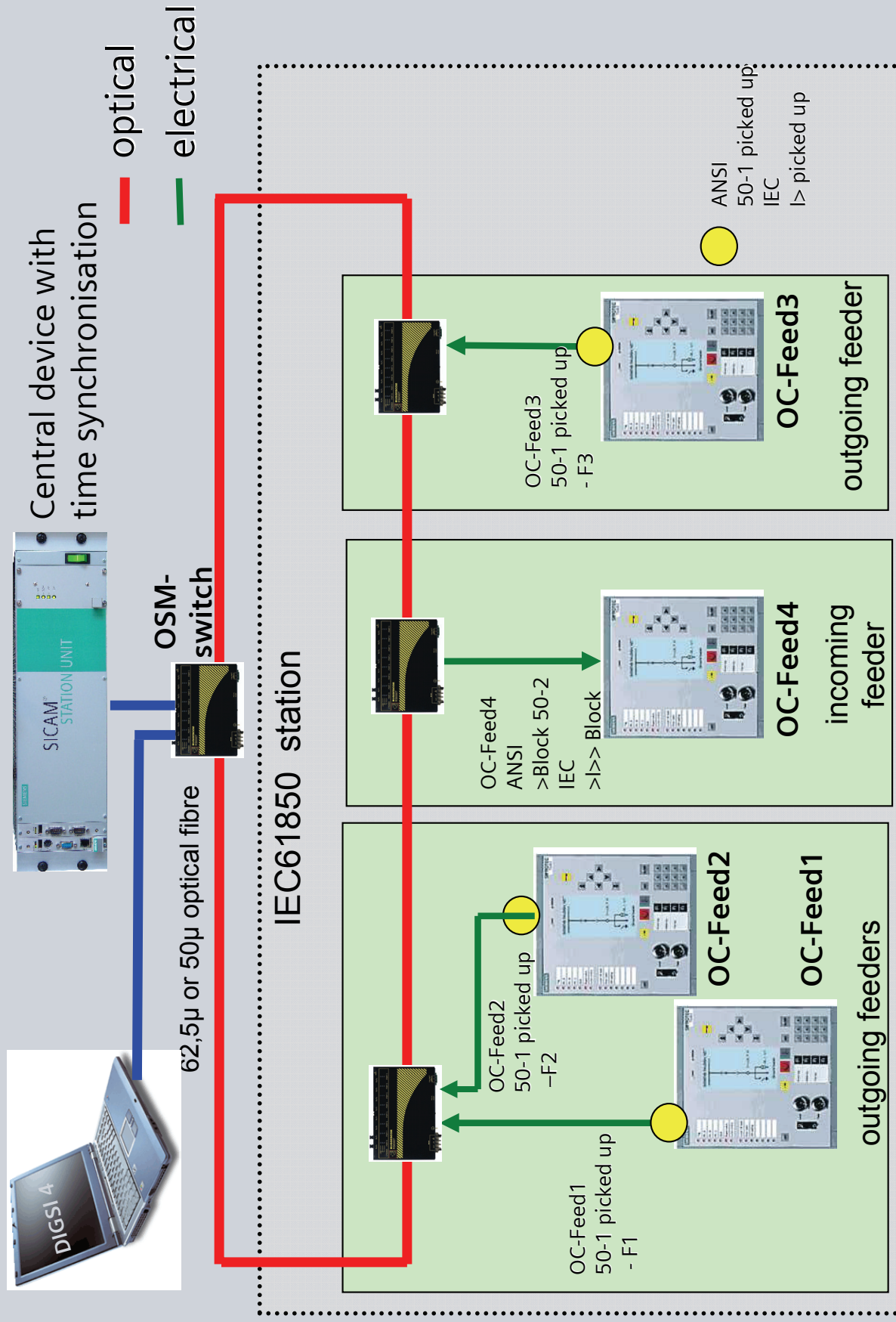
2

50-2 ($I > I_{set}$) stage of the overcurrent protection of the incoming feeder sends a trip signal after 50-100 ms, when no blocking signal is received from one or more overcurrent protection of the outgoing feeders.

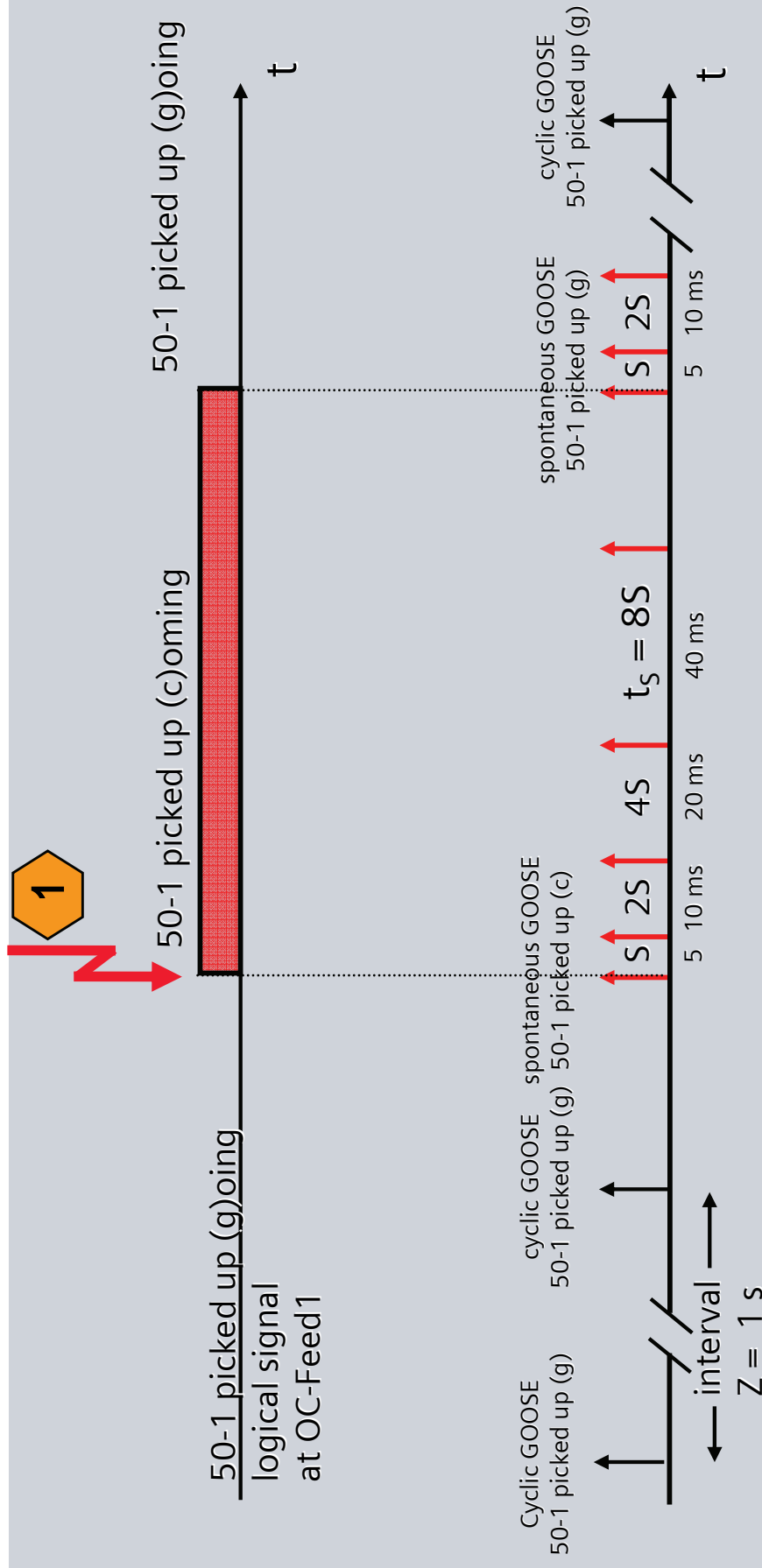
Exchange of binary information (single messages) between devices
Contacts -> Binary input (wiring between the devices)

Example on IEC 61850–GOOSE Topology of Ethernet Station-bus

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How GOOSE works according to IEC 61850: Cyclic and spontaneous GOOSE messages



- cycle interval e.g. $Z = 1\text{ s}$ (for monitoring of the status of received GOOSE messages at the receiver: here OC-Feed4)
- switch from cyclic to spontaneous when signal changes (50-1 pick up (c))
- N spontaneous repeats $t_s = 2^N \cdot S$ ($N=0,1,2,3\dots$ for $t_s < Z$, $S = 5\text{ ms}$)
- switch from spontaneous to cyclic when $t_s > Z$

1. Control

- Select before Operate (SBO) with enhanced security → all commands to the HV-process
- Direct Control with normal security → all auxiliary controls

2. Information Report

- all information in monitoring direction to the PAS-substation controller

3. GOOSE

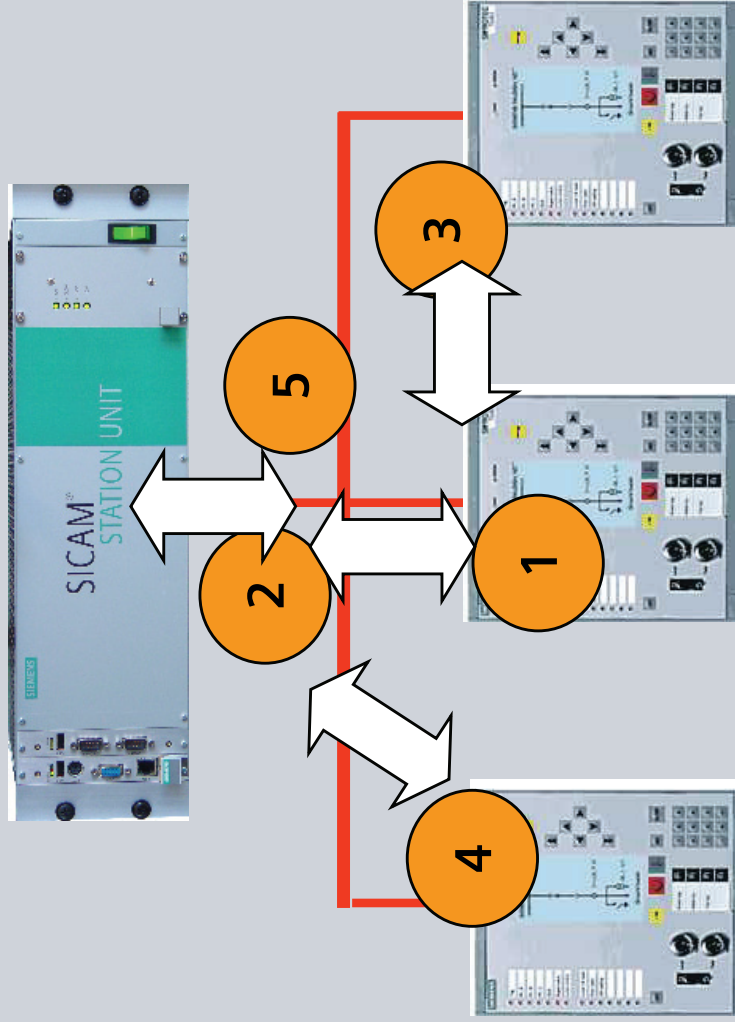
- Inter-device communication → Interlocking, Blocking etc.

4. File Transfer

- Alarm lists, Event lists, SOE
- Transmission of fault records

5. Time Synchronisation

etc.



Use of Services for SAS-Applications (1)

SAS-Application	Service in IEC 61850-7-2	Mapping IEC 61850-8-1	Remarks
Control	Select before operate (SBO) with enhanced security Direct control with normal / enhanced security	MMS-Write MMS-InformationReport	SBOwES necessary for HV equipment for of safety reasons
Monitoring, Reporting, SCADA	Unbuffered reporting	MMS-InformationReport	InformationReport controls by change of state, value, qua-lity for spontanous change of informa-tion; with polling loss of information
Interbay communicaton for e.g. exchange of status information for interlocking, blocking of protection functions etc.	GOOSE	Direct on EthernType	Multicast messaging with priorization by tagging in the EthernTypes

Use of Services for SAS-Applications (2)

SAS-Application	Service in IEC 61850-7-2	Mapping IEC 61850-8-1	Remarks
Change of parameter sets	Substitution Activation of parameter sets	MMS-Write	
Time synchronisation	Standardized Services	SNTP	
Transmission of fault records with file transfer	GetFile GetFileAttributeValues, GetDirectory	MMS-fileRead, MMS-Optainfile	
General interrogation	Unbuffered Reporting	MMS-InformationReport	
Self Monitoring of SAS	-	IEC 61850-Keep alive process for servers GetDomainList for clients	Automatically checked
Engineering	OPC-server (like in MMS-explorer) can only be configured online (real devices while engineering are necessary, IEC61850 defines engineering with substation configuration description language (SCL) with the systemconfigurator-tool		

Fully redundant →

optimized for communication to bay
controller / Protection relays

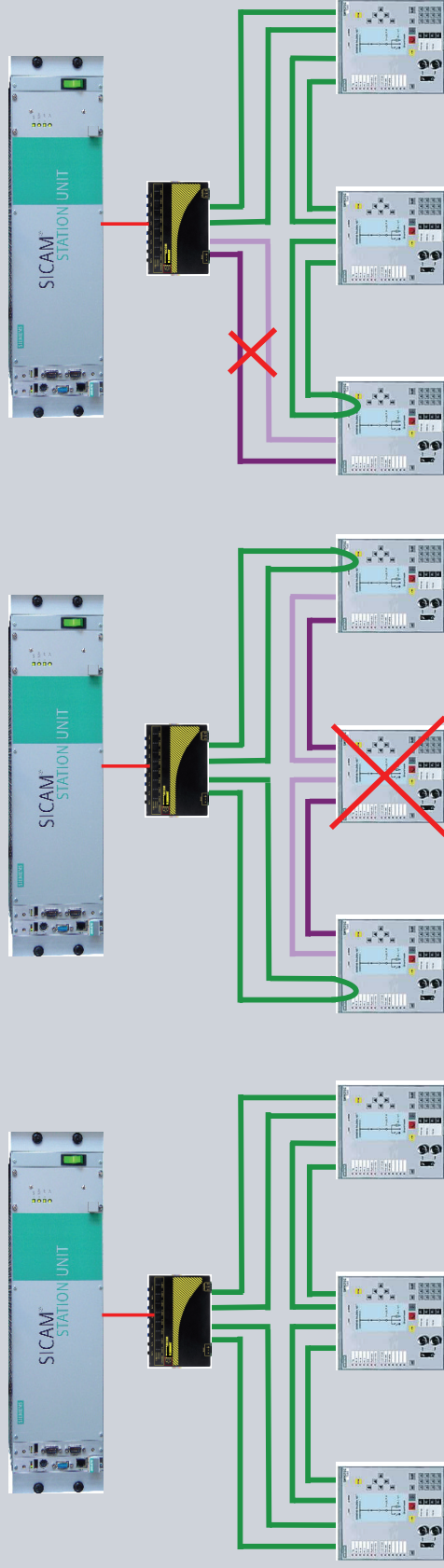
Self healing mechanisms for high reliability



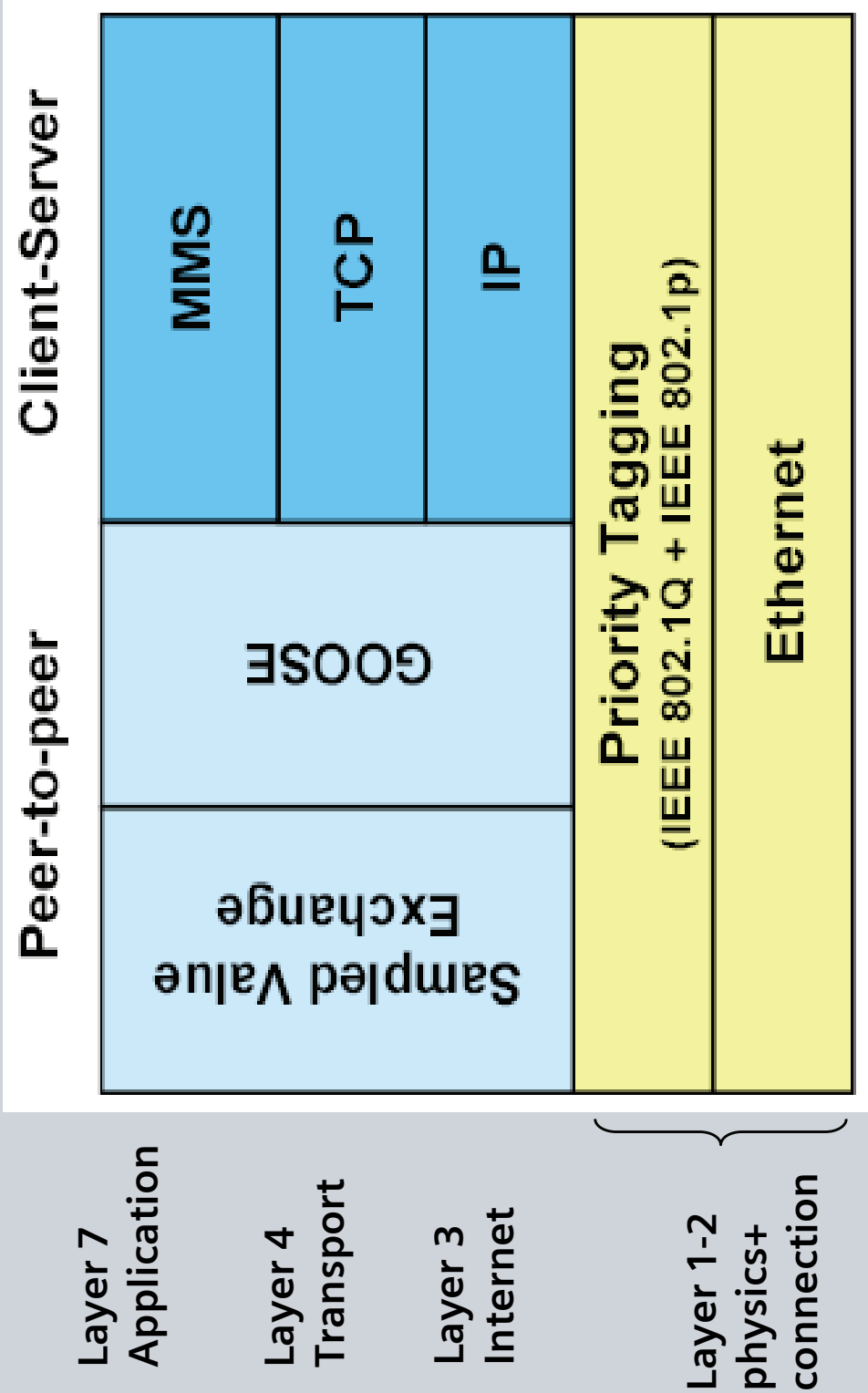
◆ OFC Ring (fullduplex)

◆ Device failure

◆ OFC failure



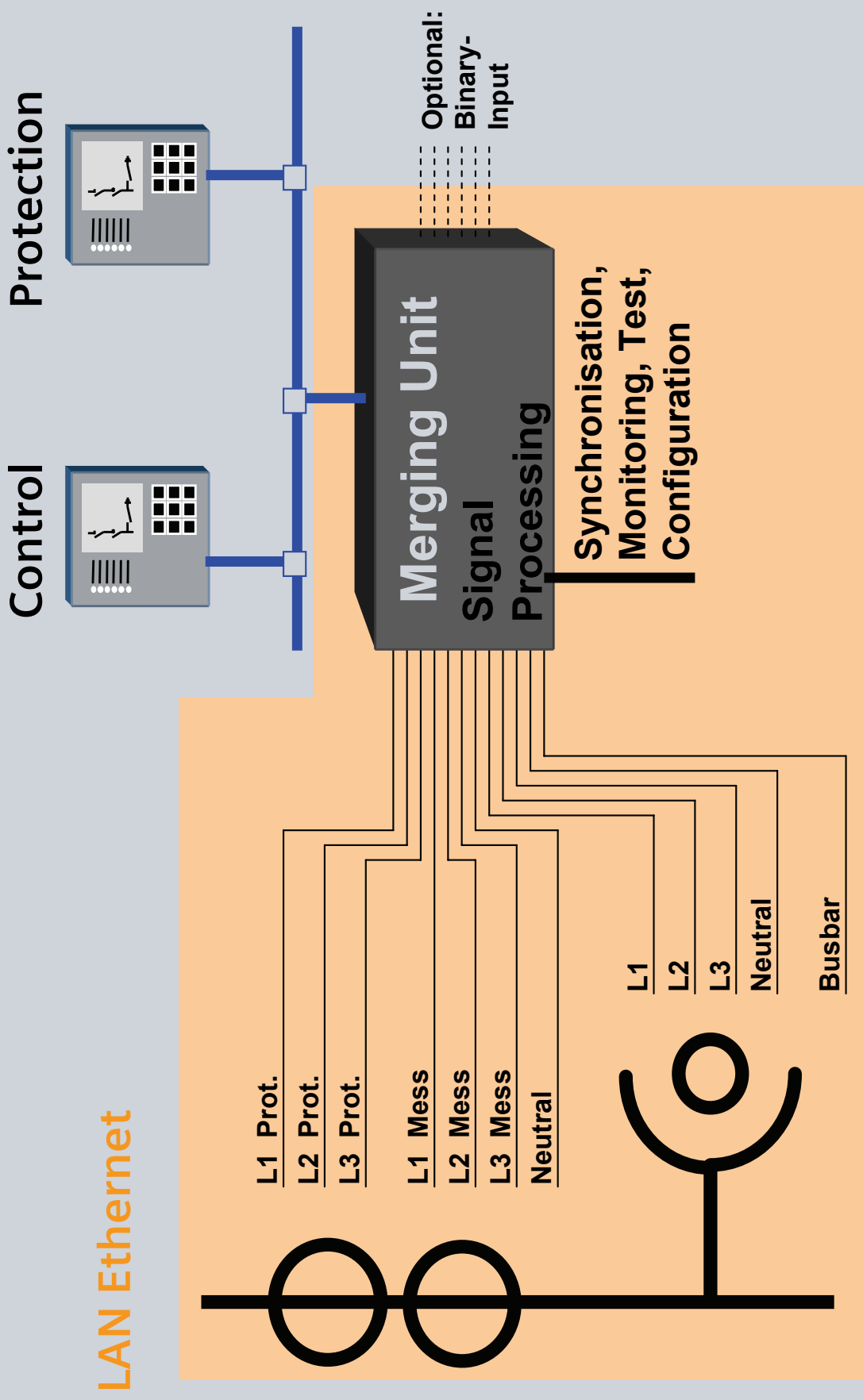
Protocol stack of IEC 61850



Benefits of IEC 61850-9-2 Process Bus

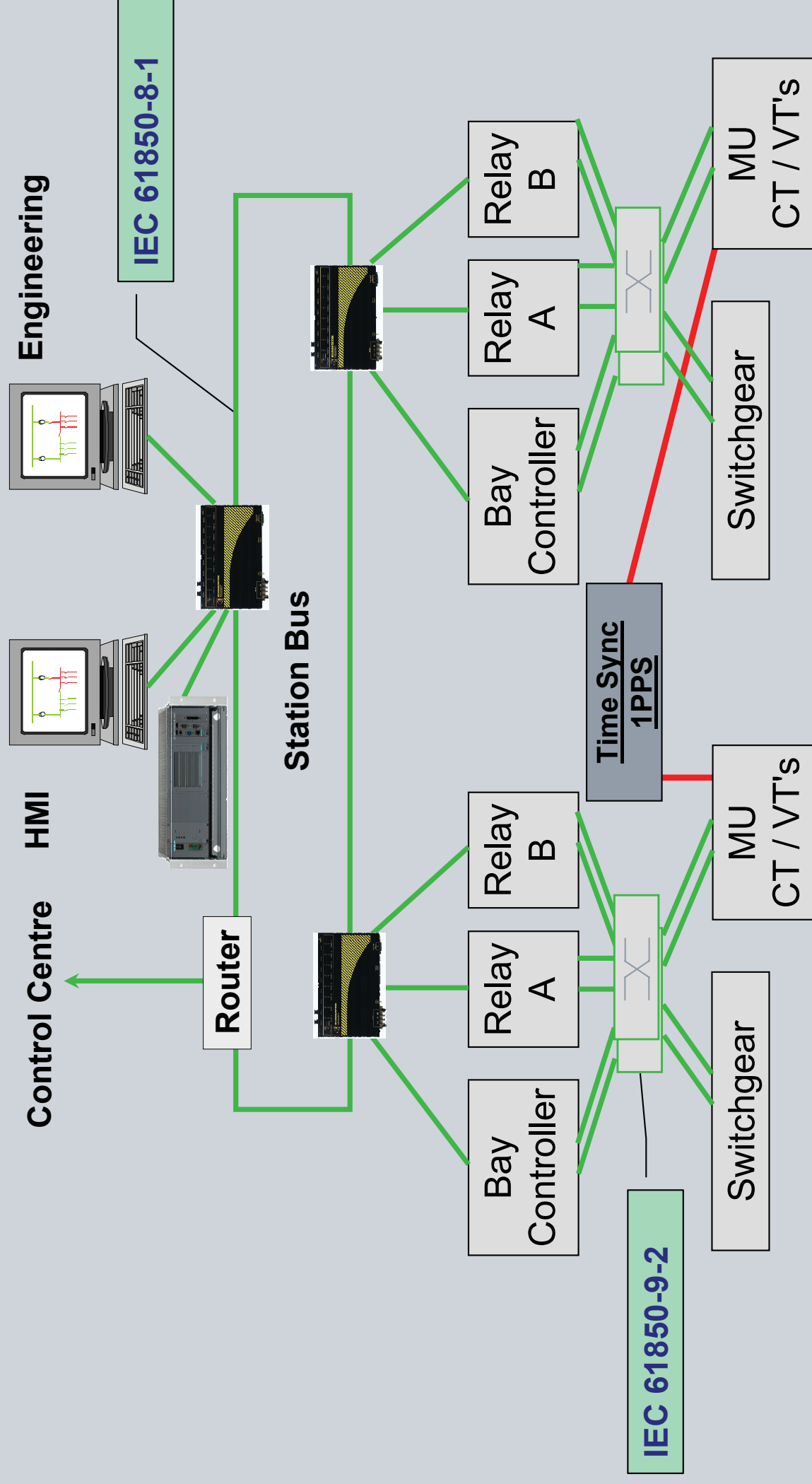
- Standardized communication interface on Ethernet
- Enabling Non Conventional Instrument Transformer Technology
- Saves cables and other hardware structures
- Saving engineering efforts
- Eases installation and maintenance
- Base for intelligent switchgear and extended monitoring features

Transmission of Sampled Values: basic system



System architecture with station bus (ring) and process bus (possible conventional configuration)

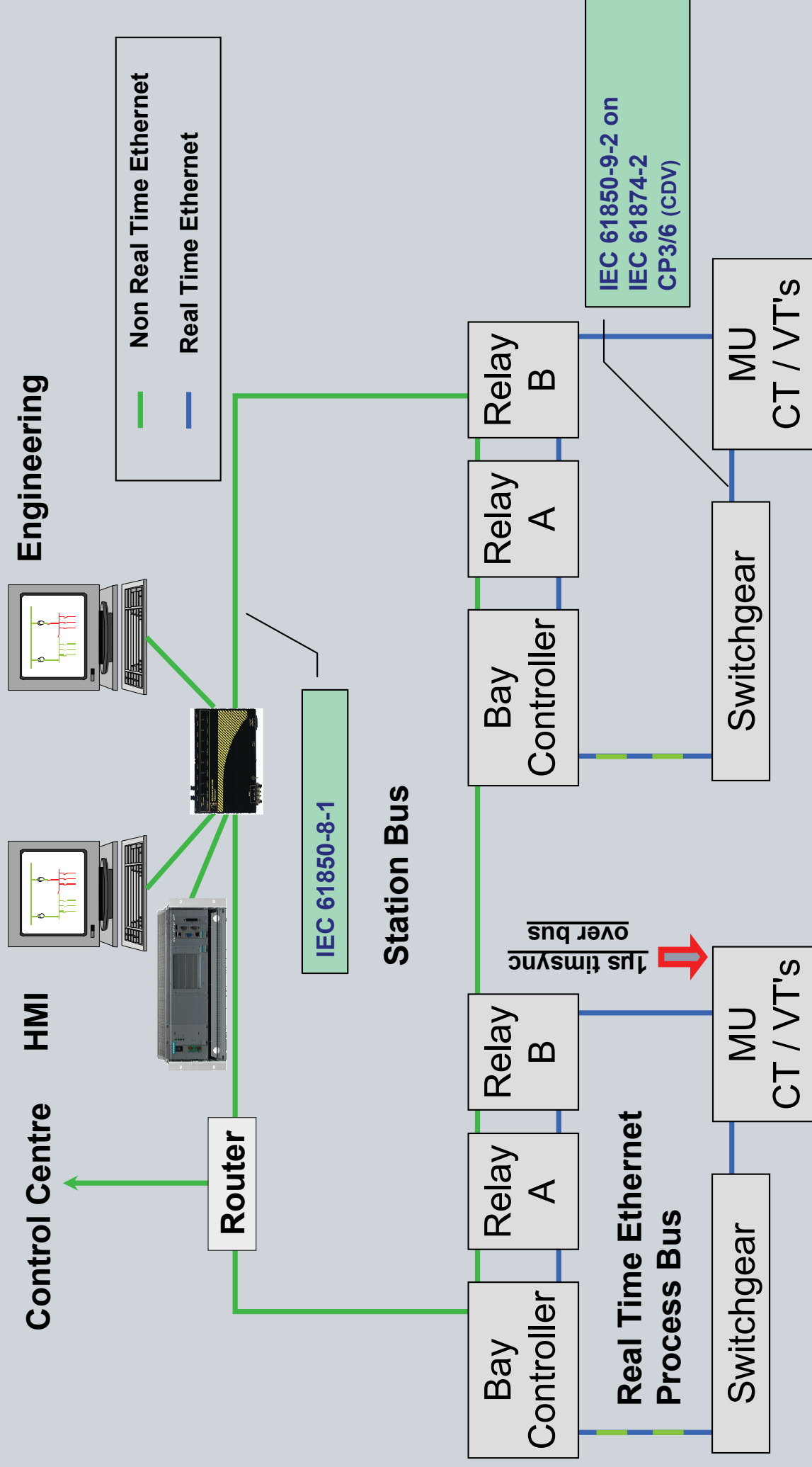
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Benefits of IEC 61850-9-2 based on Real Time Ethernet

- **Real Bandwidth Reservation**
Guaranteed response times
- **No-Dropout Ring Redundancy**
In the case of interruption not even one telegram gets lost
- **< 1 μ s Time Sync via the Ethernet**
IEEE 1688 Precision Time Protocol
20ns time sync jitter pro switching hop
Redundancy for the time sync as well
- **Real Time and non-Real-Time (TCP/IP) on the same wire/fiber**
Monitoring and Controls as well as SV and Trip-GOOSE

System architecture with station bus (ring) and process bus (Real Time Ethernet)

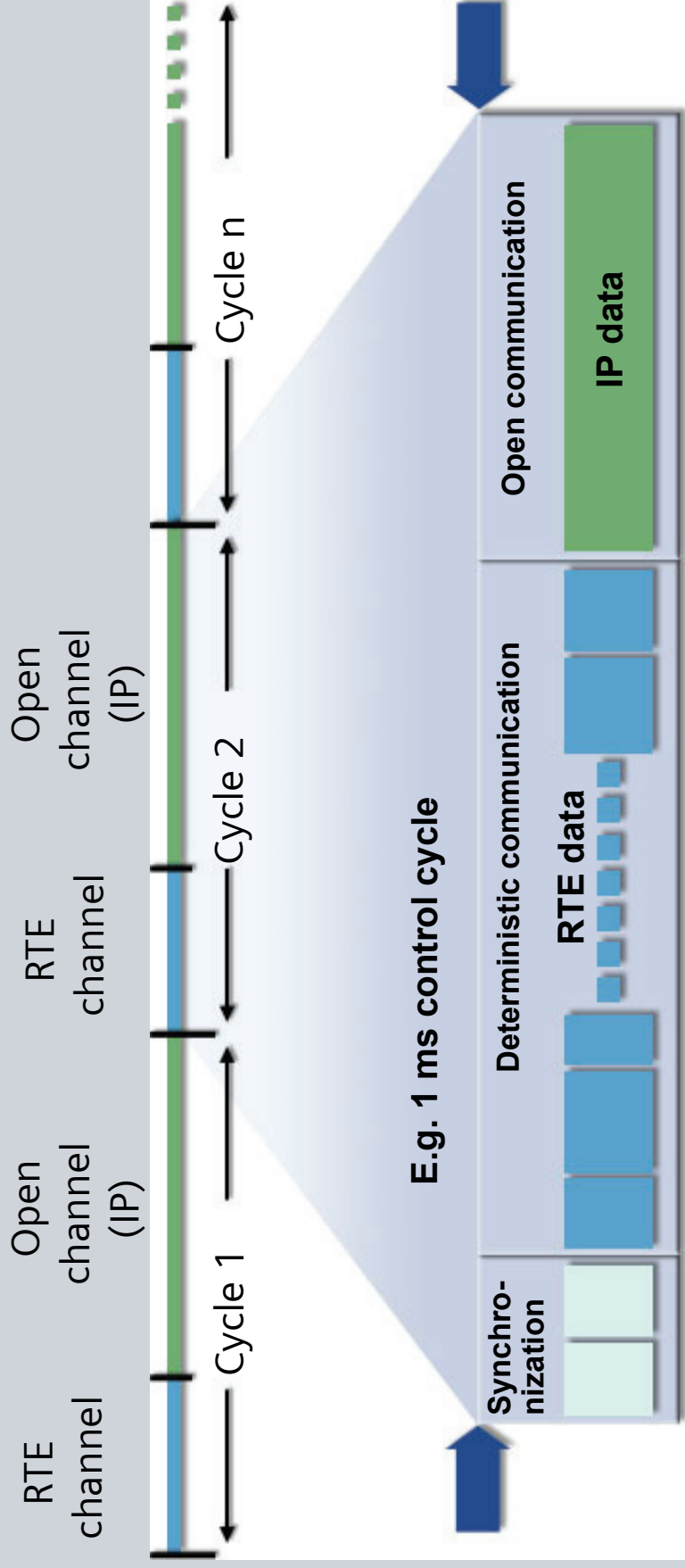


What is new with Real Time Ethernet?

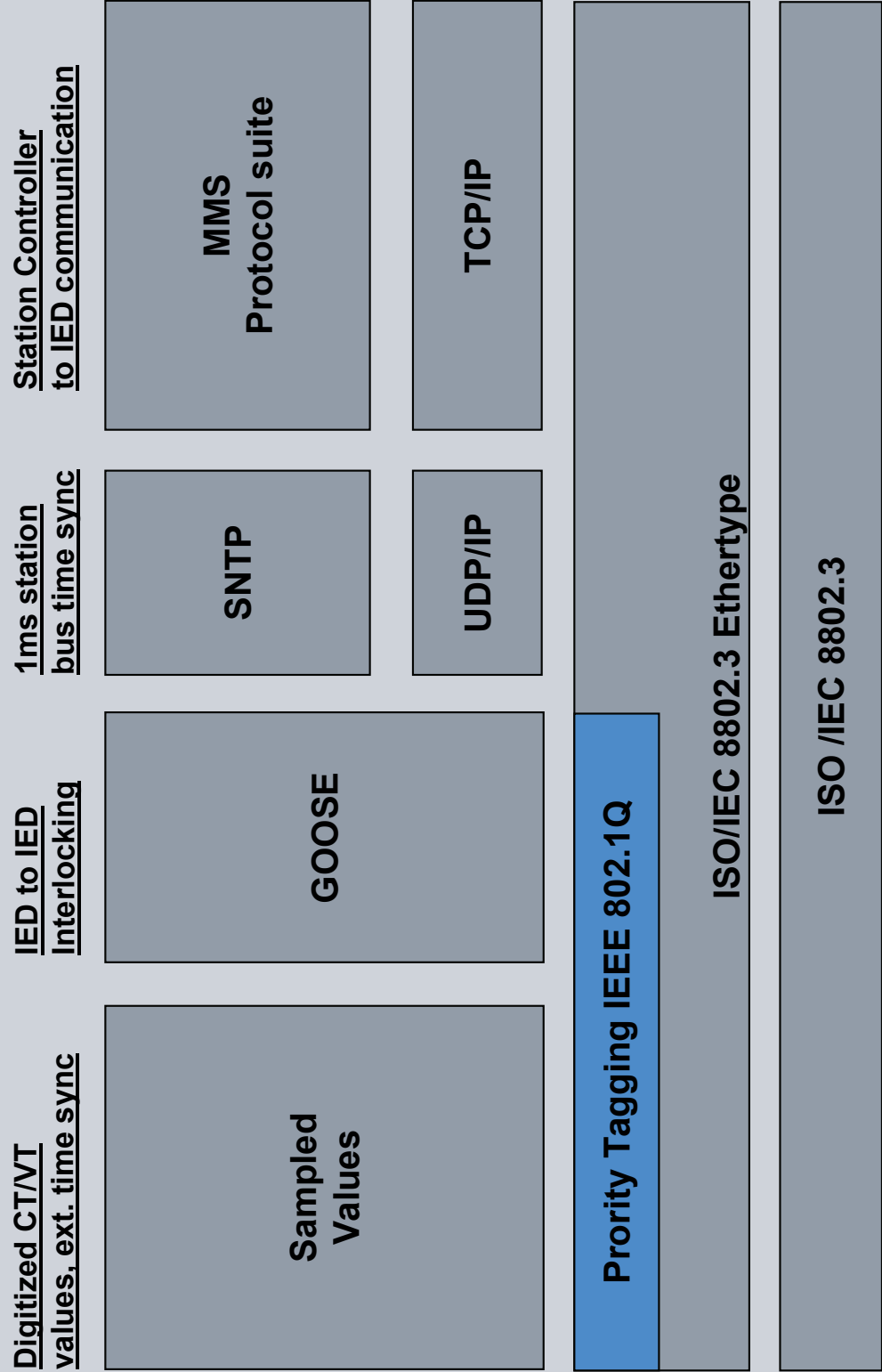


Communication system scheduling

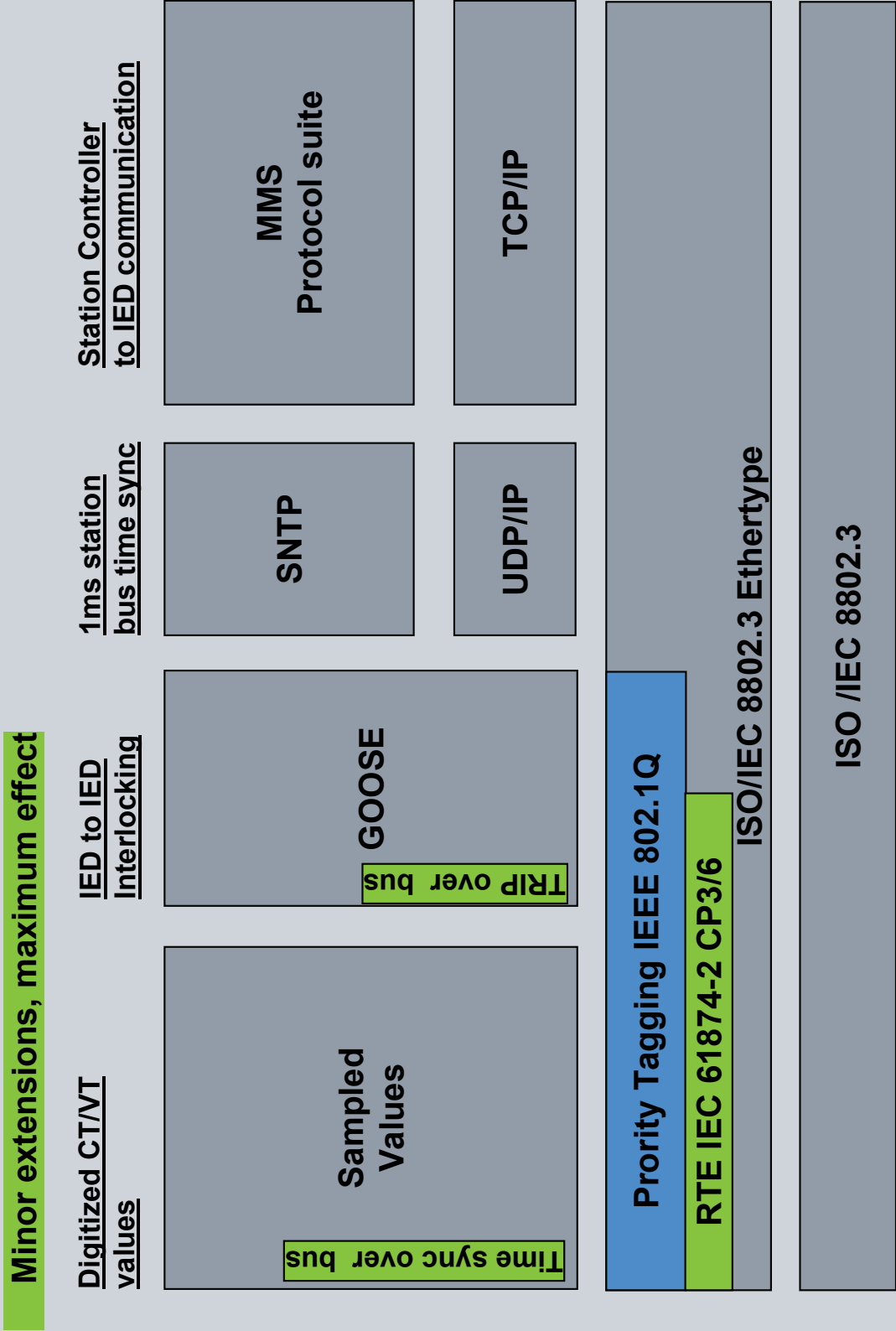
- separate time domains for real-time and non-real-time



Recent IEC 61850 Protocol Stack

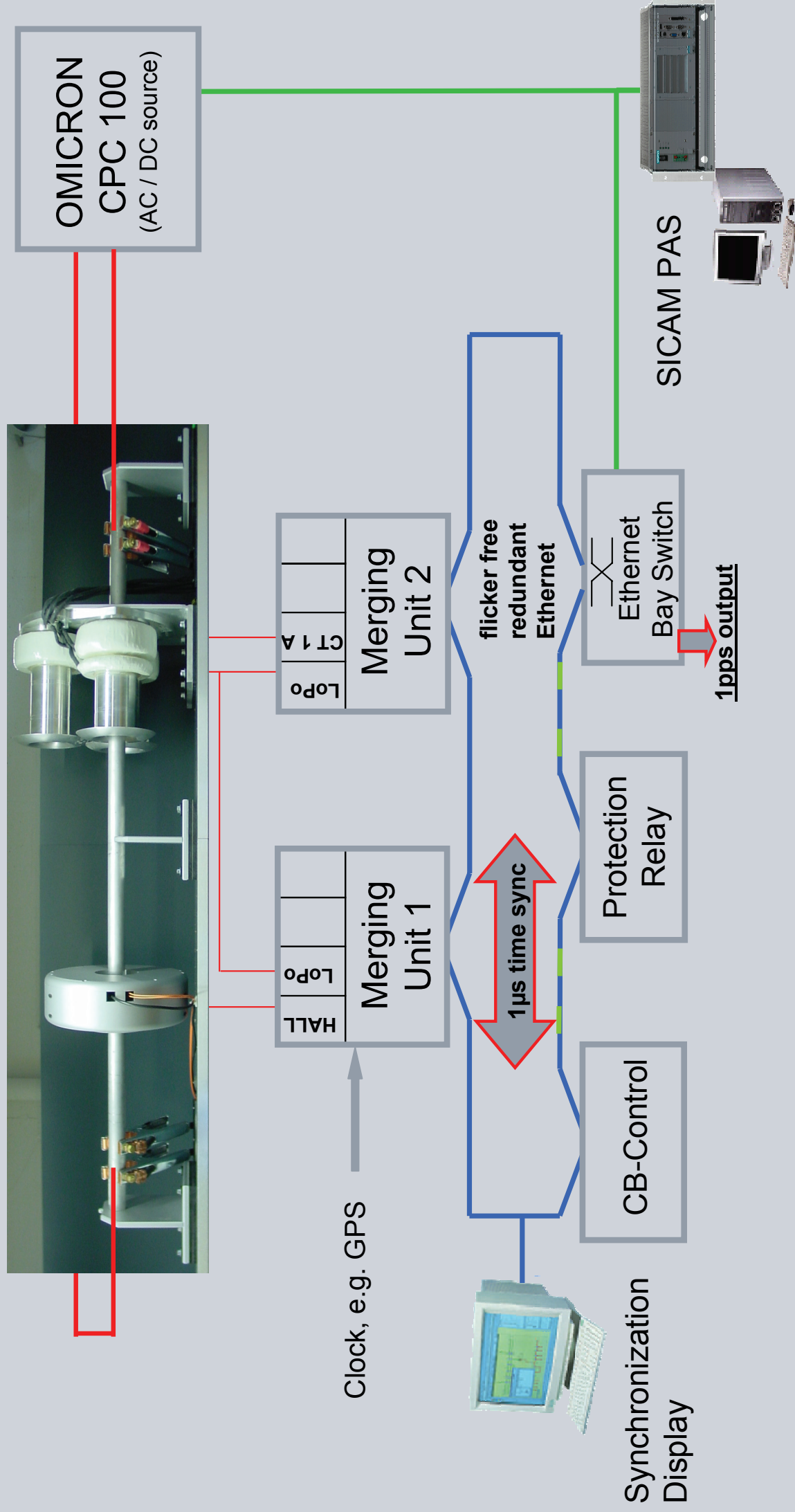


IEC 61850 Protocol Stack combined with RTE



Demo Siemens Stand CIGRE 2006

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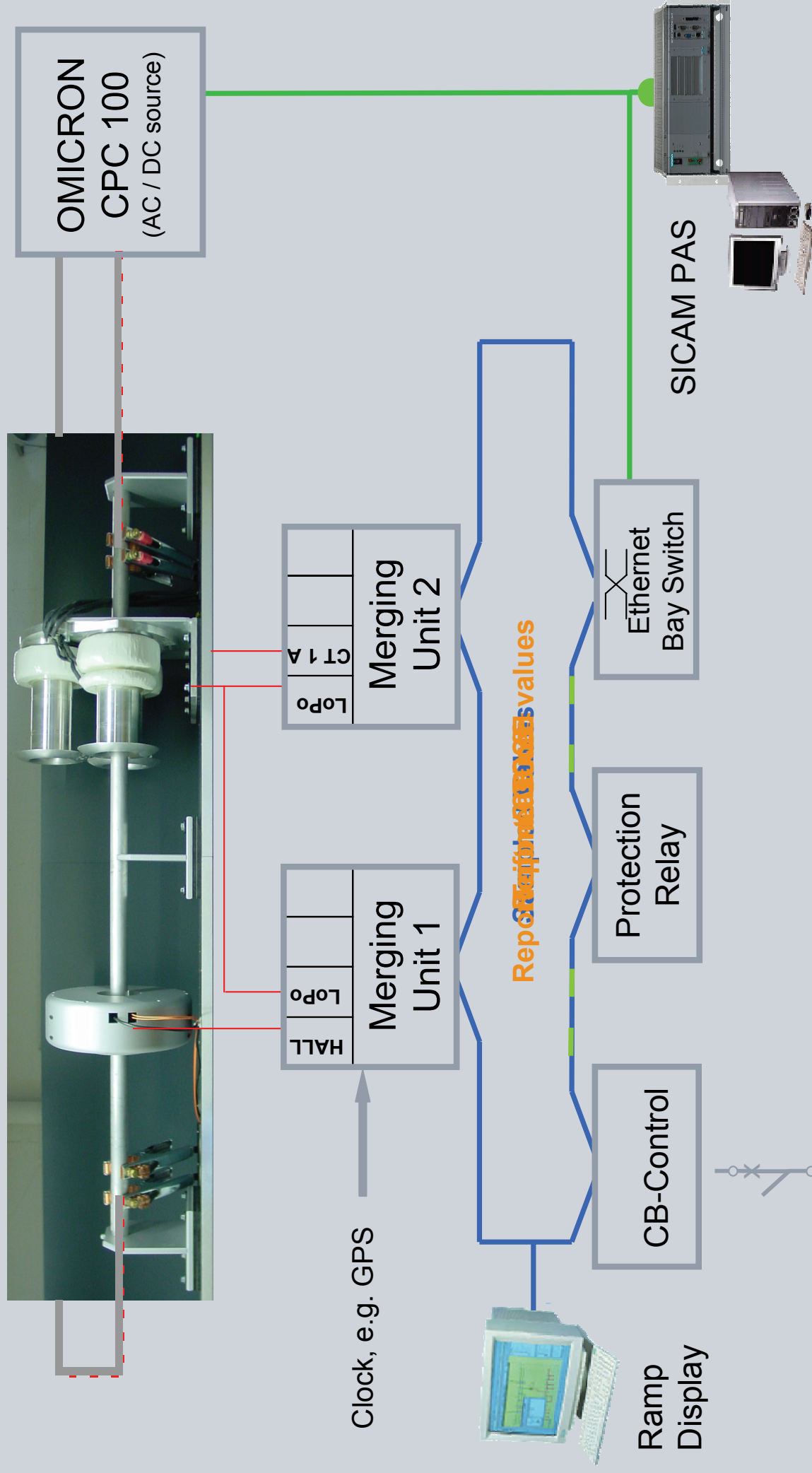


Process Bus Demo Application

- Close CB by a [IEC 61850-8-1 control signal](#) from SICAM PAS
- Closing the CB starts the sequence of Omicron stepwise increasing the current, 300 to 1500 A
- Conventional, LoPo and Hall Sensor connected to both MU's measure the current LoPo is connected to both of the MU's
- Sampled Current is transmitted via [IEC 61850-9-2 LE](#) to the relay.
Relay [reports](#) RMS measures to SICAM PAS
- Protection device sends a [Trip-GOOSE](#) to CB Controller at 1200 A;
Omicron de energizes the line
- CB sends a [report](#) to SICAM PAS

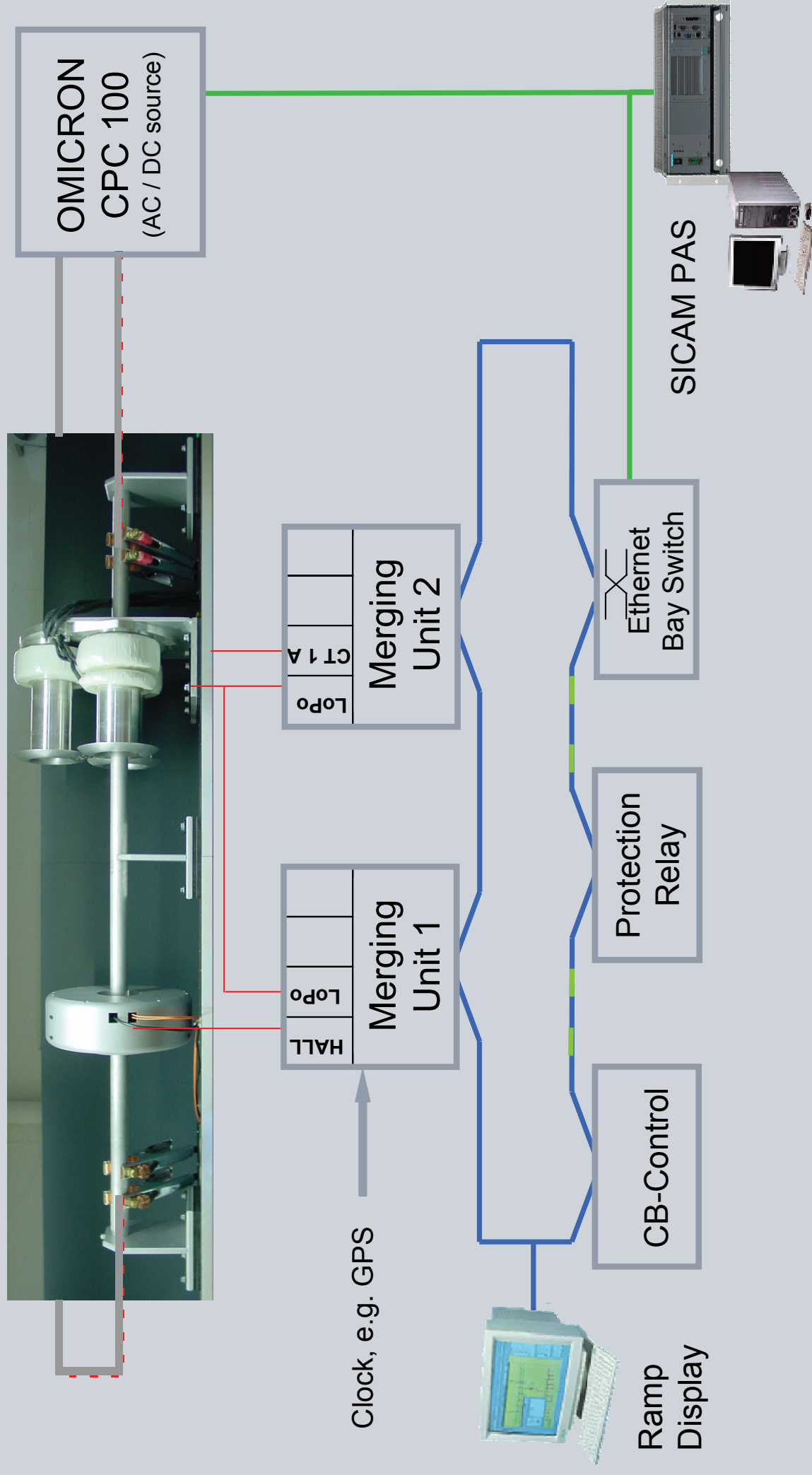
Demo Siemens Stand CIGRE 2006

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Demo Siemens Stand CIGRE 2006

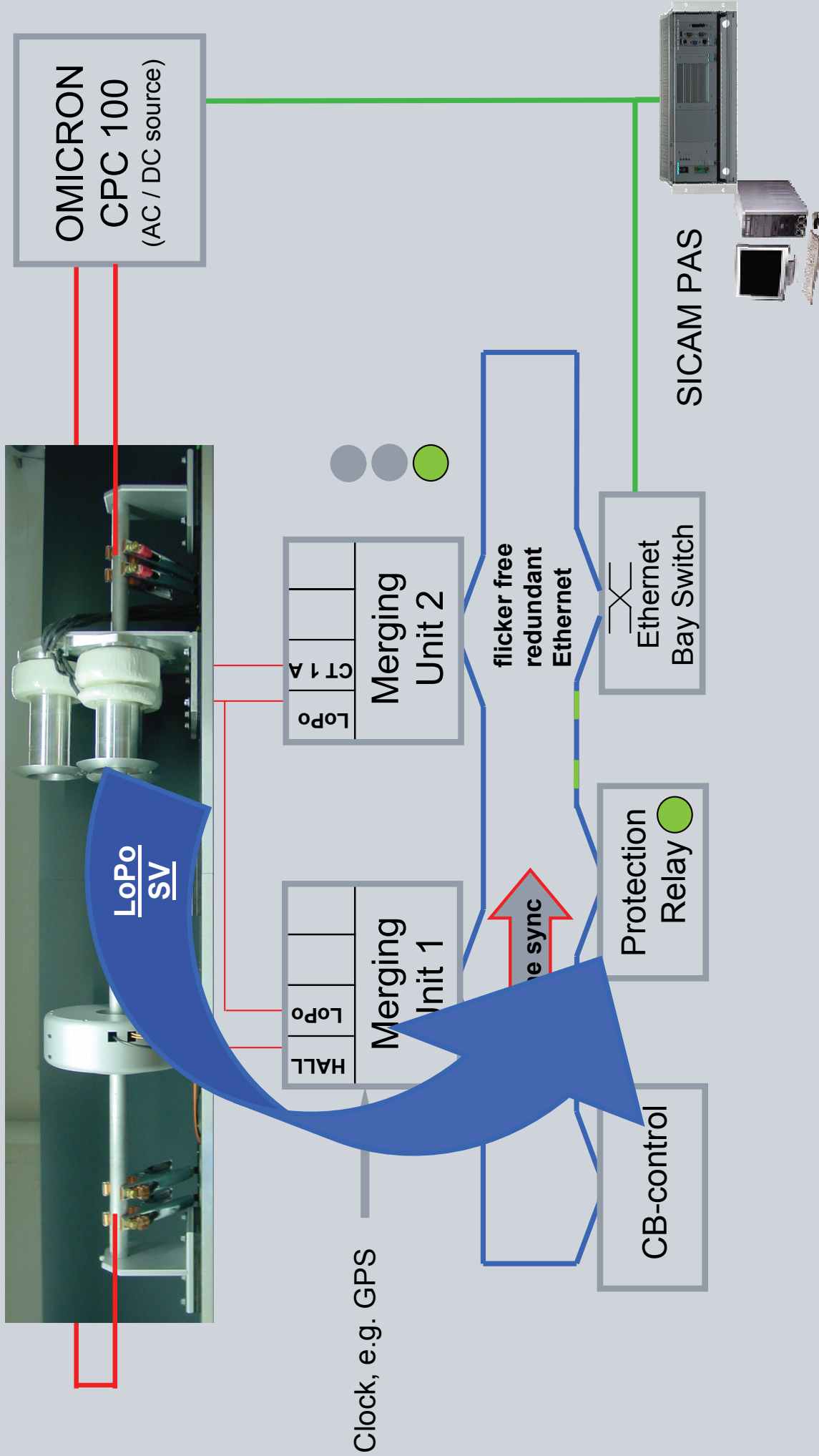
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Evidence: Redundancy:

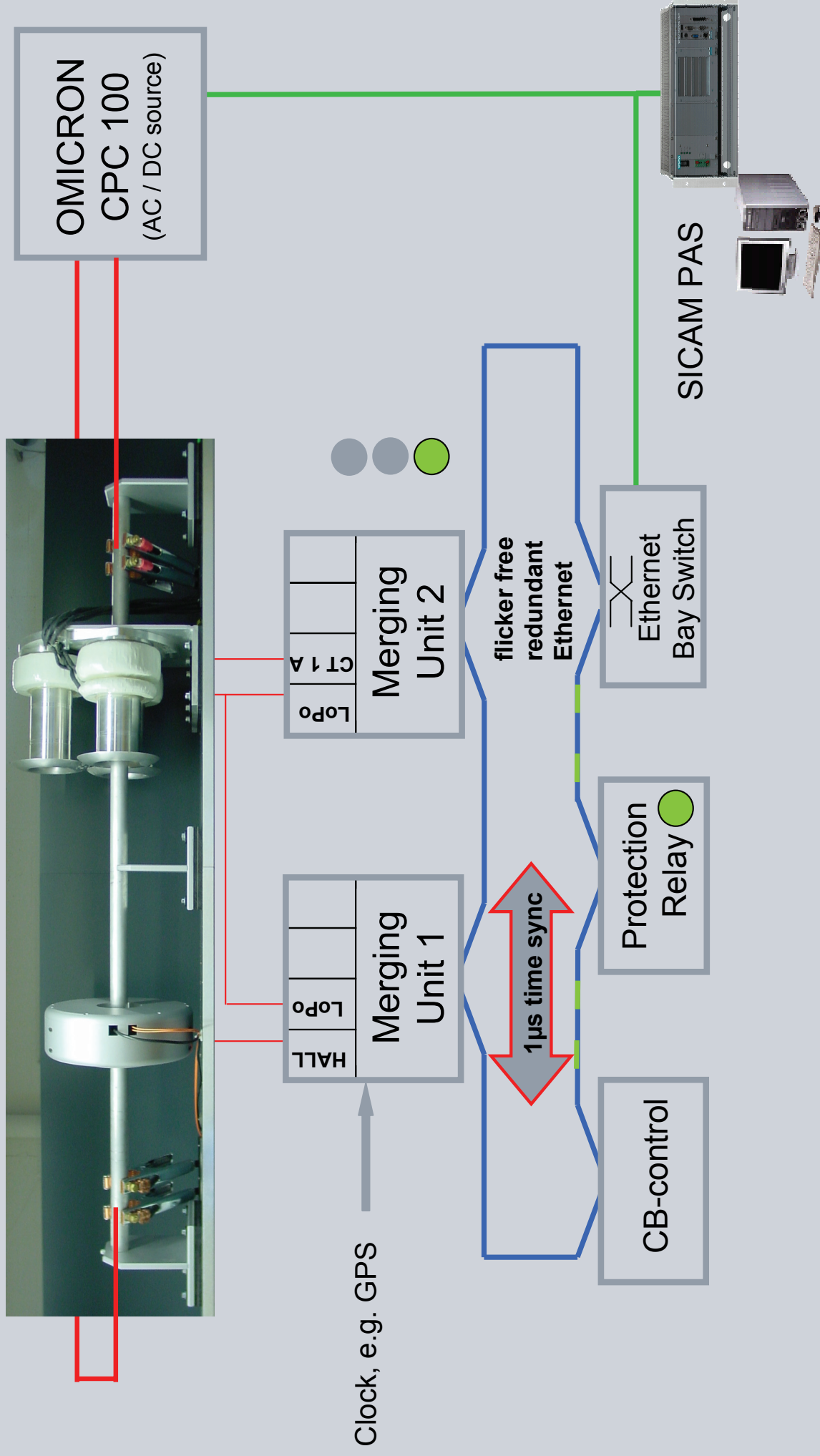
Transmission of LoPo Values to Relay

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Evidence Redundancy: Normal Operation

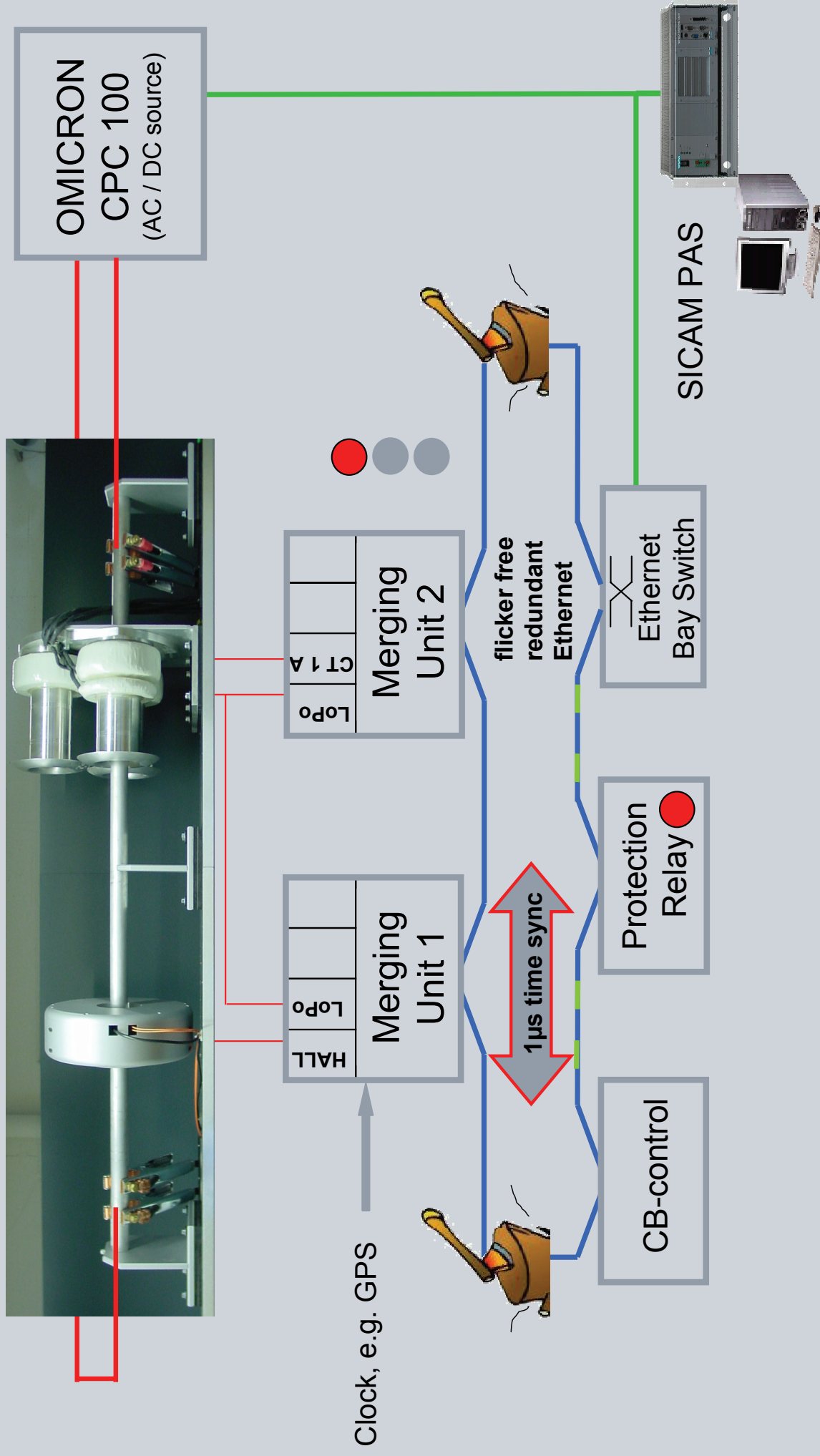
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Evidence Redundancy:

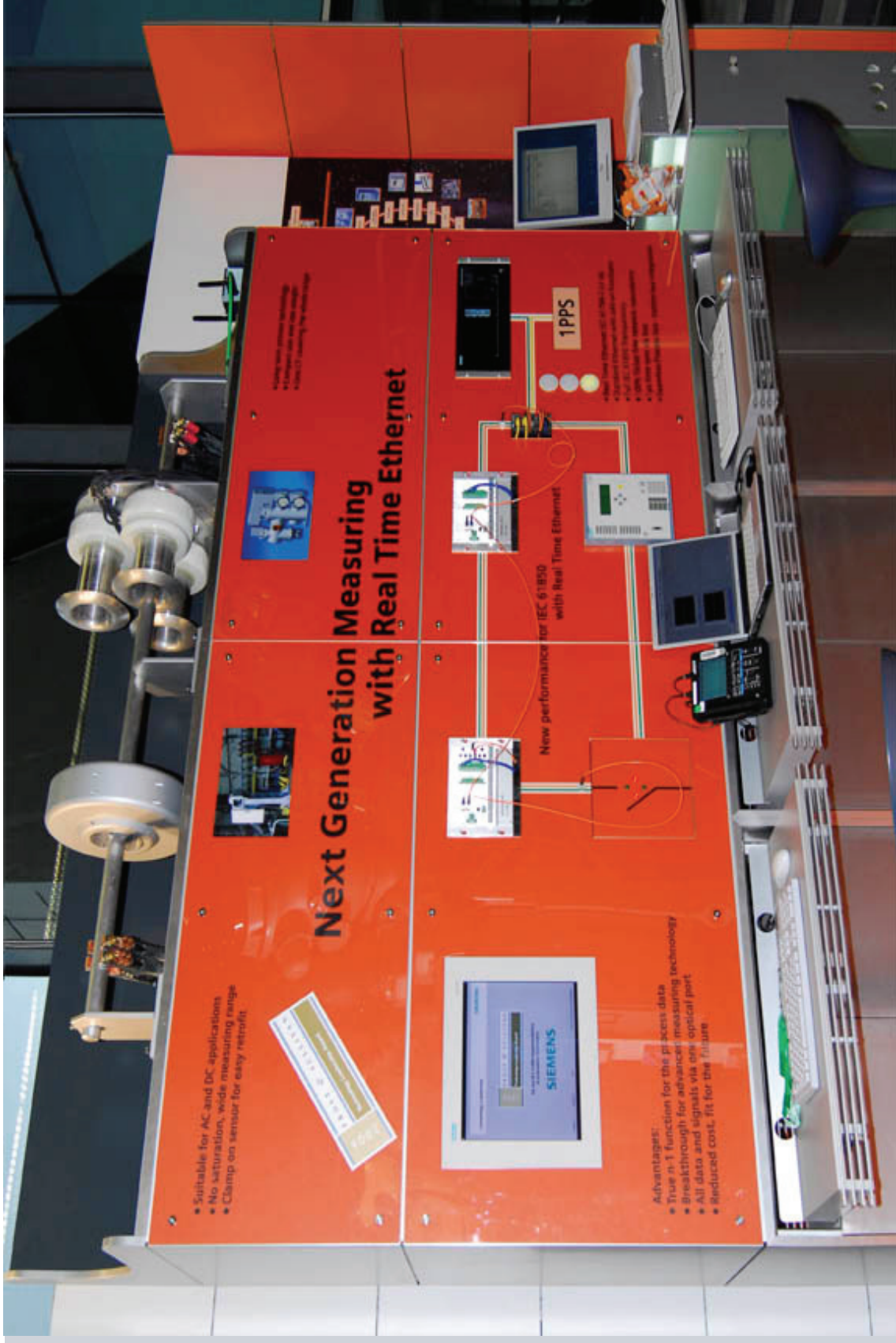
Second bus cut (n-2) , relay shows error

SIEMENS

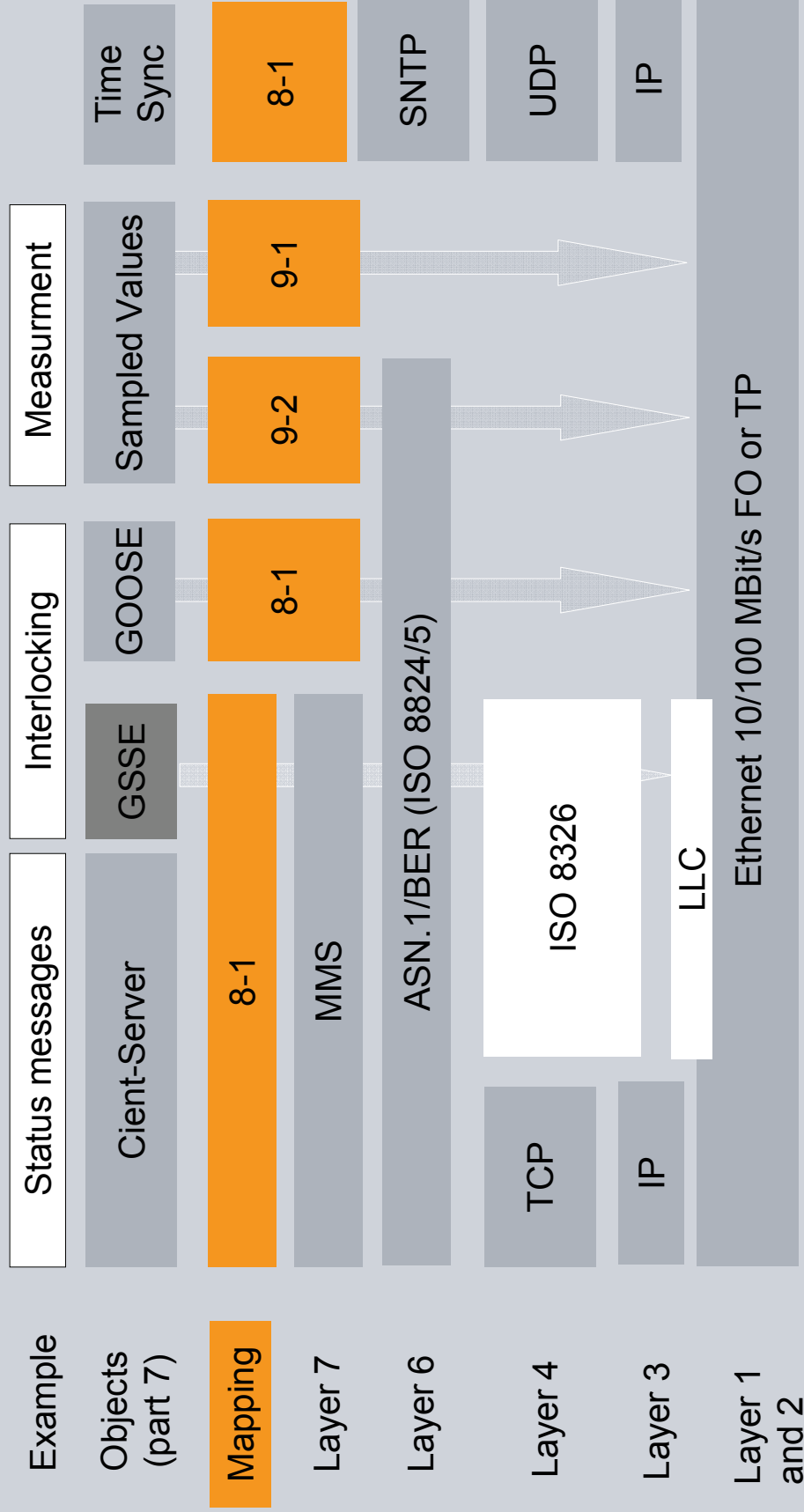


Presentation of Prototyp with Real Time Ethernet CIGRE conference Paris 2006

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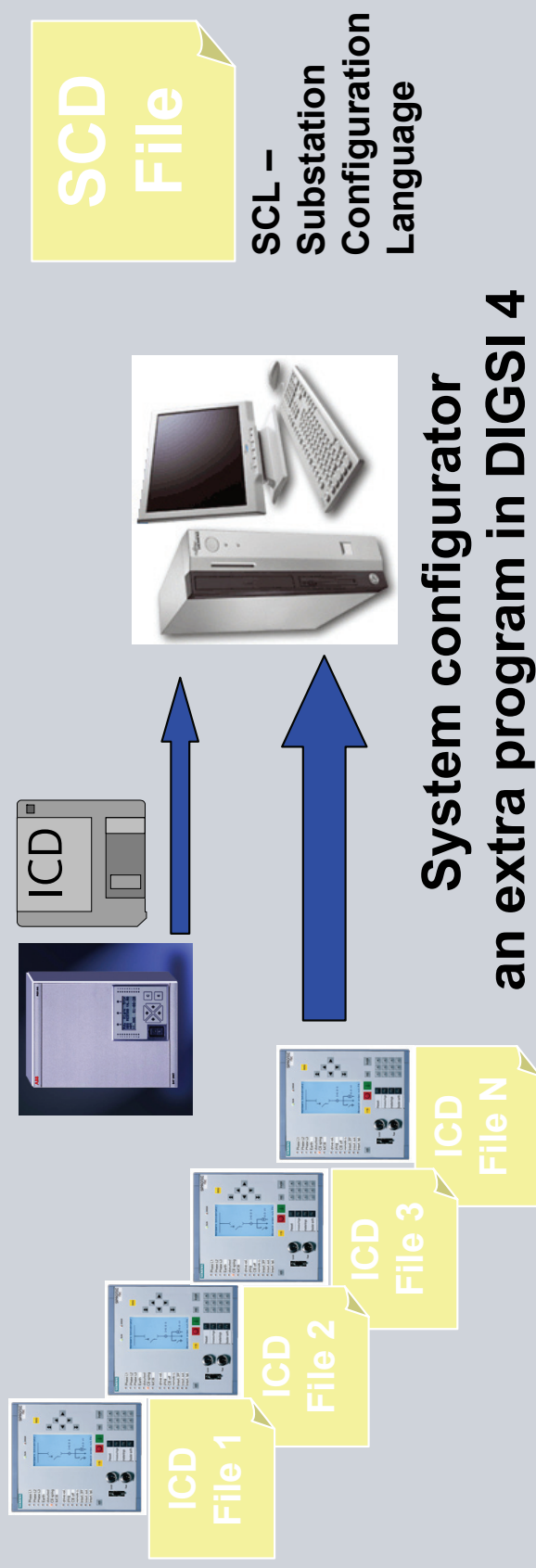


Assignment Functions, Services and Protocols



Compatibility back to UCA2.0 (not mandatory)

System configurator for managing the exchange of information on the station bus



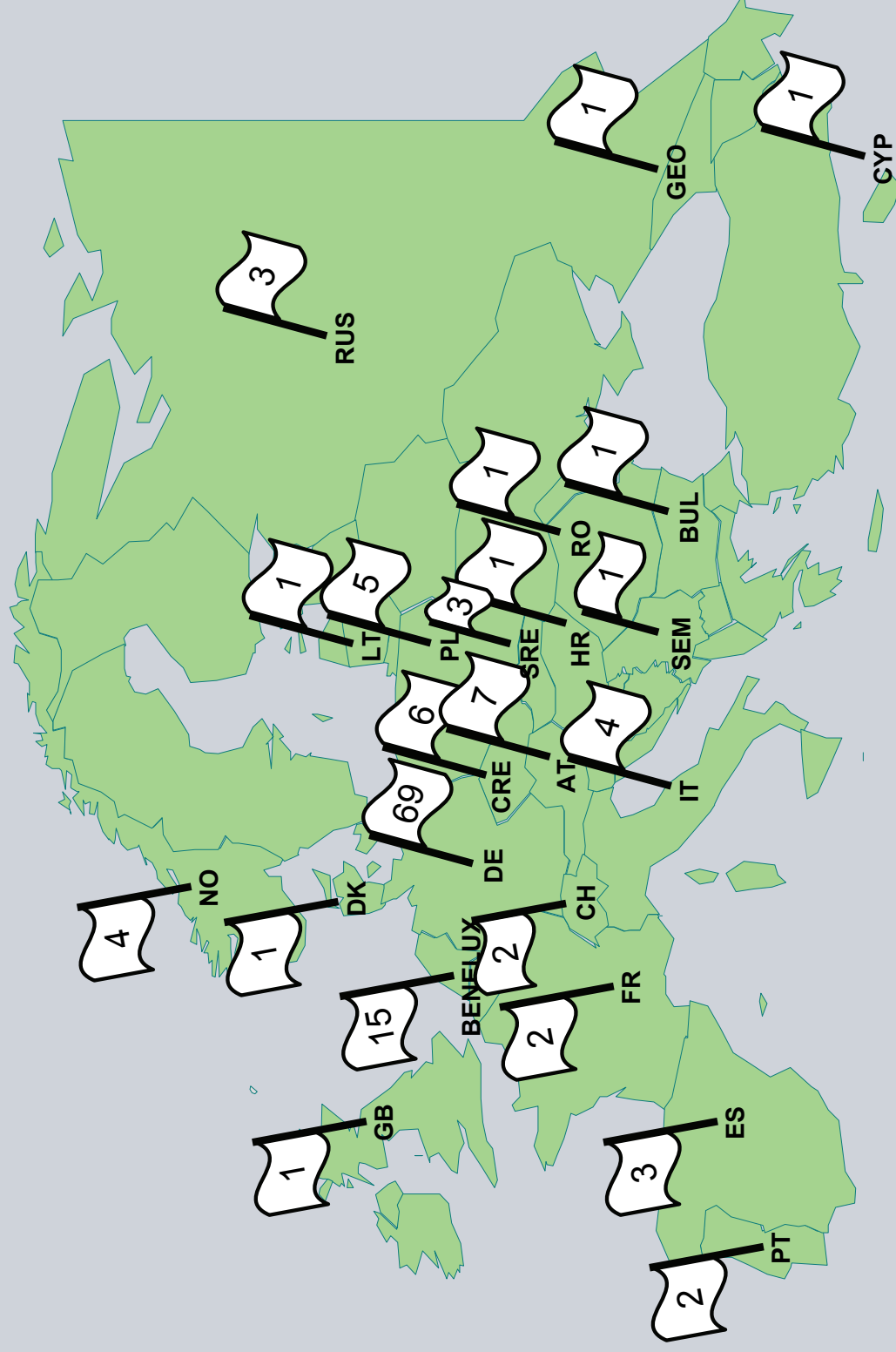
- ICD and SCL according to Part 6 of IEC 61850
 - Description of logical nodes of a device conforming to the standard (ICD): (protection functions, control commands and measured values etc.)
 - Full description of substation and communication relationships (SCD)

In DIGSI 4 information for the system interface is assigned and logical plans are designed in the CFC-logic editor.

In the System Configurator, information between devices is assigned.

Our Experience: IEC 61850 Projects - Europe

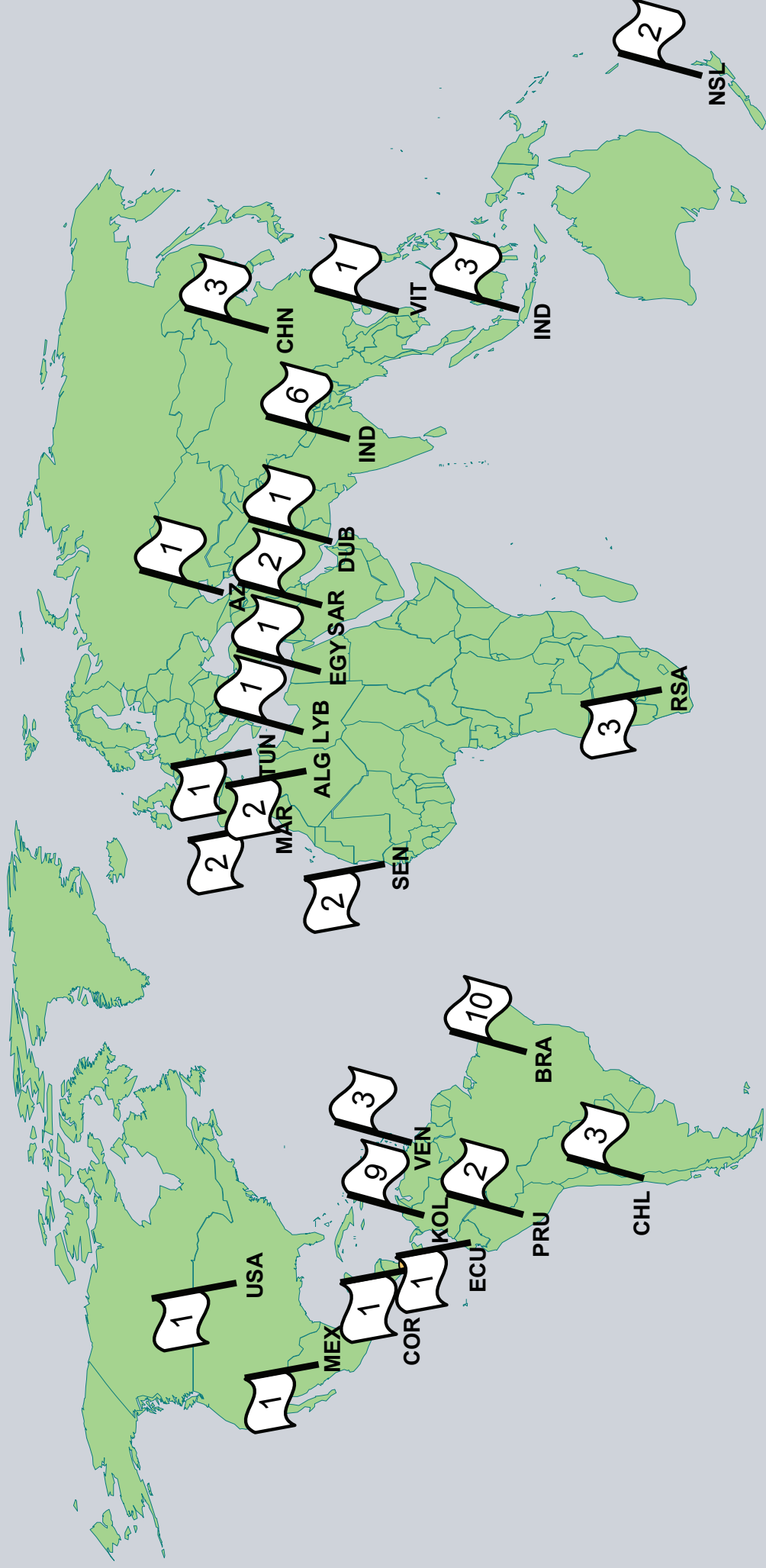
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Our Experience:

IEC 61850 Projects – World without Europe

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[illegible]

Project Opencast mining Garzweiler II, Germany

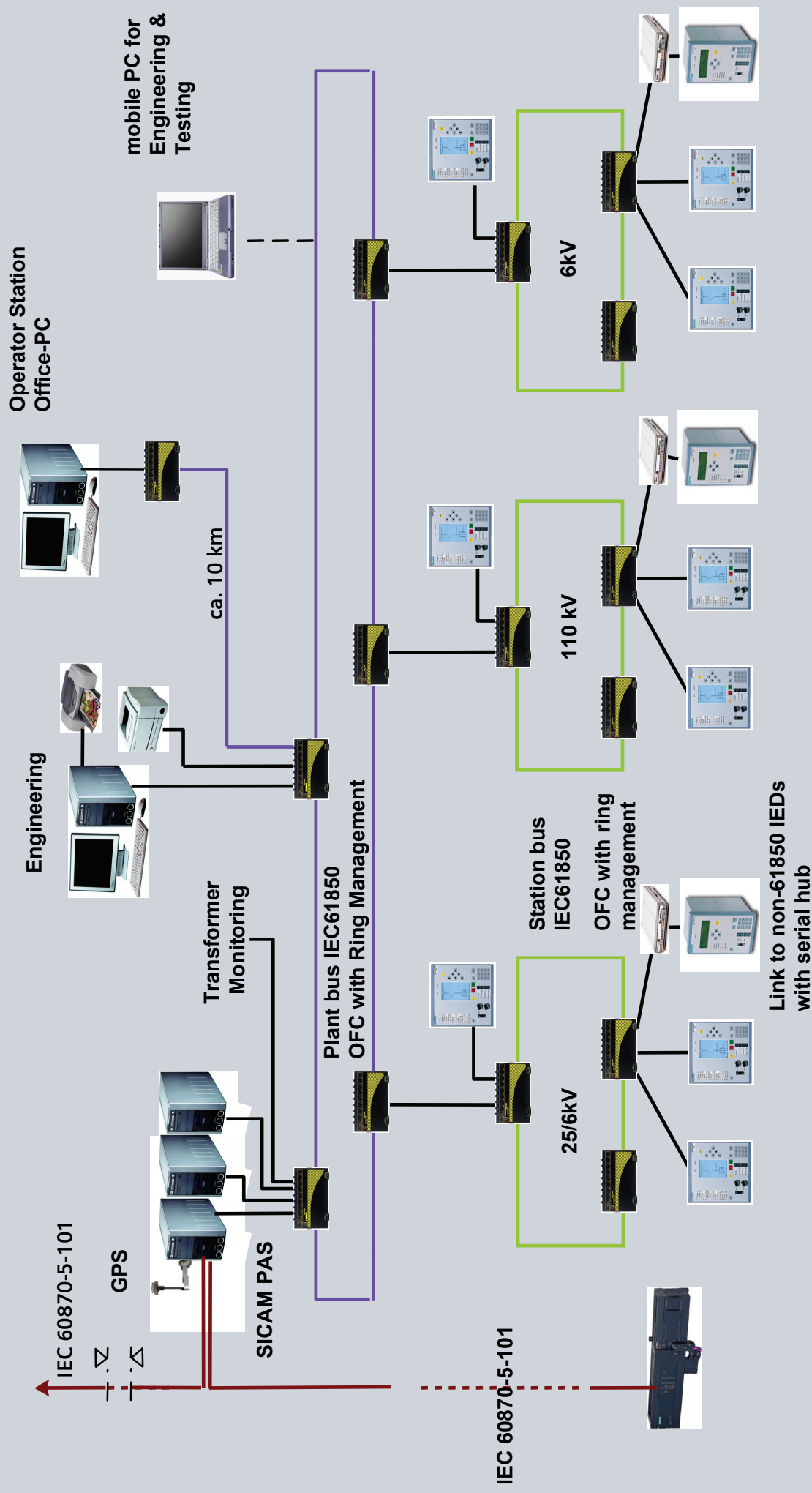
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- Customer: **RWE Power**
- Contract Award: **summer 2003**
- Main part in operation: **April 2005**
- Substation: **110, 25 & 6kV**
 - Number of bays: **134**
 - Application: power for **opencast mines** delivering coal to 4 power stations

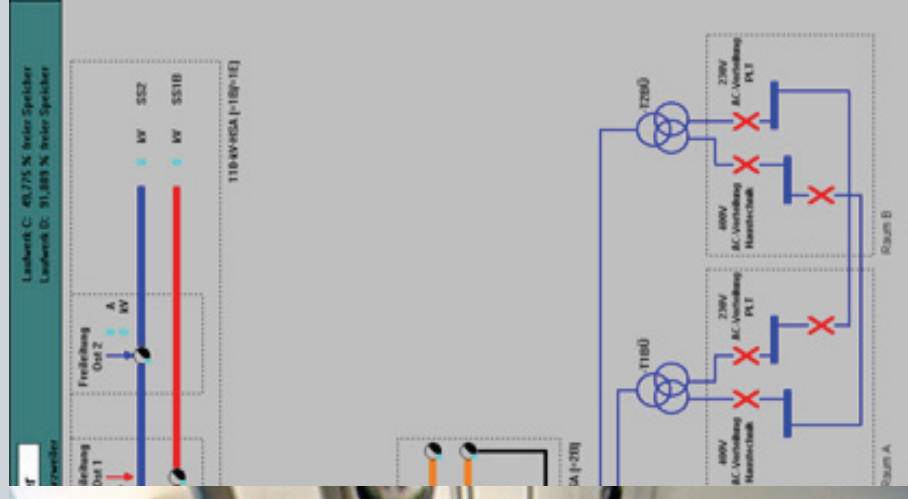
Project Opencast mining Garzweiler II, Germany

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Project Opencast mining Garzweiler II, Germany

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Project start: summer 2003

Commissioning: April 2005

SICAM PAS & IEC 61850 500kV Nanqiao Substation

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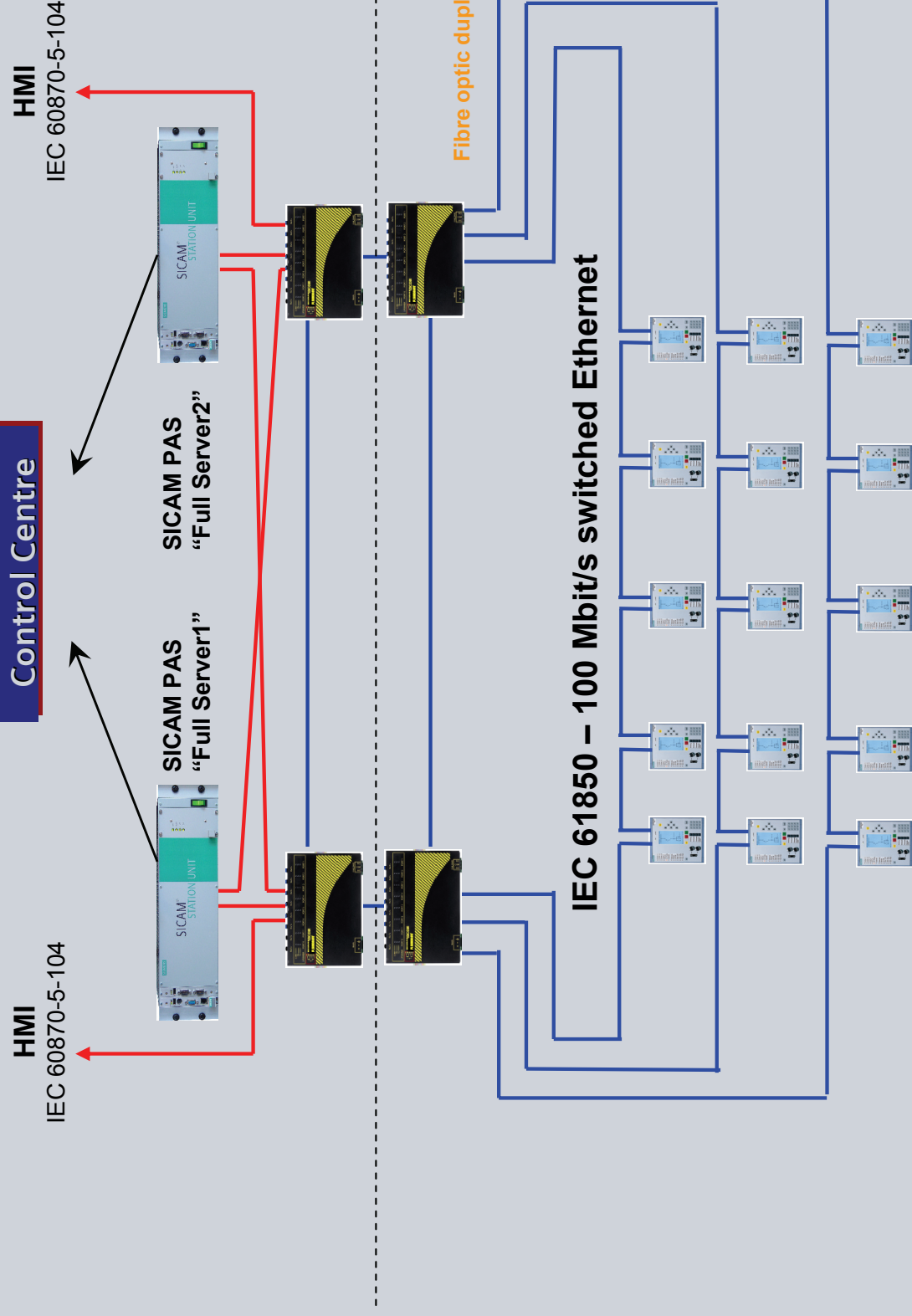


Shanghai

- costumer: **Shanghai Extra High Voltage Company**
- Sign of the contract: December **2004**
- in operation: November **2005**
- Switchgear
 - **500, 220 & 35kV**
 - **ca. 40 Bays**
 - **82 IEC 61850 Devices**

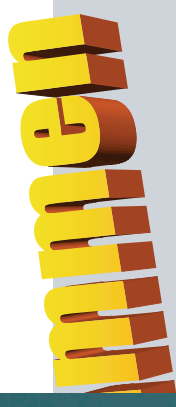
SICAM PAS & IEC 61850 500kV Nanqiao Substation

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International
Usersgroup

Our Mission

The UCA International Users Group is dedicated to enabling utility integration through the deployment of open standards by providing a forum in which the various stakeholders in the utility industry can work cooperatively together as members of a common organization.

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- ABB Automation
- American Electric Power (AEP)
- AREVA T&D
- Basler Electric
- BCHydro
- Black & Veatch
- Bonneville Power Administration
- Cinergy
- City Public Service of San Antonio
- ComEd (Exelon)
- ConEdison
- Entergy
- EPRI
- GE Multilin
- Hathaway
- Hydro-Québec
- Indianapolis Power and Light Company
- KC Associates
- KEMA Consulting
- LiveData
- Neftek Automation
- Omaha Public Power District
- OMICRON
- On-Line Monitoring
- Pennsylvania Power & Light
- Power Systems Engineering Research Center
- QEI
- RuggedCom
- Schweitzer Engineering Labs (SEL)
- Siemens PTD
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- Southern California Edison
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UCA[®] International Users Group

International
Users group

Advancing
Interoperability for
the Utility Enterprise

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Raleigh, NC 27614 USA
Fax: +919-847-2939
www.ucausersgroup.org



UCA International Stand auf der CIGRÉ 2006 / Paris

UCA International Annual Meeting

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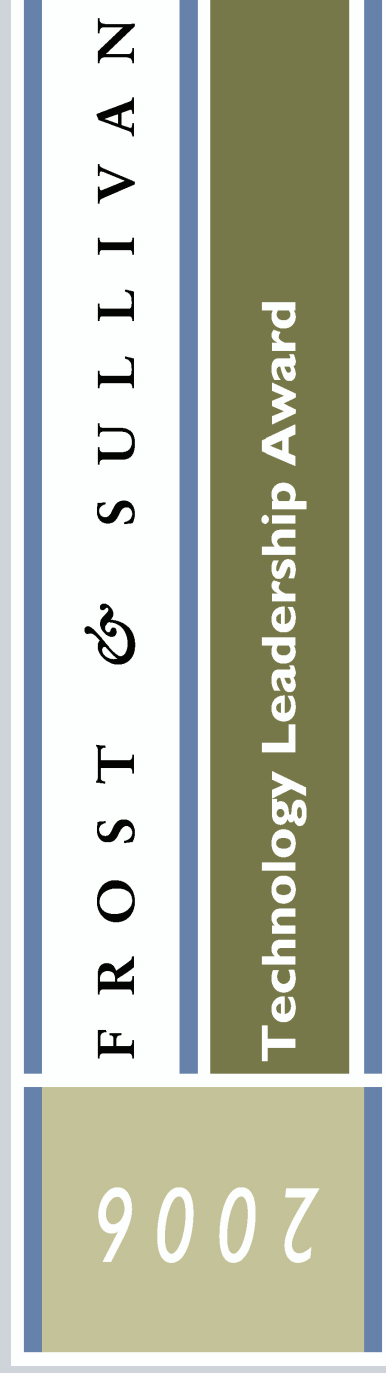






Technology Leadership

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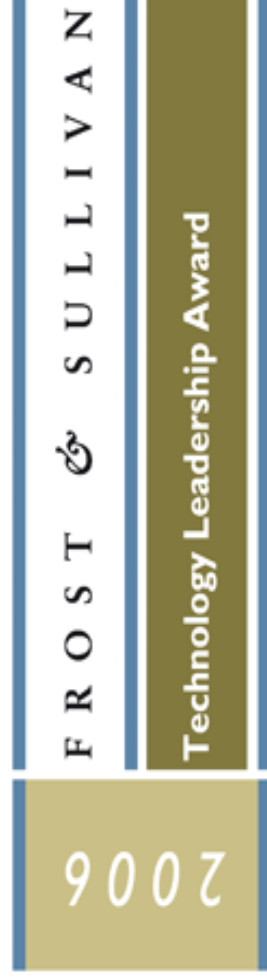


**for our IEC 61850 implementations
in Substation Automation**

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The award

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Frost & Sullivan's Technology Leadership Award...

- “is bestowed upon a company that has **pioneered** the development of an innovative technology”
- “recognises companies... for demonstrating superior **performance** in areas such as leadership and technological innovation”

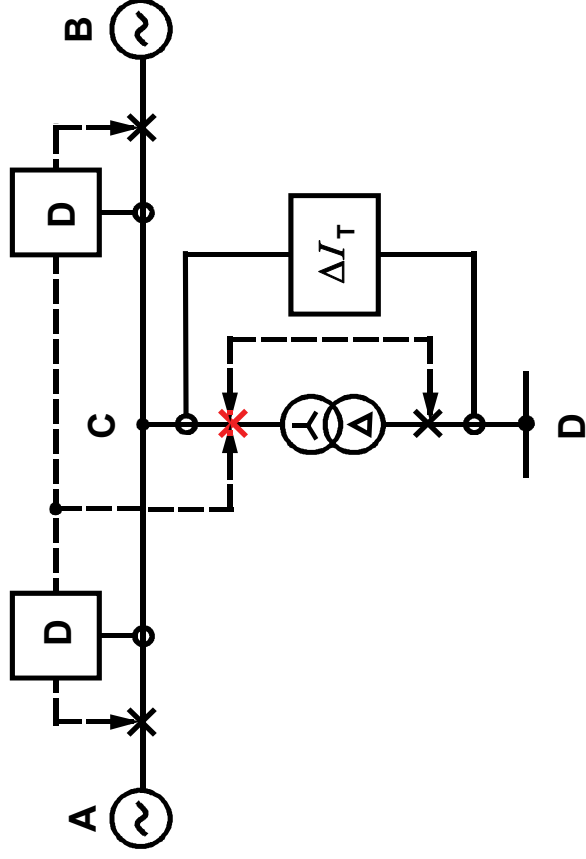


Distance Protection of Tapped

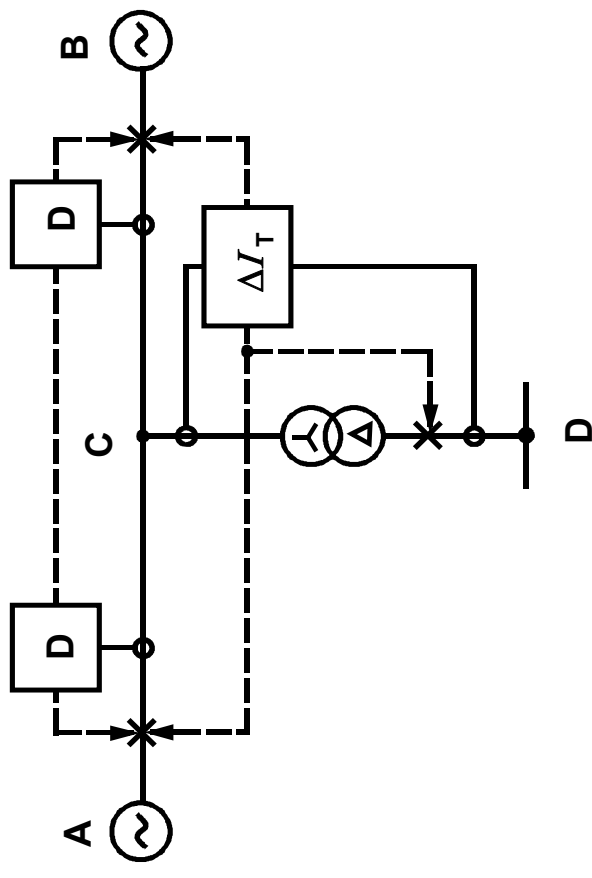
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Distance protection of tapped lines Basic tap configurations

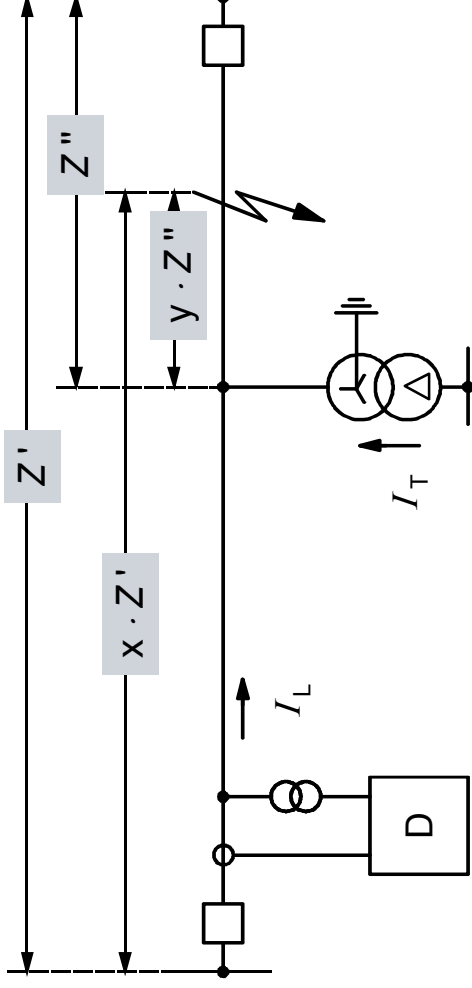


With circuit breaker at the tap



Without circuit breaker at the tap

Tapped line, Distance measurement during Ph-E fault Influence of earthed transformers (1)



With k_0 set to : $\frac{Z'_E}{Z'_1}$

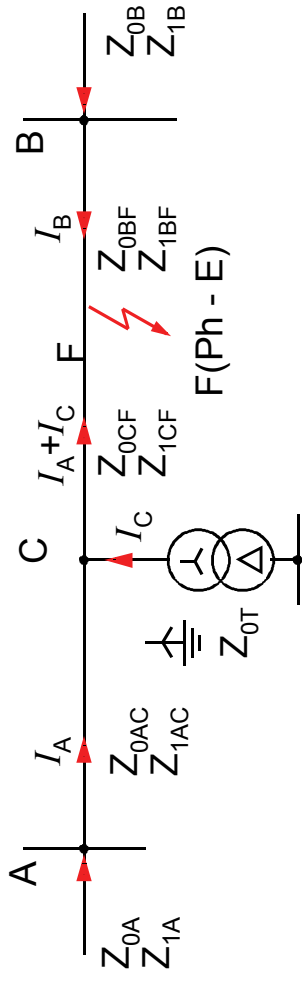
$$\begin{aligned} V_{L1-Relais} &= x [I_{L1-L} \cdot Z'_1 + I_{E-L} \cdot Z'_E] + y [I_{L1-T} \cdot Z'_1 + I_{E-T} \cdot Z'_E] \\ &= x \cdot Z'_1 \left[I_{L1-L} + I_{E-L} \cdot \frac{Z'_E}{Z'_1} \right] + y [I_{L1-T} \cdot Z'_1 + I_{E-T} \cdot Z'_E] \end{aligned}$$

$$Z_{L1-Relay} = \frac{U_{L1-Relay}}{I_{L1-L} + k_0 \cdot I_{EL}}$$

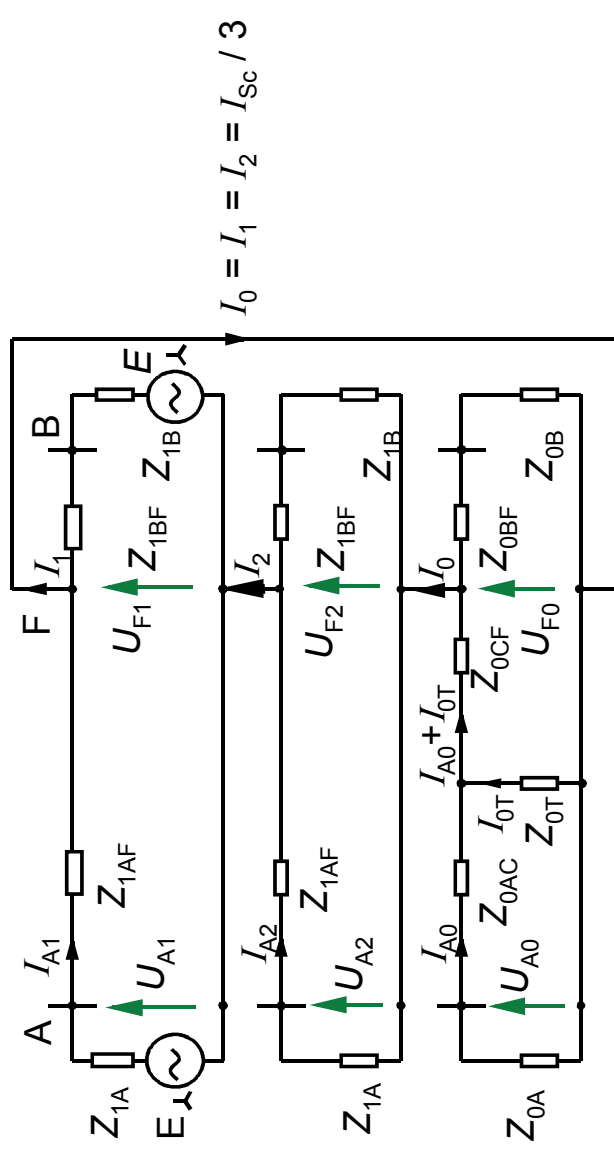
$$Z_{L1-R} = x \cdot Z'_1 + y \cdot Z'_1 \cdot \underbrace{\frac{I_{L1-T} \cdot Z''_1 + I_{E-T} \cdot Z'_E}{I_{L1-L} \cdot Z'_1 + I_{E-L} \cdot Z'_E}}_{\text{Measuring error}}$$

Measuring error

Tapped line, Distance measurement during Ph-E fault Influence of earthed transformers (2)



a) Single-phase equivalent circuit



b) Equivalent circuit with symmetrical components

Tapped line, Distance measurement during Ph-E fault Influence of earthed transformers (3)

$$U_{A0} = U_{F0} + Z_{0CF} \cdot (I_{A0} + I_{0T}) + Z_{0AC} \cdot I_{A0}$$

$$U_{A1} = U_{F1} + Z_{1AF} \cdot I_{A1}$$

$$U_{A2} = U_{F2} + Z_{1AF} \cdot I_{A2}$$

with $U_{F0} + U_{F1} + U_{F2} = 0$ und $Z_{0AC} + Z_{0CF} = Z_{0AF}$:

$$U_A = Z_{0AF} \cdot I_{A0} + Z_{0CF} \cdot I_{0T} + Z_{1AF} \cdot (I_{A1} + I_{A2})$$

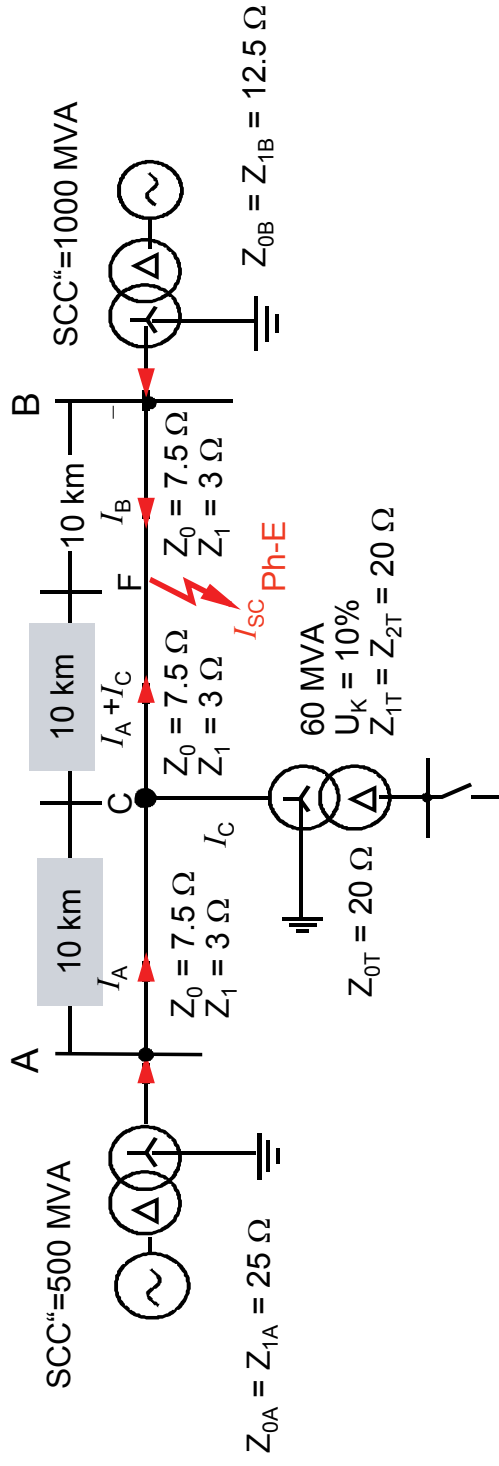
$$I_A = I_{A0} + I_{A1} + I_{A2}$$

Symmetrical component currents :

$$I_{A0} = \frac{Z_{0T}}{Z_{0T} + Z_{0A} + Z_{0AC}} \cdot \frac{Z_{0B} + Z_{0BF}}{Z_{0B} + Z_{0BF} + Z_{0CF} + \frac{Z_{0T}(Z_{0A} + Z_{0AC})}{Z_{0T} + Z_{0A} + Z_{0AC}}} I_0$$

$$I_{A1} = I_{A2} = \frac{Z_{1B} + Z_{1BF}}{Z_{1B} + Z_{1BF} + Z_{1A} + Z_{1AF}} I_0$$

Tapped line, Distance measurement during Ph-E fault Influence of earthed transformers, example



True positive sequence impedance to fault point: $Z_{1A-F} = 6 \Omega$

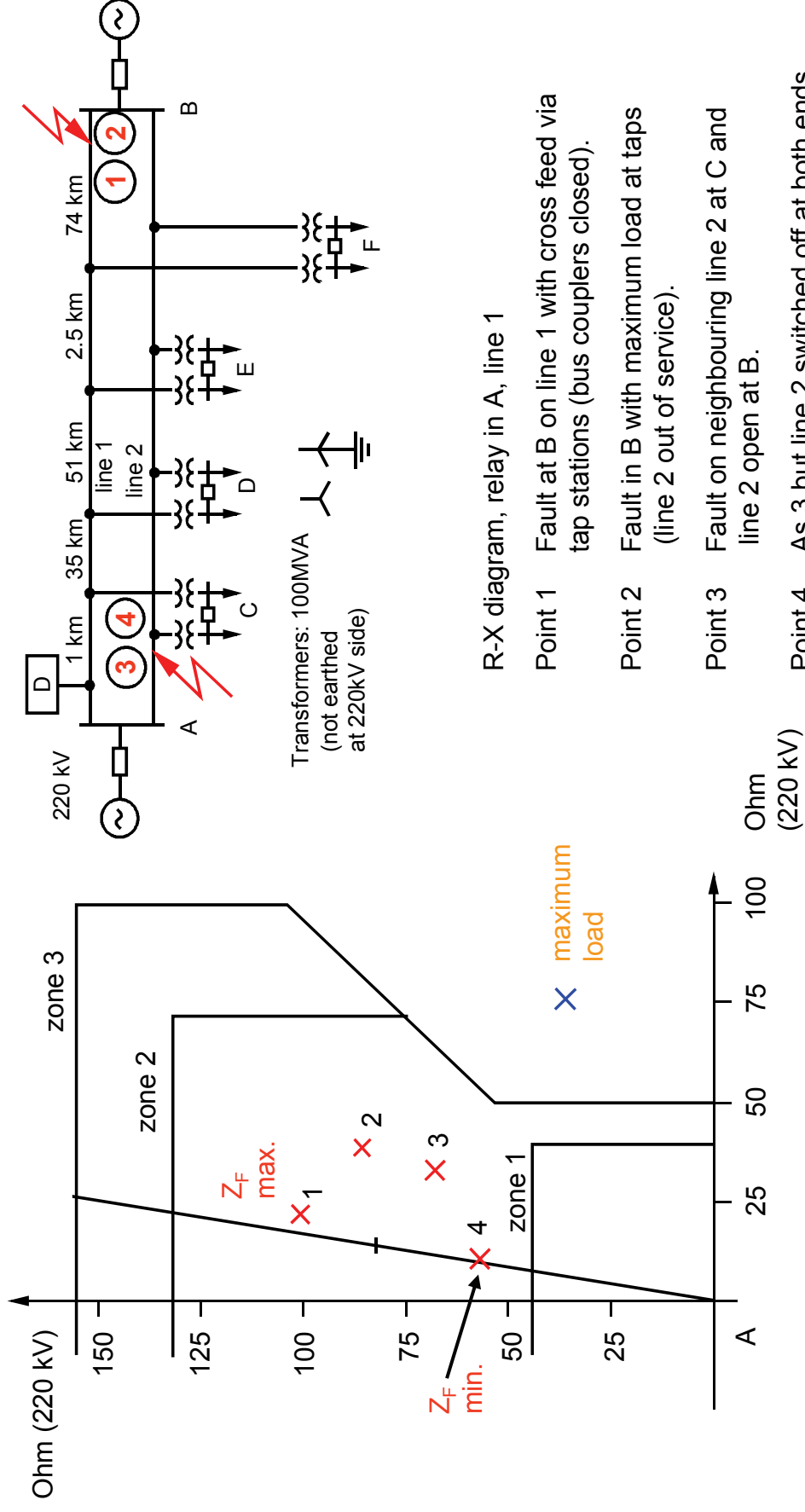
Measuring error = 2Ω :

The fault appears 6.7 km further away.

There is an underreach of about 33%.

$$\begin{aligned}
 Z_{0F} &= 10 \Omega \\
 Z_{1F} &= Z_{2F} = 10.3 \Omega \\
 I_0 &= I_1 = I_2 = 110 \text{ kV} / (\sqrt{3}(10+2 \cdot 10.3 \Omega)) = 2.1 \text{ kA} \\
 I_{SC} &= I_0 + I_1 + I_2 = 6.3 \text{ kA} \\
 I_{A0} + I_{T0} &= 0.5 I_0 = 1.05 \text{ kA} \\
 I_{A0} &= 0.4 \text{ kA}; \quad I_{0T} = 0.65 \text{ kA}; \quad I_{AE} = 3 \cdot I_{A0} = 1.2 \text{ kA} \\
 I_{A1} &= I_{A2} = 0.33 I_0 = 0.7 \text{ kA} \\
 U_A &= 7.5 \Omega \cdot 0.4 \text{ kA} + 7.5 \Omega \cdot 1.05 \text{ kA} + 6 \Omega \cdot 0.7 \text{ kA} + 6 \Omega \cdot 0.7 \text{ kA} = 19.3 \text{ kV} \\
 I_A &= 0.4 \text{ kA} + 2 \cdot 0.7 \text{ kA} = 1.8 \text{ kA} \\
 Z_{mA} &= U_A / (I_A + k_0 \cdot I_{AE}) = 19.3 \text{ kV} / (1.8 \text{ kA} + 0.5 \cdot 1.2 \text{ kA}) = 8 \Omega
 \end{aligned}$$

Multiply tapped double circuit line (220 kV) Distance protection setting



Fault locator with 2 ended measurement

Power Transmission
and Distribution

Consultant Power System Protection

Gustav Steynberg

PTD PA13 Nuremberg

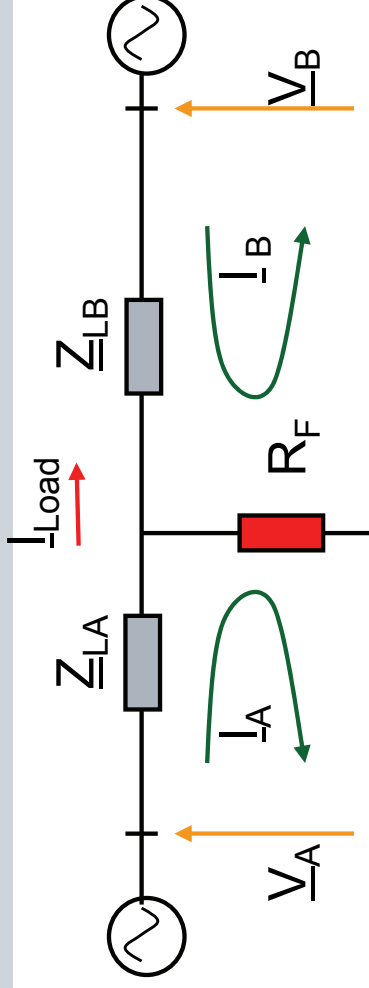
Phone: +49 911 433 7012

Fax: +49 911 433 8301

Email: Gustav.Steynberg@siemens.com

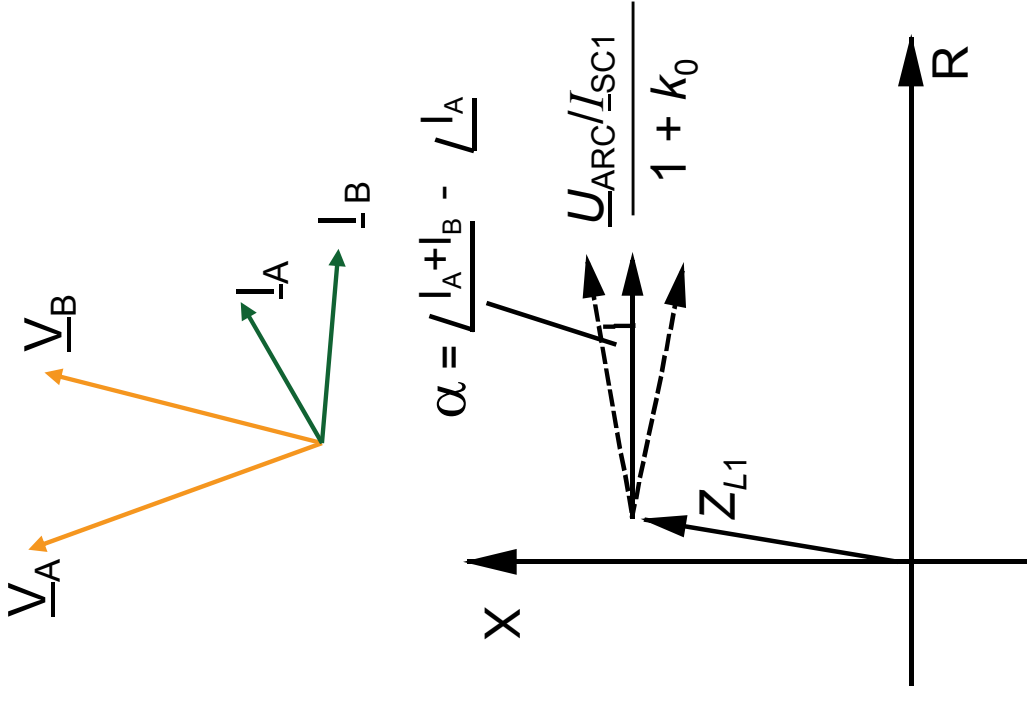


Fault Locator: Load and Fault Resistance

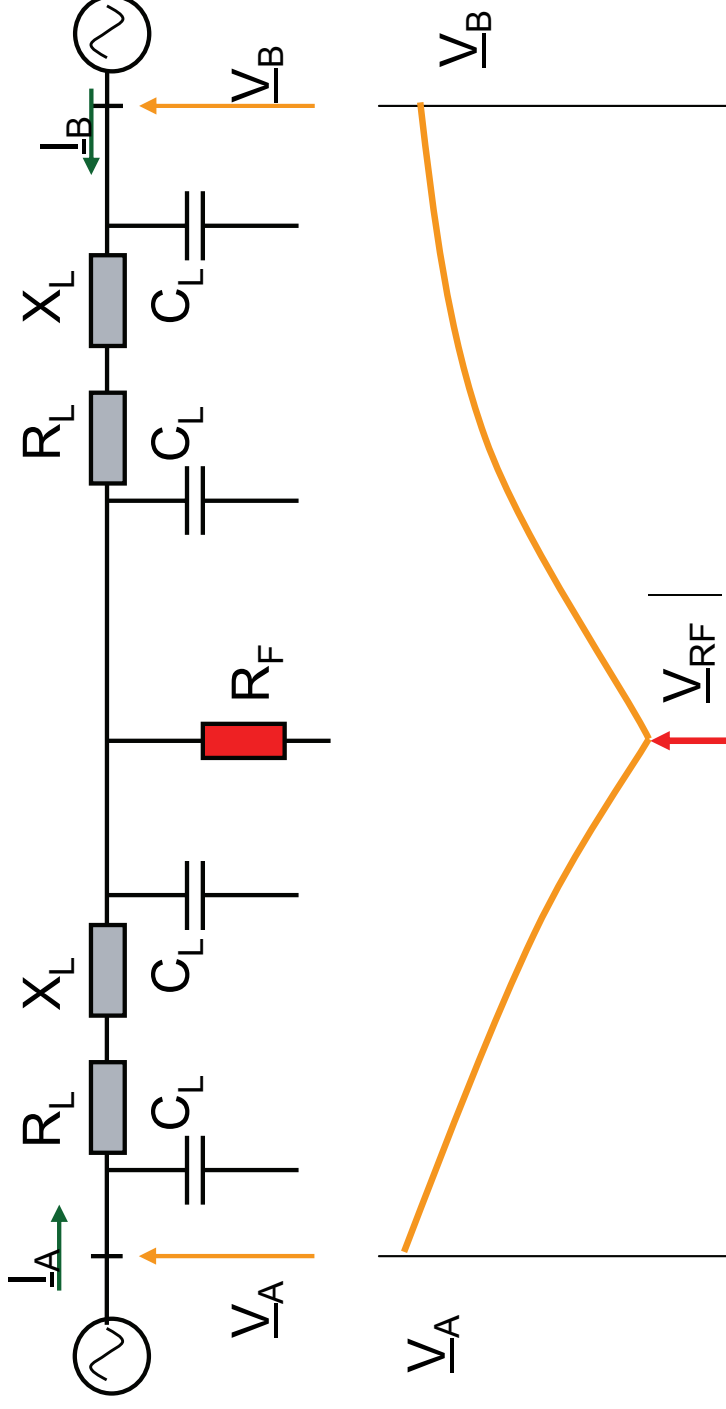


Due to load current there is an angular displacement between the voltages. This angle and possible differences in the source impedance angle cause the angular displacement between current $\underline{I}_A$ and $\underline{I}_B$. As a result, the voltage drop across R_F is affected by this angle between the currents.

The single ended measurement cannot compensate for this.



Fault Locator: 2 ended with transmission line equation

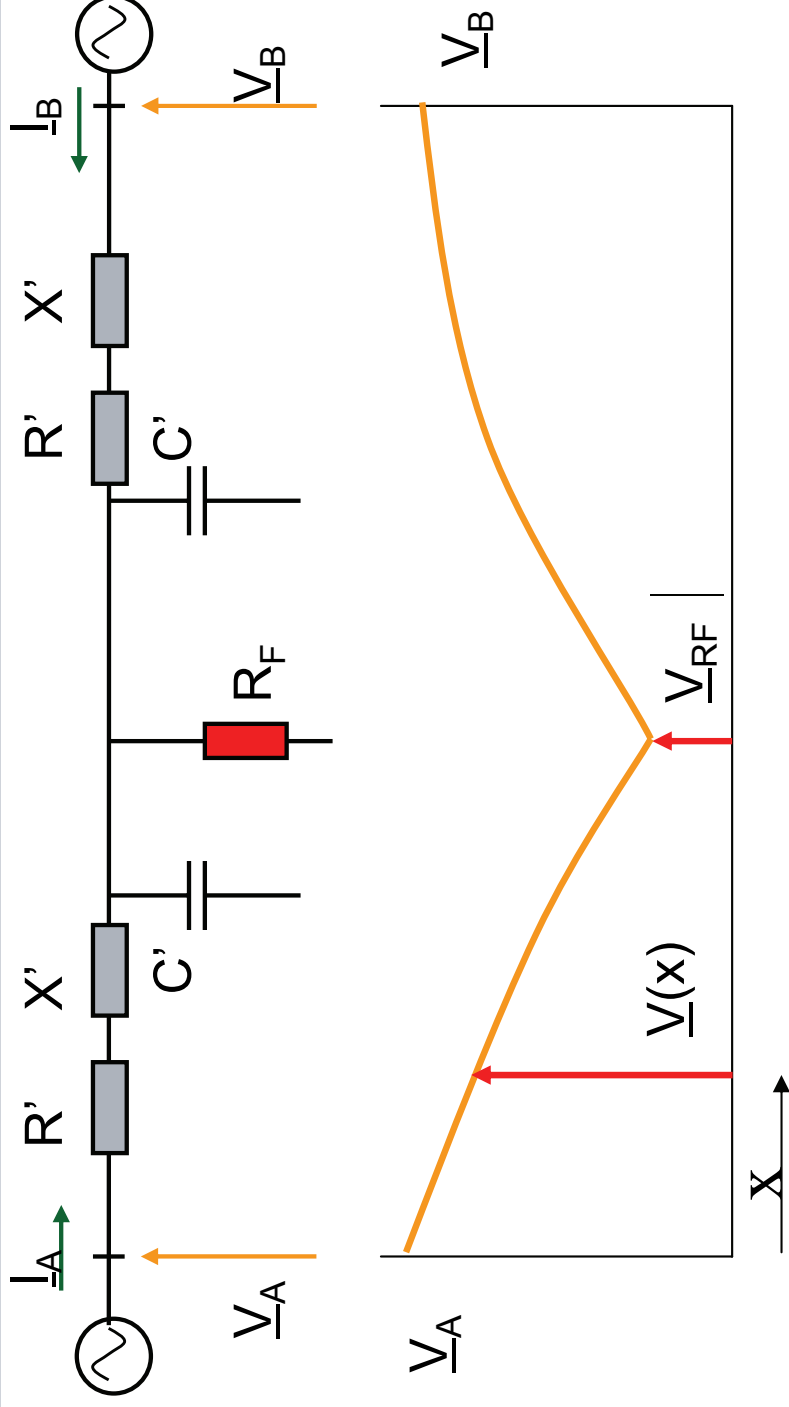


R_L X_L C_L
are distributed
positive sequence
line resistance,
inductance and
capacitance

Based on measured positive sequence voltage and current from both line ends, the positive sequence voltage drop along the line upto the fault location is calculated. At the fault location the calculated voltages from end A and end B are equal.

Data from both ends are required for the computation.

Fault Locator: 2 ended with transmission line equation



R' X' C'
are positive
sequence line
resistance, and
inductance and
capacitance
per km

$$\underline{V}(x) = \underline{V}_A \cdot \cosh(\underline{\gamma} \cdot x) - \underline{Z} \cdot \underline{I}_A \sinh(\underline{\gamma} \cdot x)$$

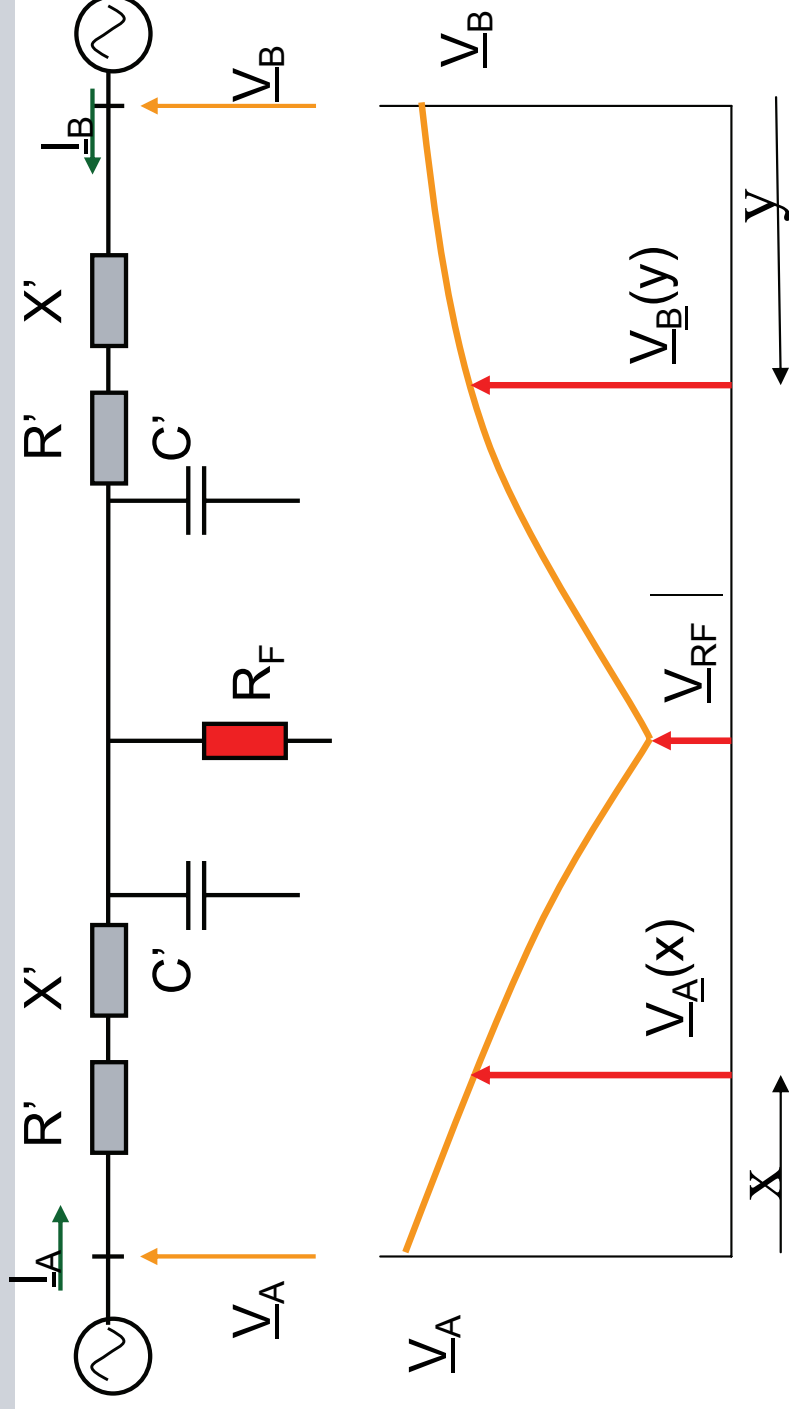
$$\underline{\gamma} = \sqrt{(R' + j\omega L') \cdot j\omega C'}$$

Propagation
constant

$$\underline{Z} = \sqrt{\frac{R' + j\omega L'}{j\omega C'}}$$

characteristic
impedance

Fault Locator: comparison of results from both line ends



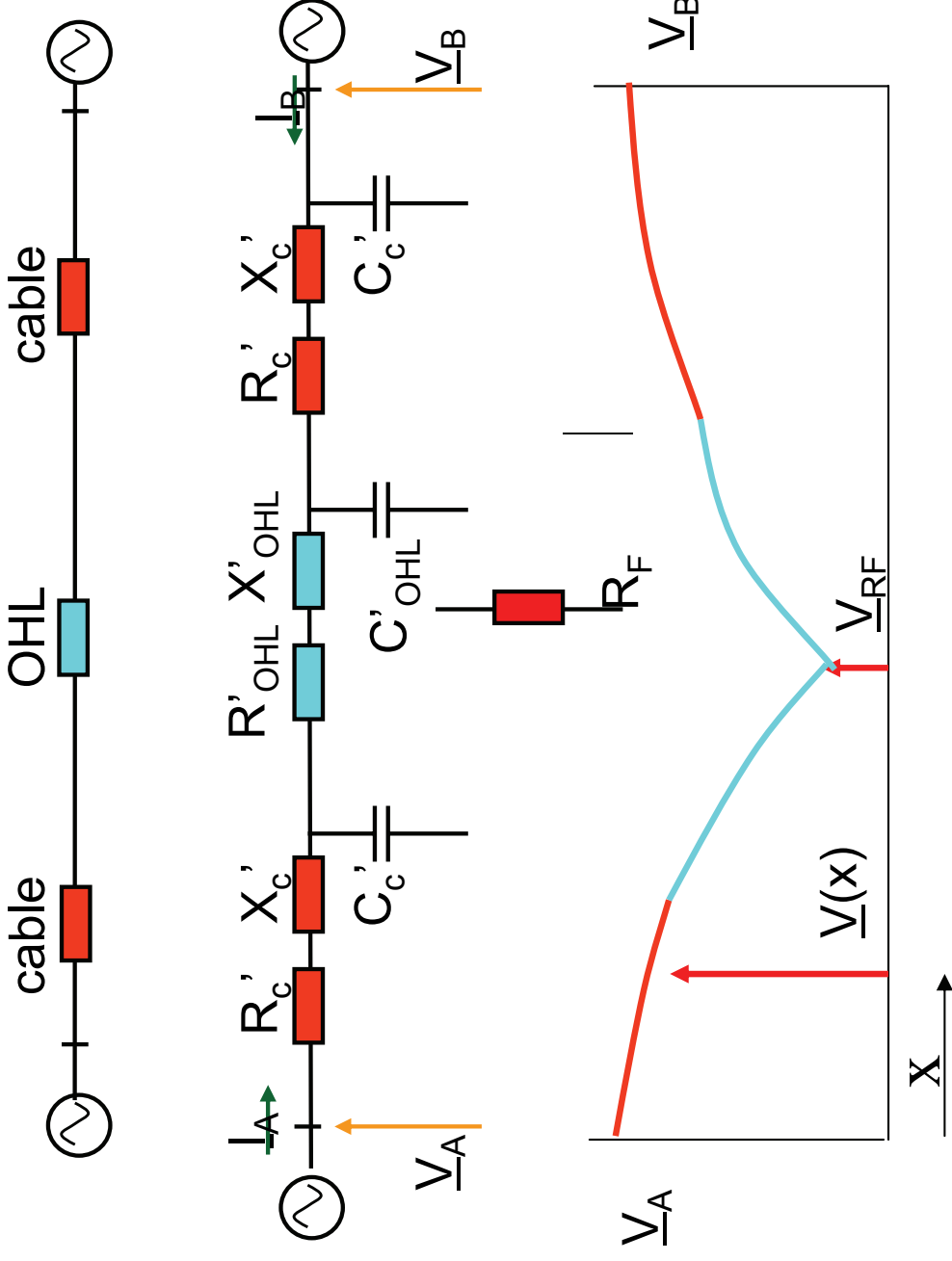
The measured current and voltage signals at end A and B are transmitted via communication interface and then synchronised at each line end.

$$\varepsilon(x, y) = \underline{V}_A \cdot (x) - \underline{V}_B(y)$$

$$\text{ideally : } \varepsilon(x, y) = 0$$

By minimising the error ε the fault location (x,y) is obtained

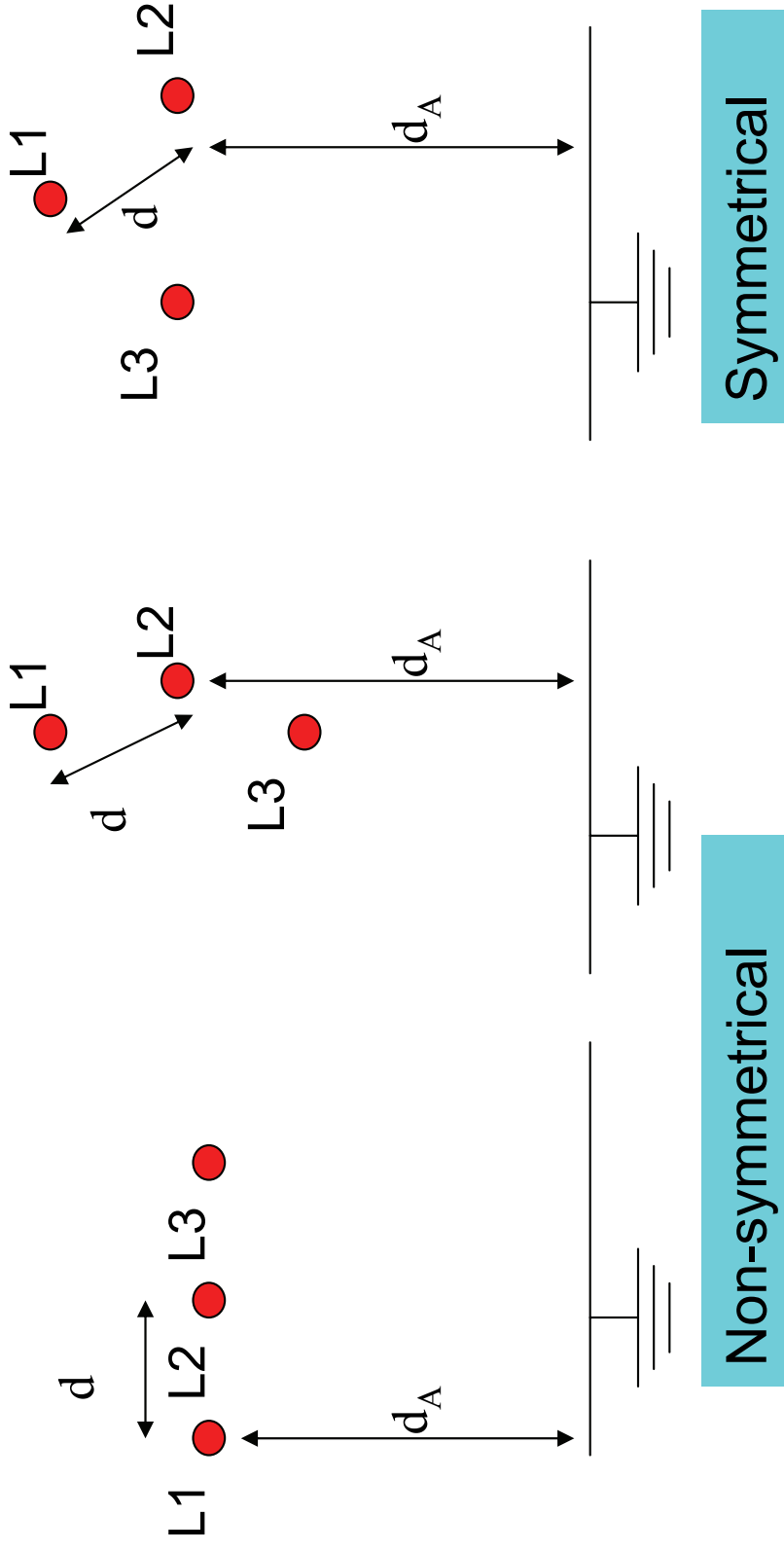
Fault Locator: multiple feeder sections



$R' \quad X' \quad C'$

line/cable
resistance,
inductance and
capacitance
per km for each line
section must be set

Fault Locator: Non-symmetrical and Non-transposed lines

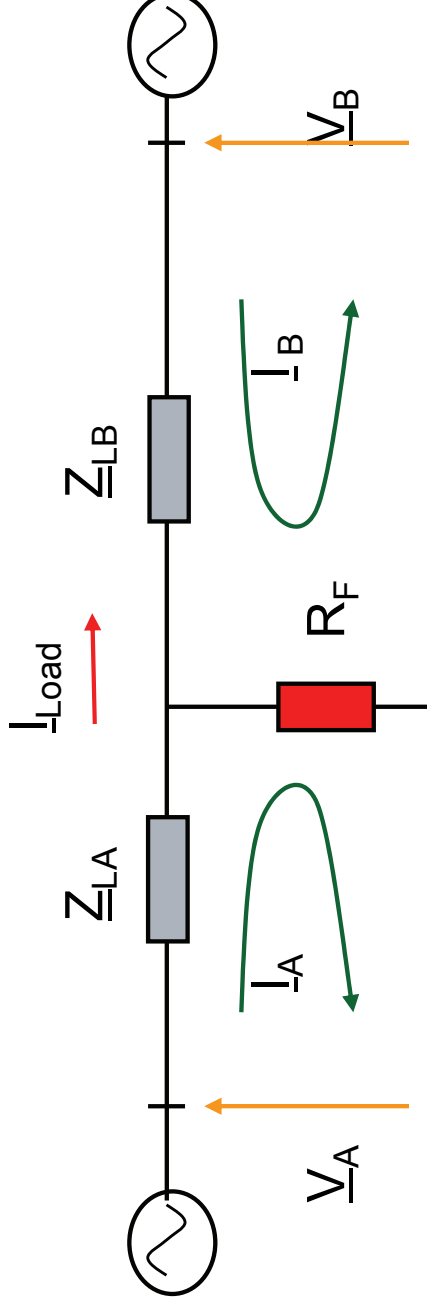


The coupling impedances of the three phases are not the same. By defining the centre conductor (in this case L2), the impedance non-symmetry can be considered in the calculation of the voltage profile.

Fault Locator: advantage of 2 ended method

- The measurement is not dependant on zero sequence system data (XE/XL, RE/RL etc.)
- Fault resistance and load current do not affect the accuracy
- Coupling of parallel lines only has a negligible effect on the measurement
- Fault location accuracy is also achieved on non-symmetrical and non-transposed lines

Example: Single and 2 end fault locator – Influence of load current and fault resistance



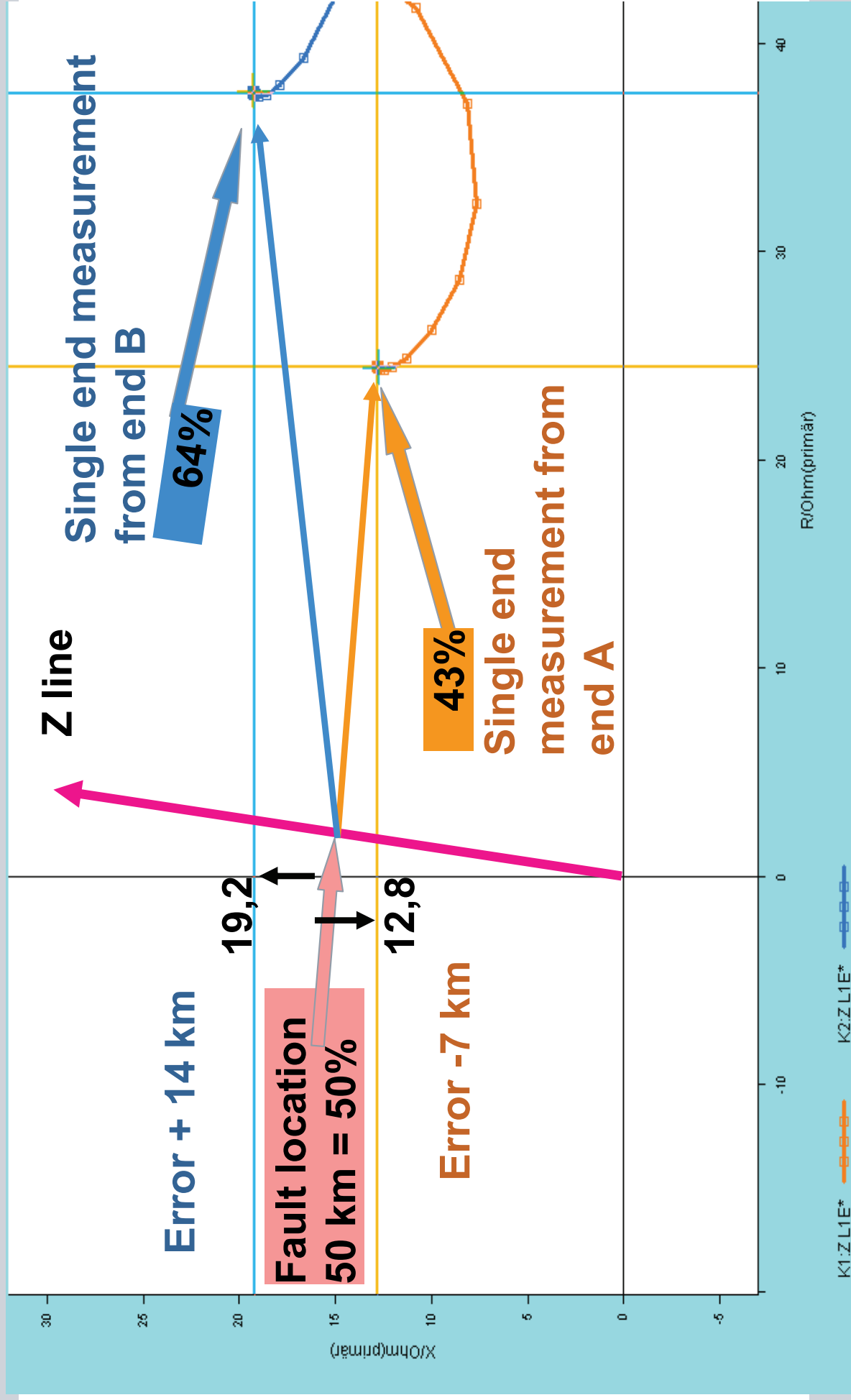
$R_F = 30 \text{ Ohm}$

$I_{Load} = 300 \text{ A}$ (10° between sources)

$Z_{LA} = Z_{LB} = 2 + j15 \text{ Ohm}$ (fault at 50%)

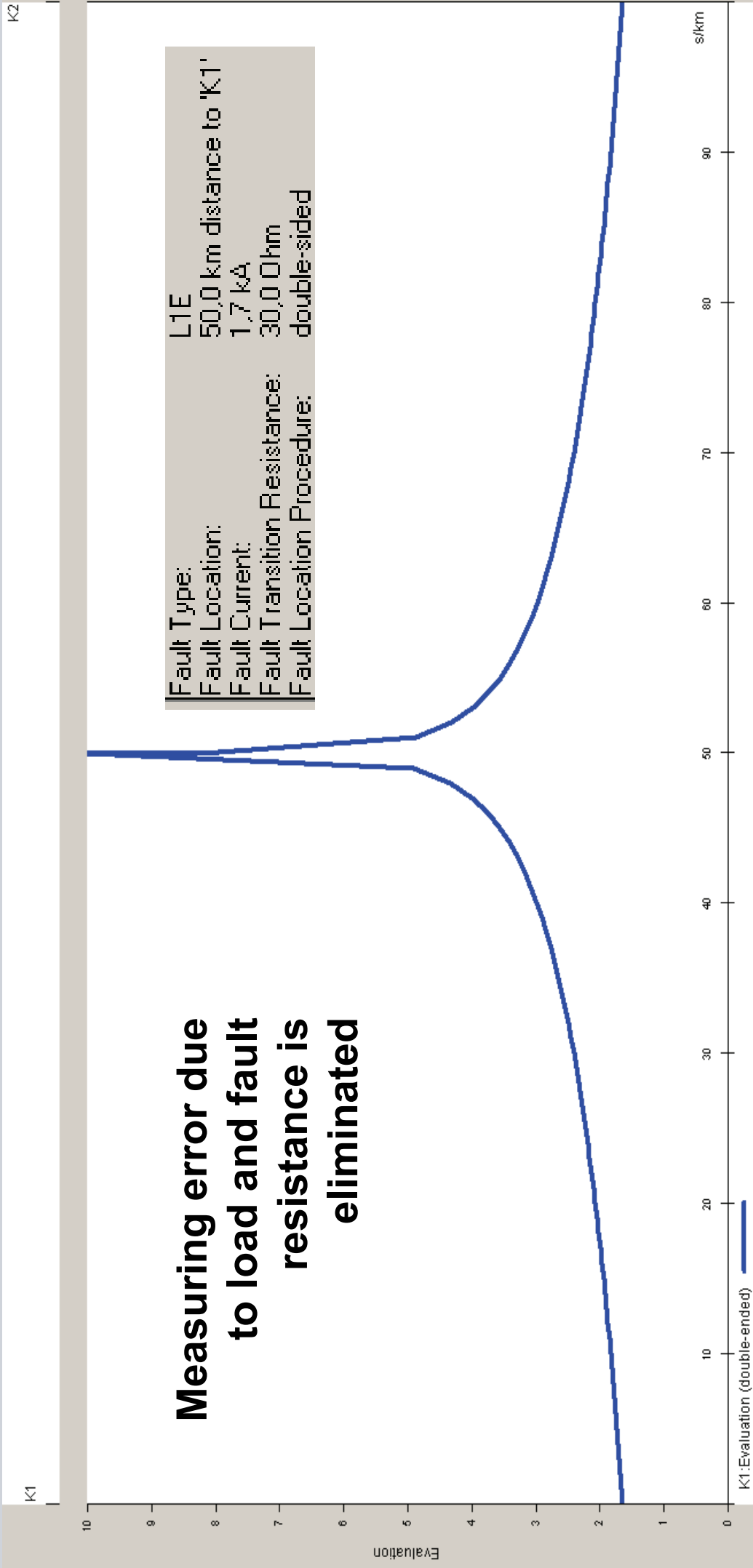
Line length = 100 km

Measured single end fault location (L1-G with fault resistance 30 Ohm and load current 300 A)

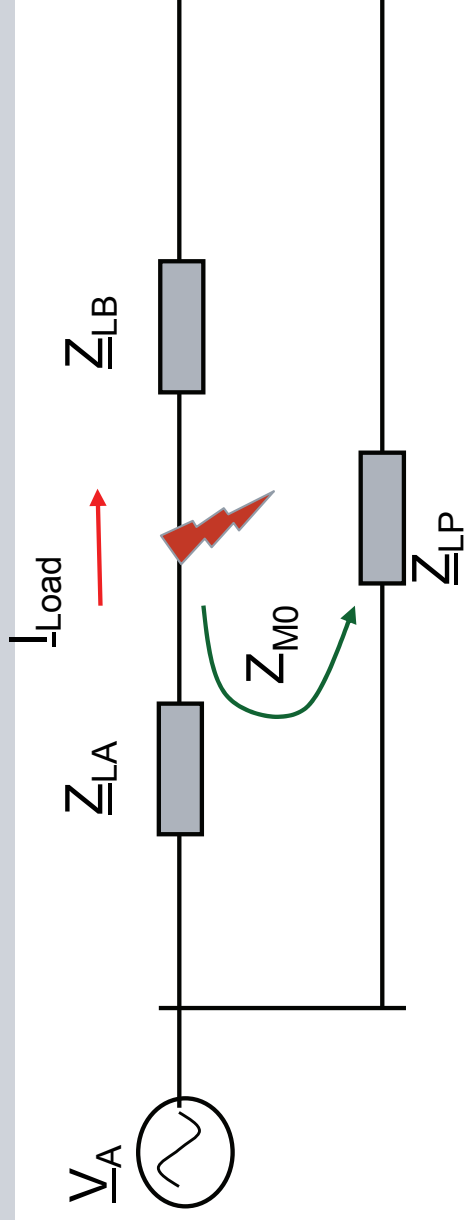


Measured 2 end fault location (L1-G with fault resistance 30 Ohm and load current 300 A)

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Example: Single and 2 end fault locator – Influence parallel line (mutual coupling of zero sequence)



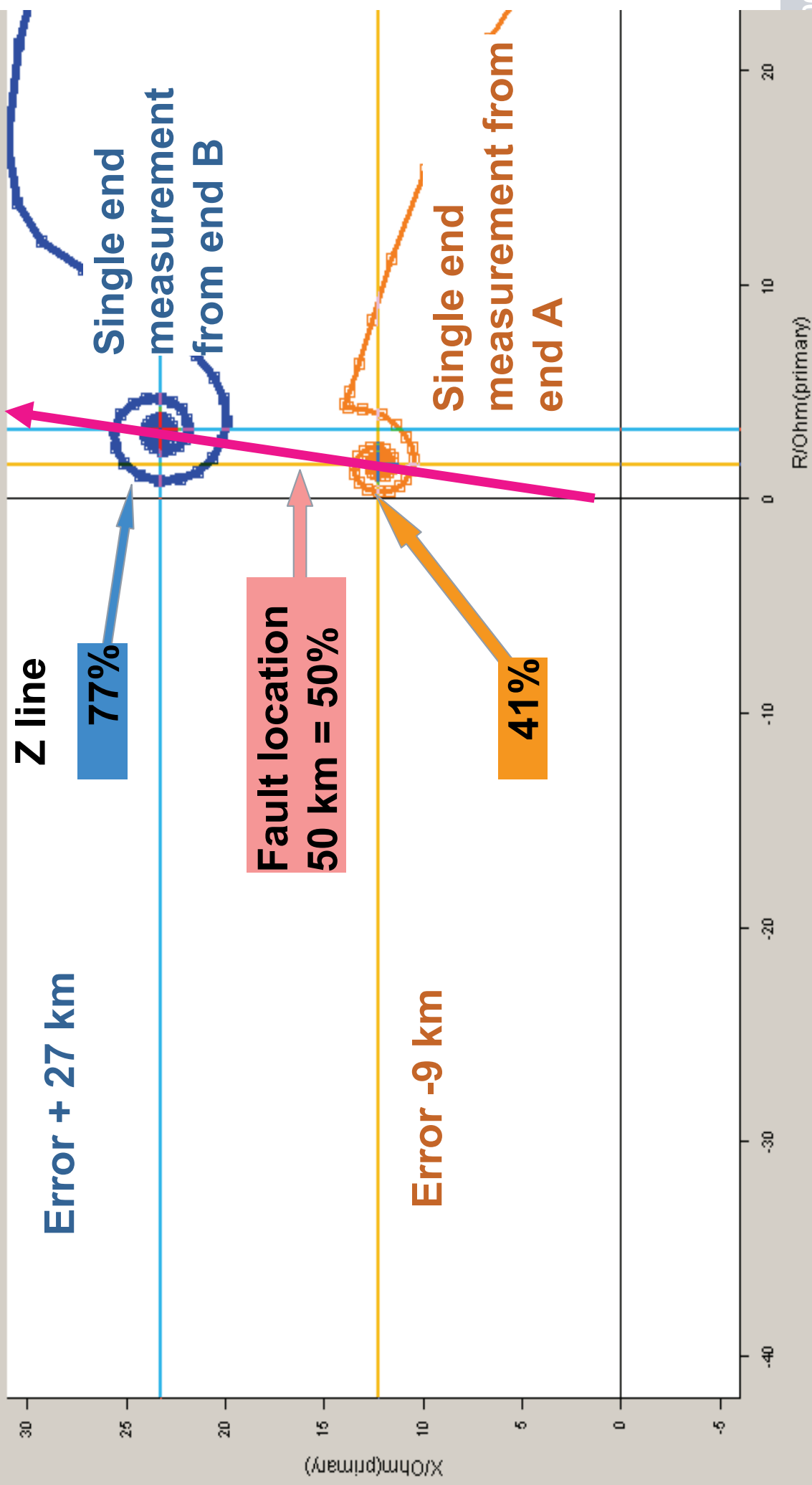
$$Z_{M0} = 15 + j100$$

$$I_{Load} = 300 \text{ A (} 10^\circ \text{ between sources)}$$

$$Z_{LA} = Z_{LB} = 2 + j15 \text{ Ohm (fault at 50\%)}$$

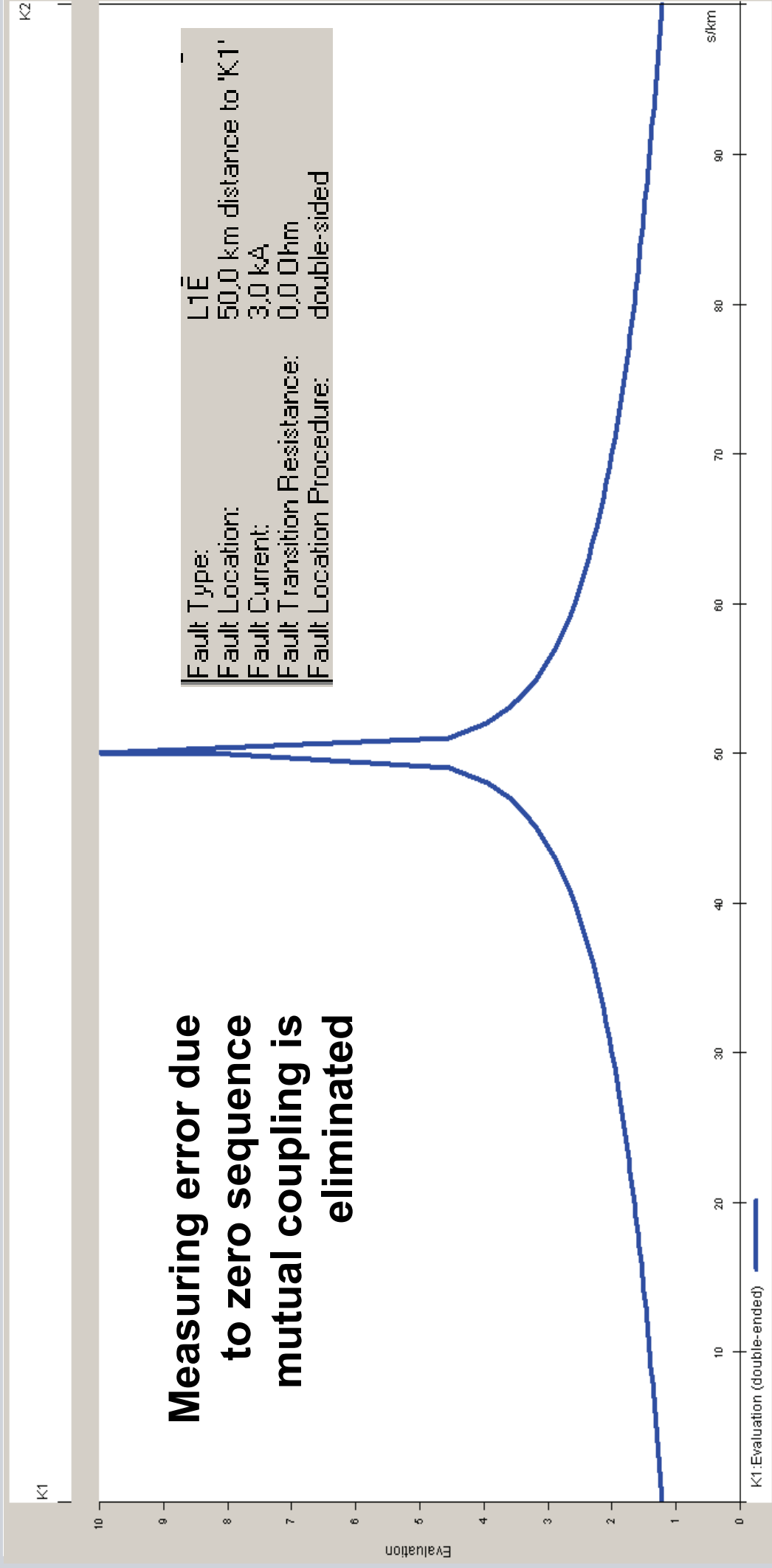
$$\text{Line length} = 100 \text{ km}$$

Measured single end fault location (L1-G with zero sequence mutual impedances of parallel line)



Measured 2 end fault location (L1-G with fault resistance 30 Ohm and load current 300 A)

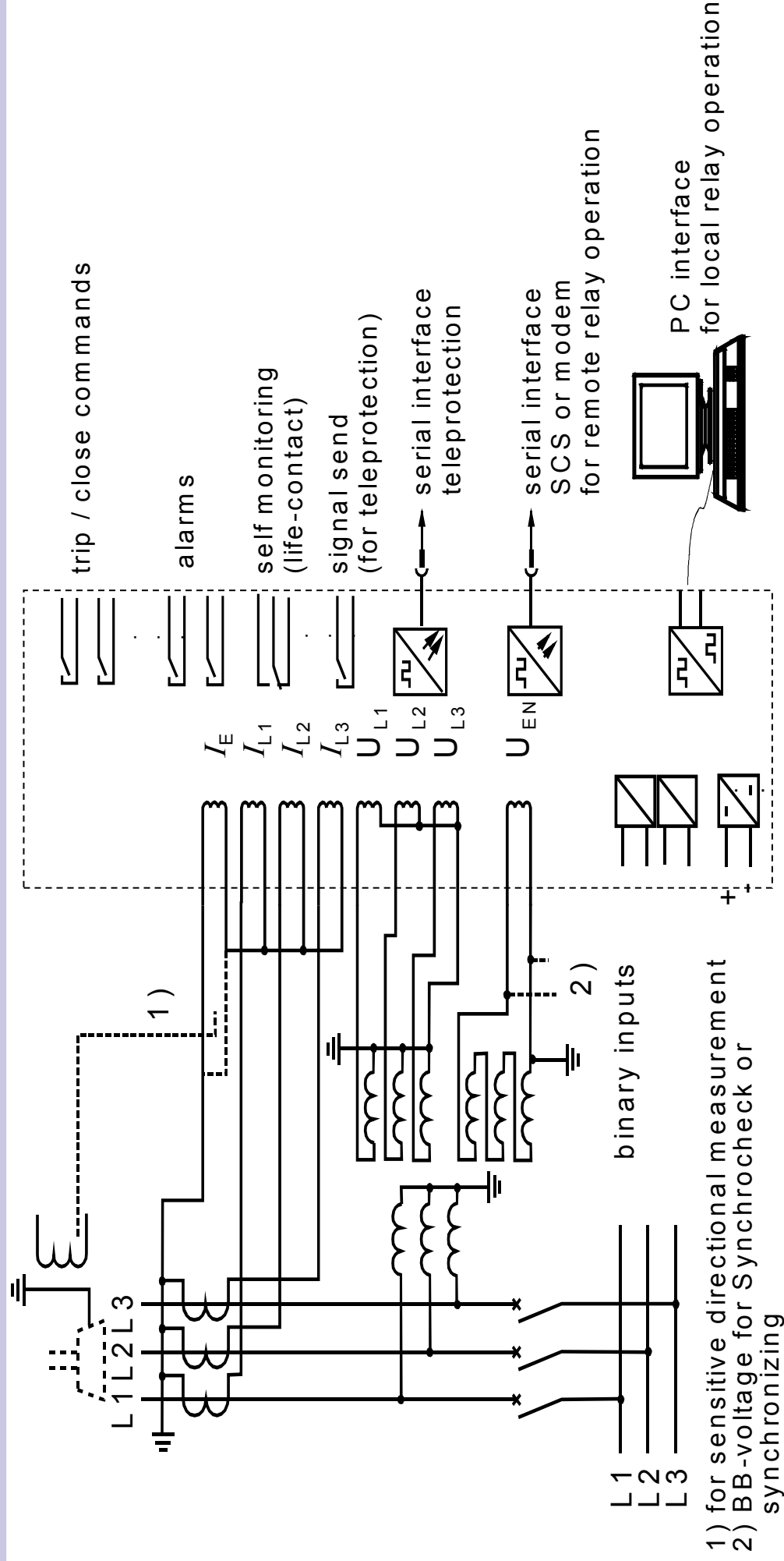
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Distance Protection Connection, Commissioning, Maintenance

Distance protection Connection

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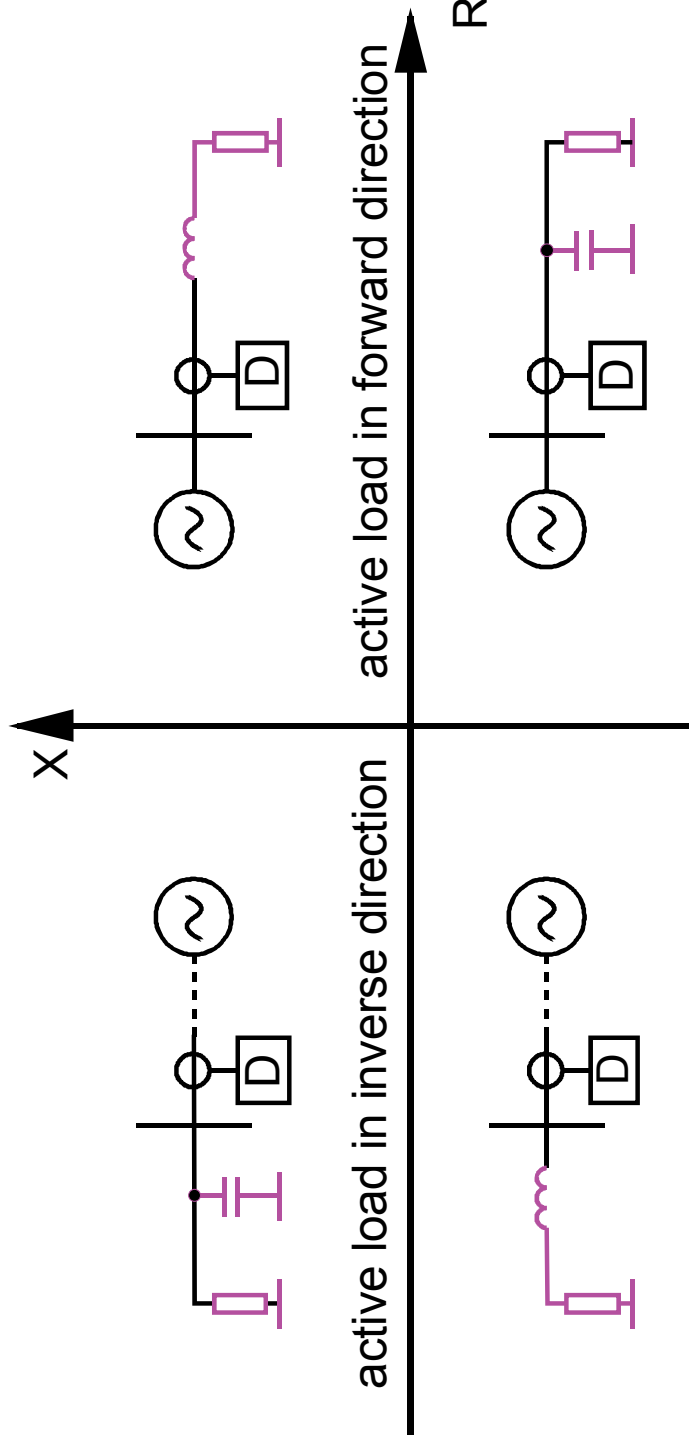


Directional test using load current

Sign of measured impedance R+jX

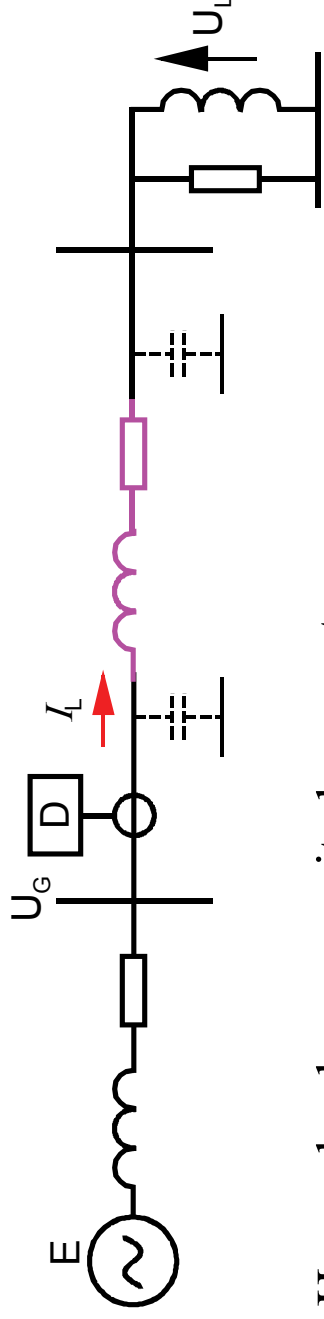
$$R = \frac{U_N^2 \cdot P_{\text{active}}}{P_{\text{active}}^2 + P_{\text{reactive}}^2}$$

$$X = \frac{U_N^2 \cdot P_{\text{reactive}}}{P_{\text{active}}^2 + P_{\text{reactive}}^2}$$

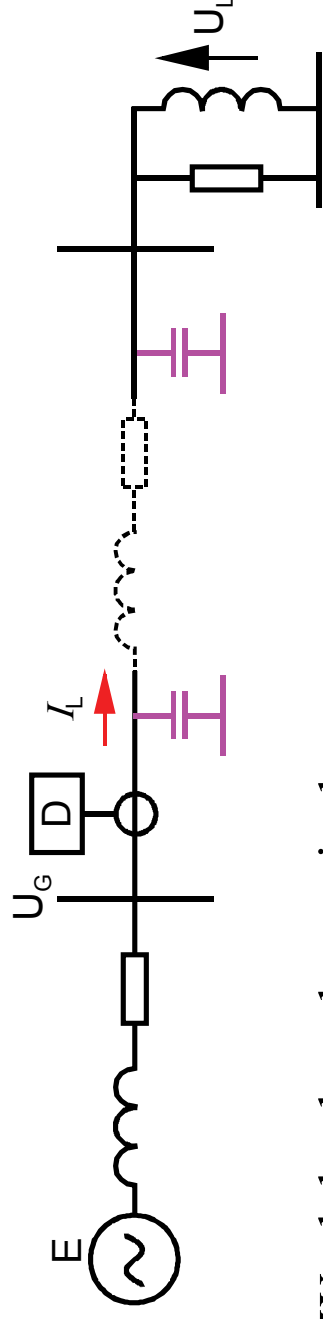
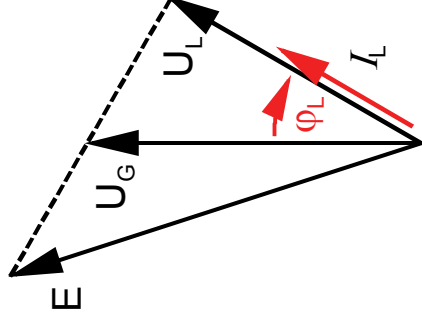


Infeed to a network Load angle at the relay

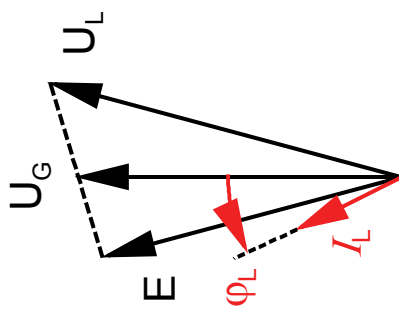
SIEMENS



Heavy load, overexcited generator

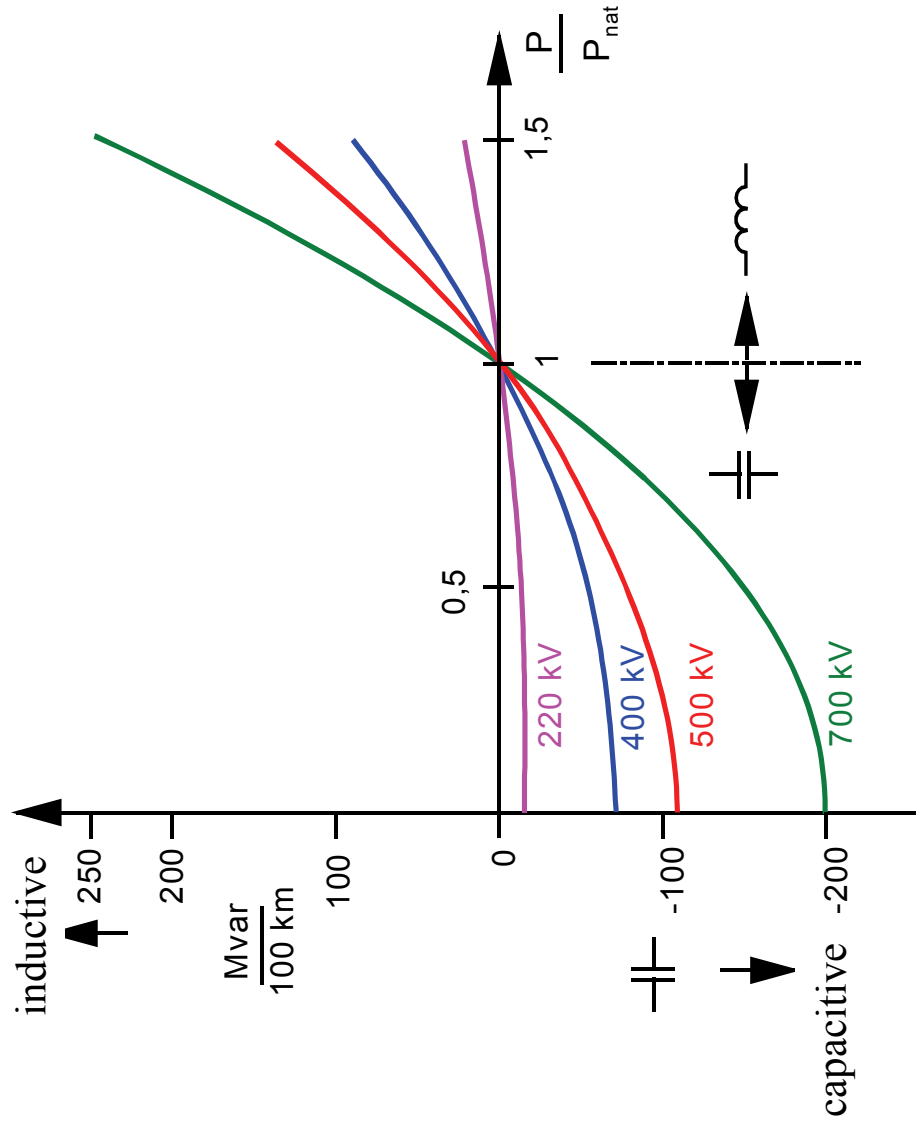


Weak load, underexcited generator

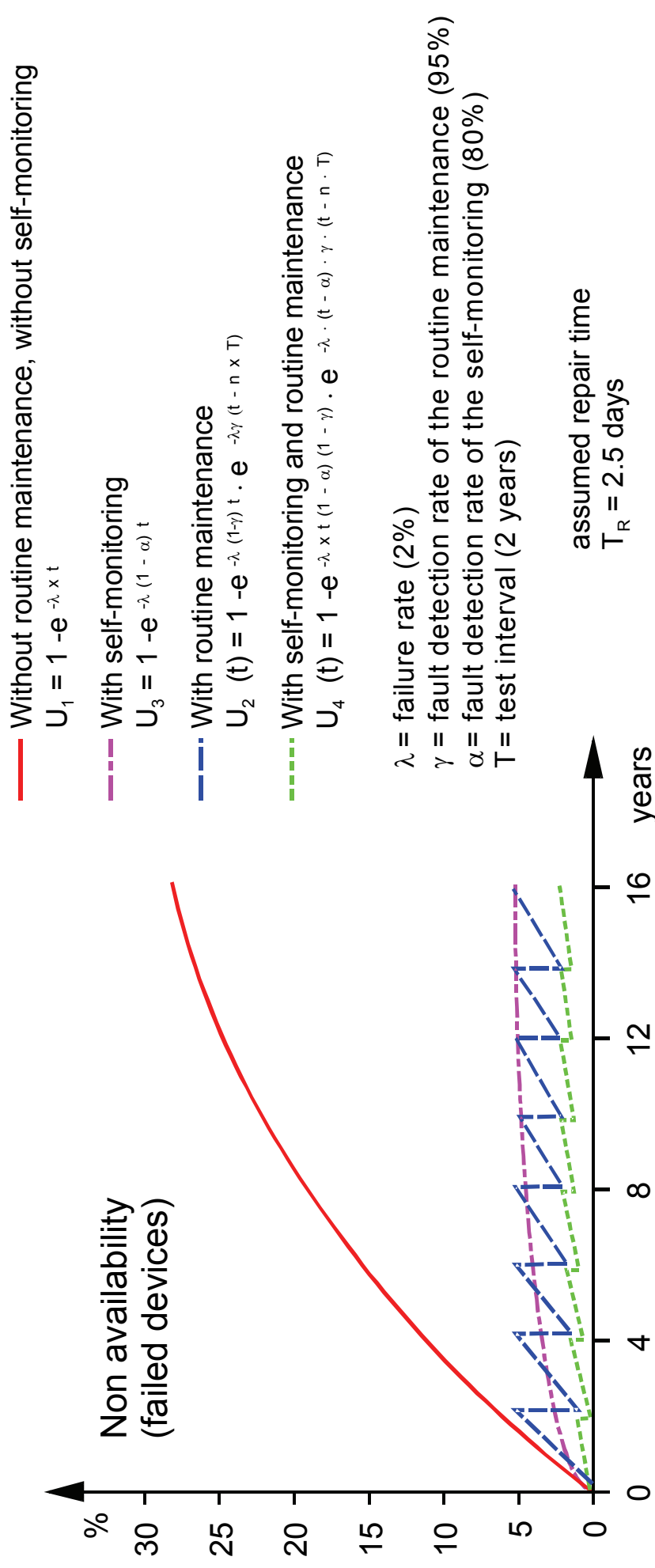


Reactive power demand of a transmission line

SIEMENS

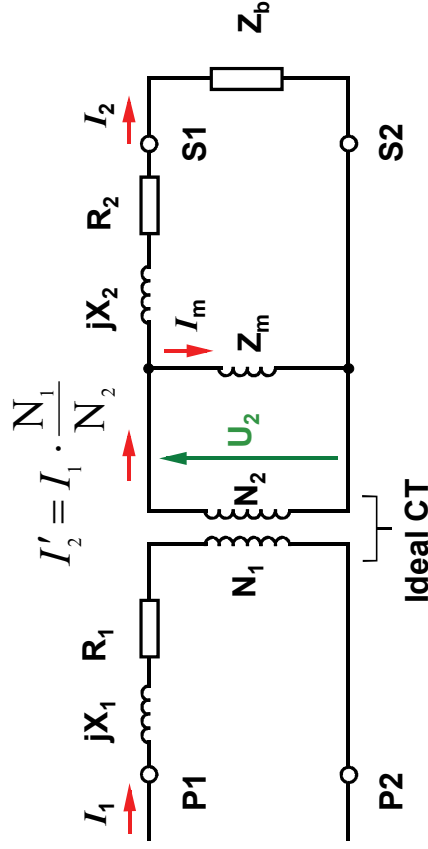


Protection availability, influence of self monitoring (values in brackets were assumed as an example)



Current and Voltage Transformers Performance Requirements

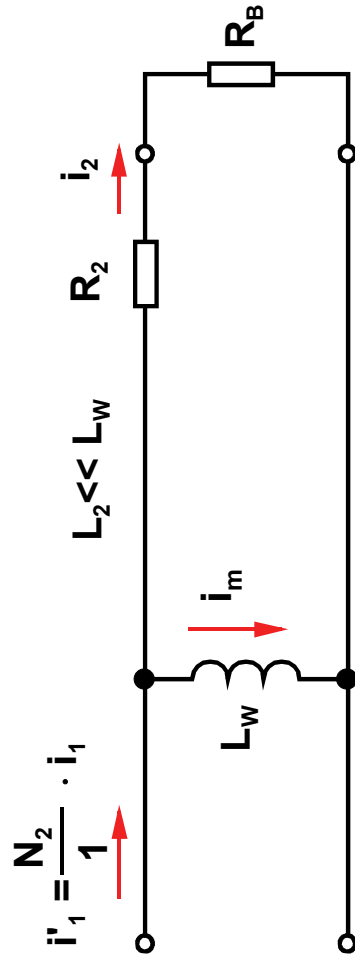
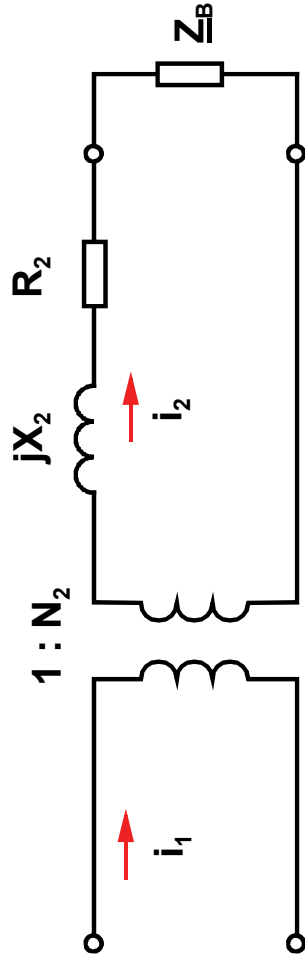
Equivalent current transformer circuit



- X_1 = Primary leakage reactance
- R_1 = Primary winding resistance
- X_2 = Secondary leakage reactance
- Z_0 = Magnetizing impedance
- R_2 = Secondary winding resistance
- Z_b = Secondary load

Note: Normally the leakage fluxes X_1 and X_2 can be neglected

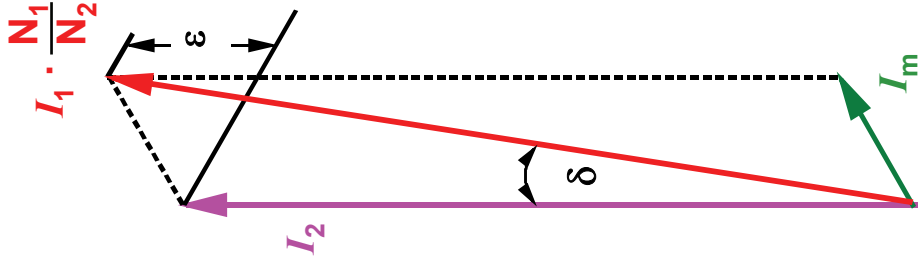
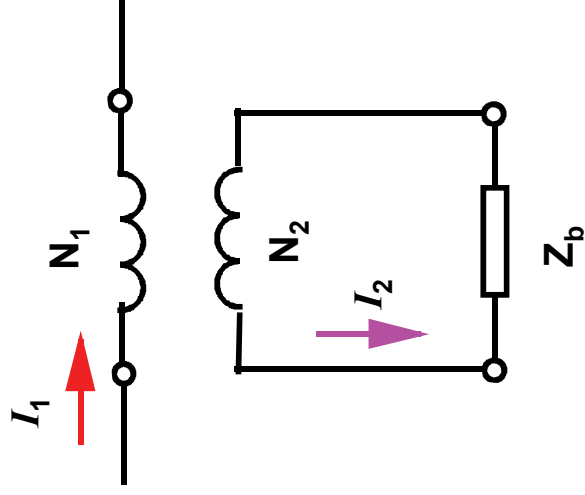
Current transformer, simplified equivalent circuit



Current transformer:

Phase displacement (δ) and current ratio error (ε)

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Current transformer, Standard for steady-state performance

IEC 60044-1 specifies the following classes:

Accuracy class	Current error at nominal current (I _n)	Angle error δ at rated current I _n	Total error at $n \times I_n$ (rated accuracy limit)
5P	$\pm 1 \%$	± 60 minutes	5 %
10P	$\pm 5\%$	—	10 %

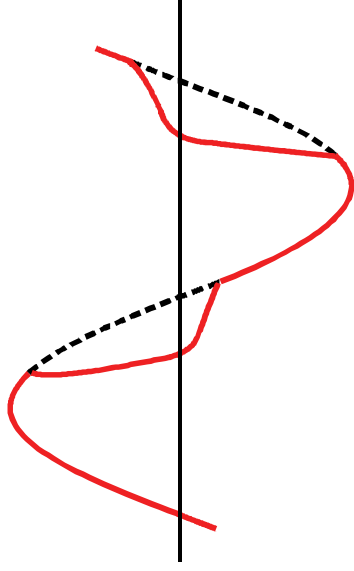
Current transformers, Standard for transient performance

IEC 60044-6 specifies four classes:

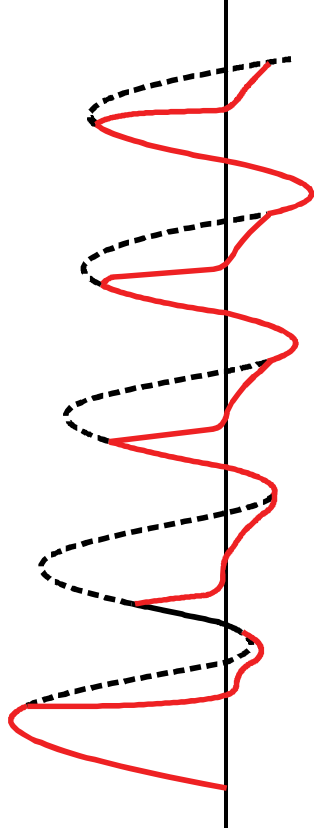
Class	Error at rated current		Maximum error at rated accuracy limit	Remanence
	Ratio error	Angle error		
TPX (closed iron core)	$\pm 0,5 \%$	$\pm 30 \text{ min}$	$\hat{\epsilon} \leq 10\%$	no limit
TPY with anti-remanence air gap	$\pm 1,0 \%$	$\pm 30 \text{ min}$	$\hat{\epsilon} \leq 10\%$	$< 10 \%$
TPZ linear core	$\pm 1,0 \%$	$\pm 180 \pm 18 \text{ min}$	$\hat{\epsilon} \leq 10\%$ (a.c. current only)	negligible
TPS closed iron core	Special version for high impedance protection (Knee point voltage, internal secondary resistance)			No limit

Current transformer saturation

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Steady-state saturation with AC current

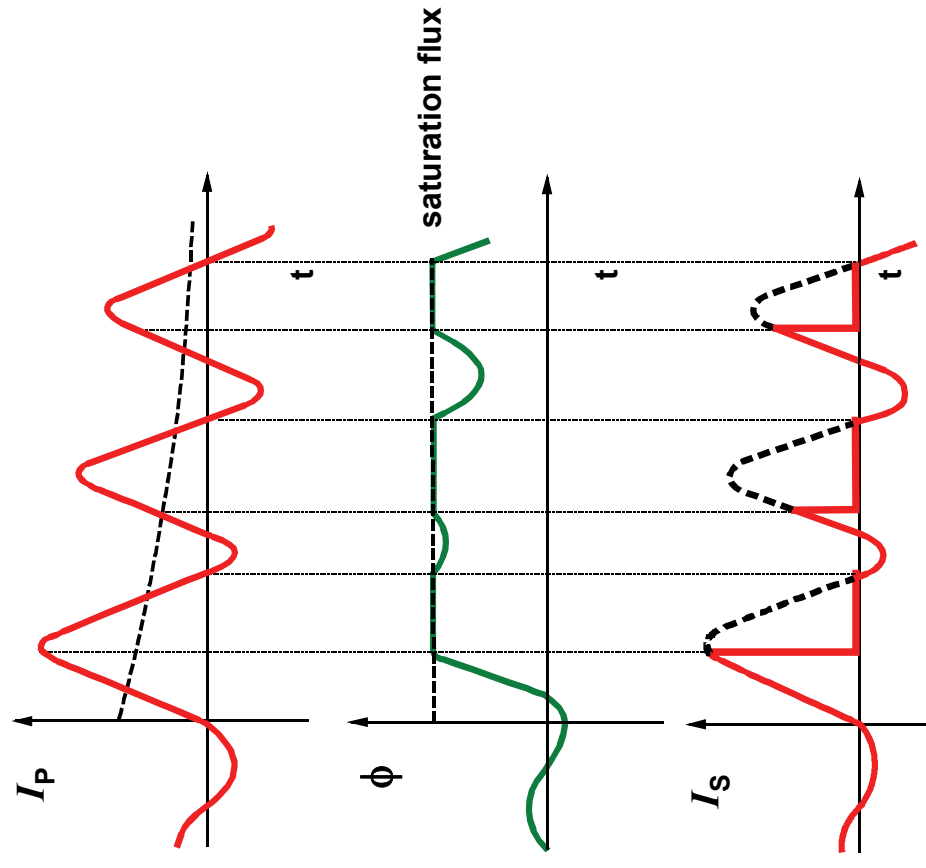


Transient saturation with offset current

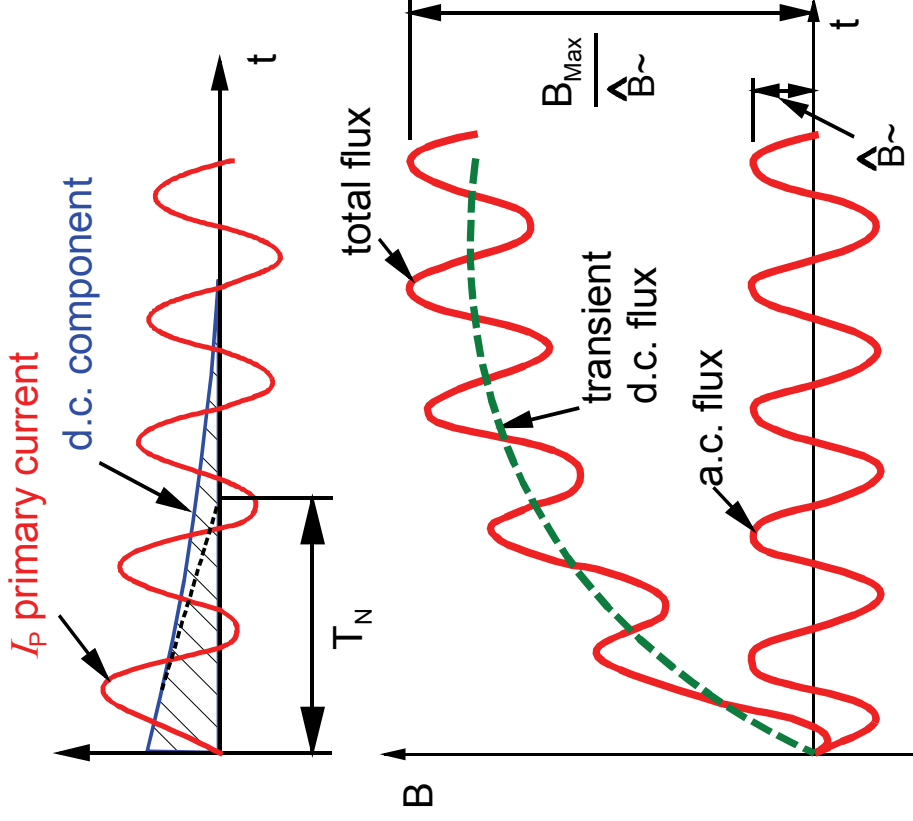
CT saturation

Currents and magnetising

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Course of CT-flux during off-set short-circuit current



$$\frac{B}{\hat{B}_{\sim}} = 1 + \frac{\omega \cdot T_N \cdot T_S}{T_N - T_S} \left(e^{\frac{t}{T_N}} - e^{\frac{t}{T_S}} \right)$$

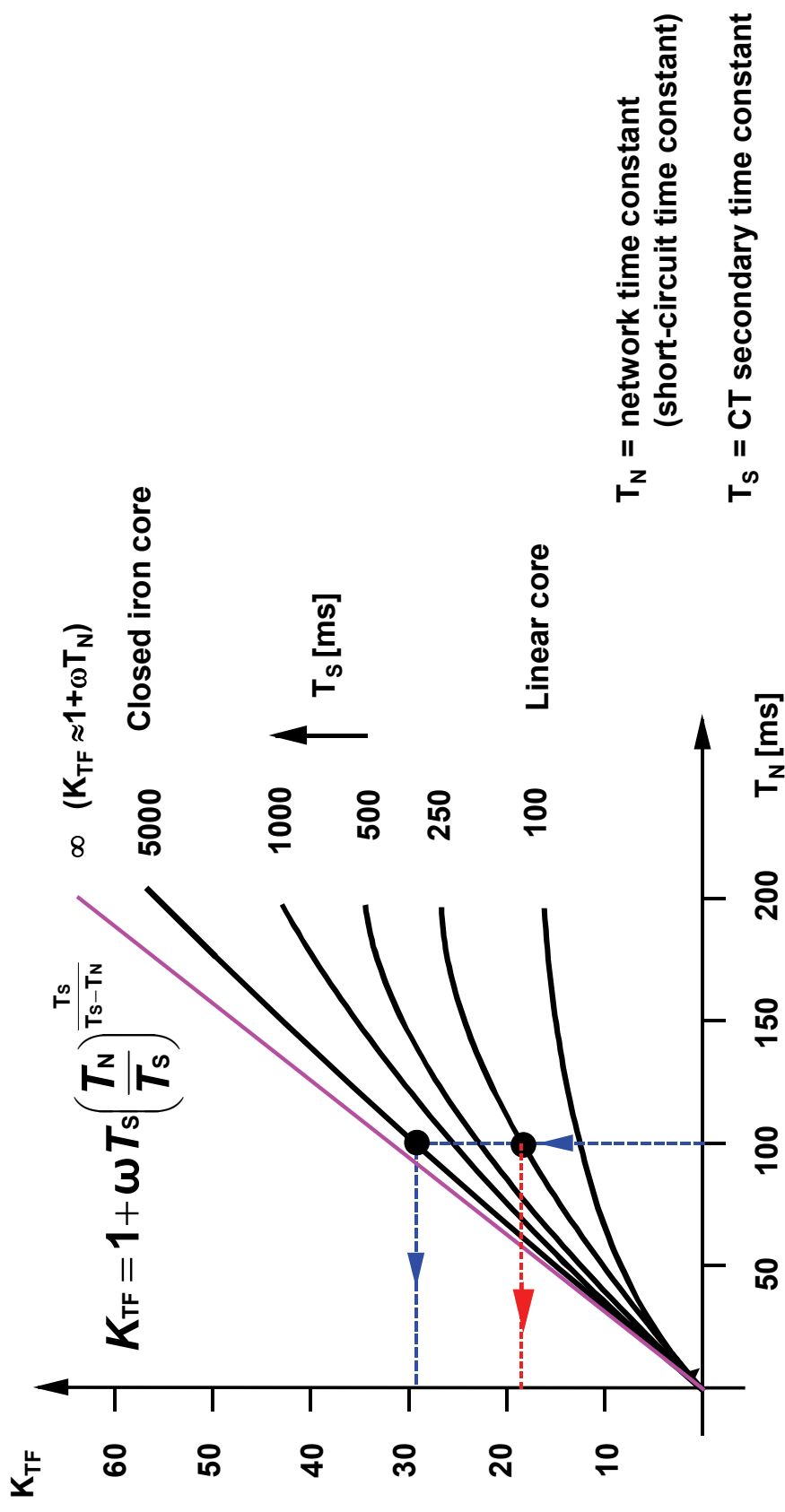
$$\frac{B_{Max}}{B_{\sim}} = 1 + \omega \cdot T_S \cdot \left(\frac{T_N}{T_S} \right)^{\frac{T_S}{T_S - T_N}}$$

$$t_{B_{Max}} = \frac{T_N \cdot T_S}{T_S - T_N} \cdot \ln \frac{T_S}{T_N}$$

$$T_S = \frac{L_W}{R_i + R_B} = \frac{1}{\omega \cdot \tan \delta}$$

For 50 Hz: $T_S = \frac{10900}{\delta_{[min]}} [ms]$

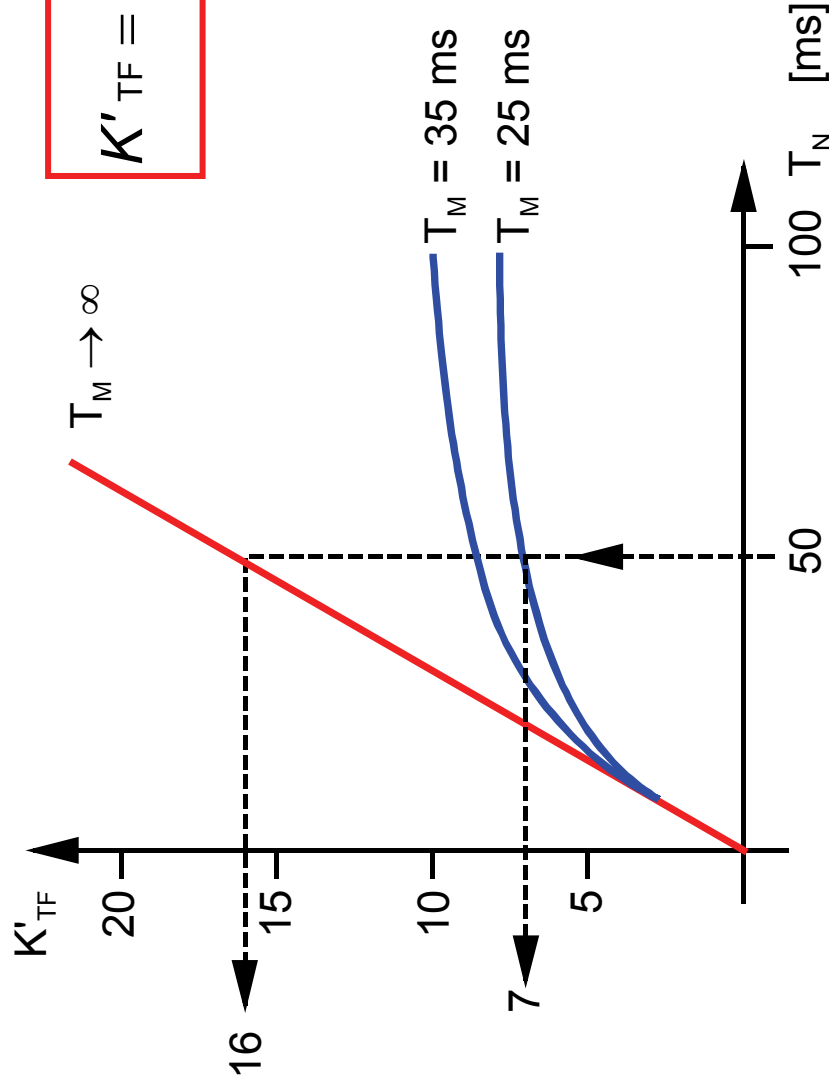
CT transient over-dimensioning factor K_{TF}



CT with closed iron core,

Over-dimensioning factor for a specified time to saturation (T_M)

SIEMENS

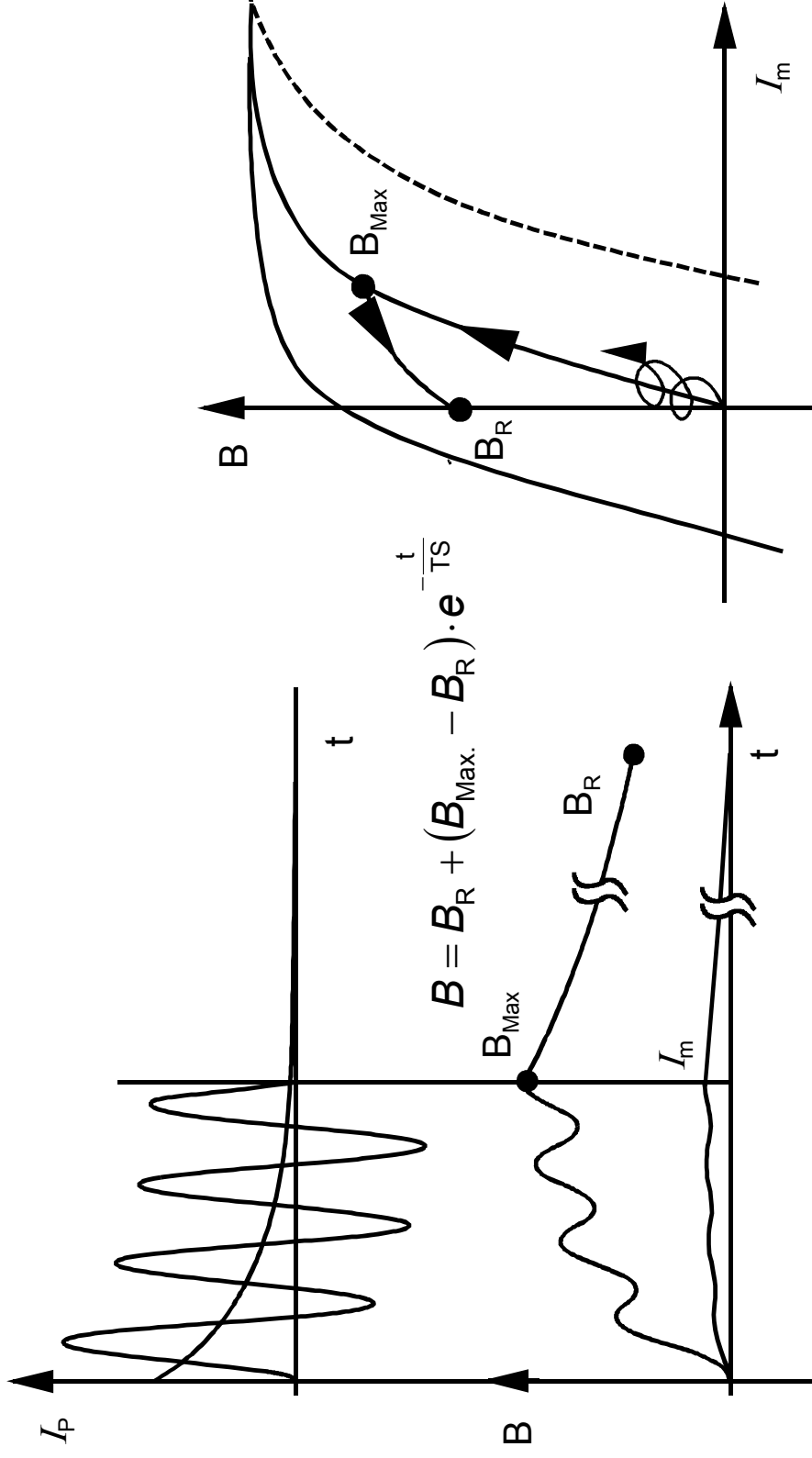


$$K'_{TF} = 1 + \omega T_N = 1 + \frac{X_N}{R_N}$$

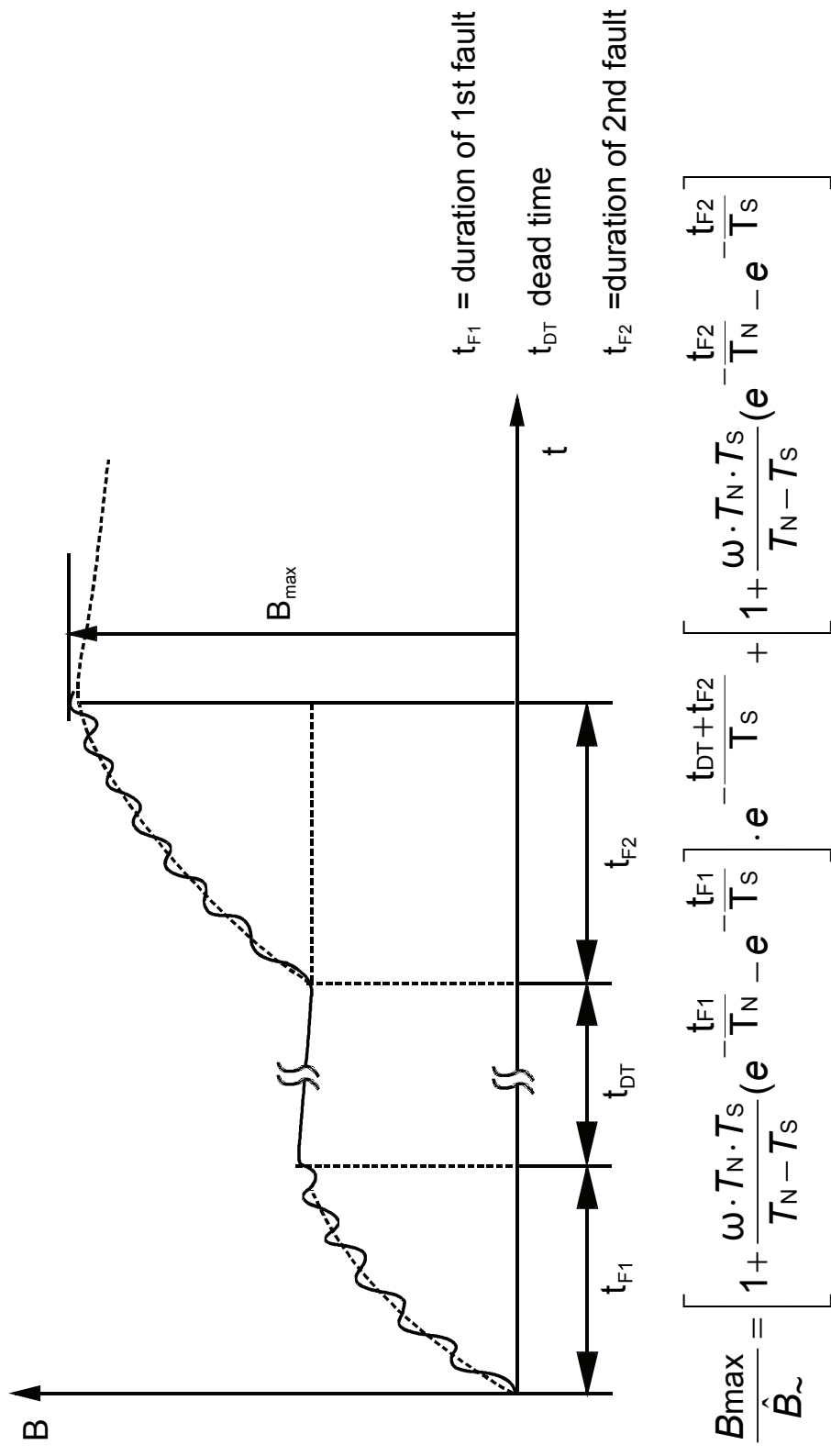
$$K'_{TF} = 1 + \omega T_N \left(1 - e^{-\frac{T_M}{T_N}} \right)$$

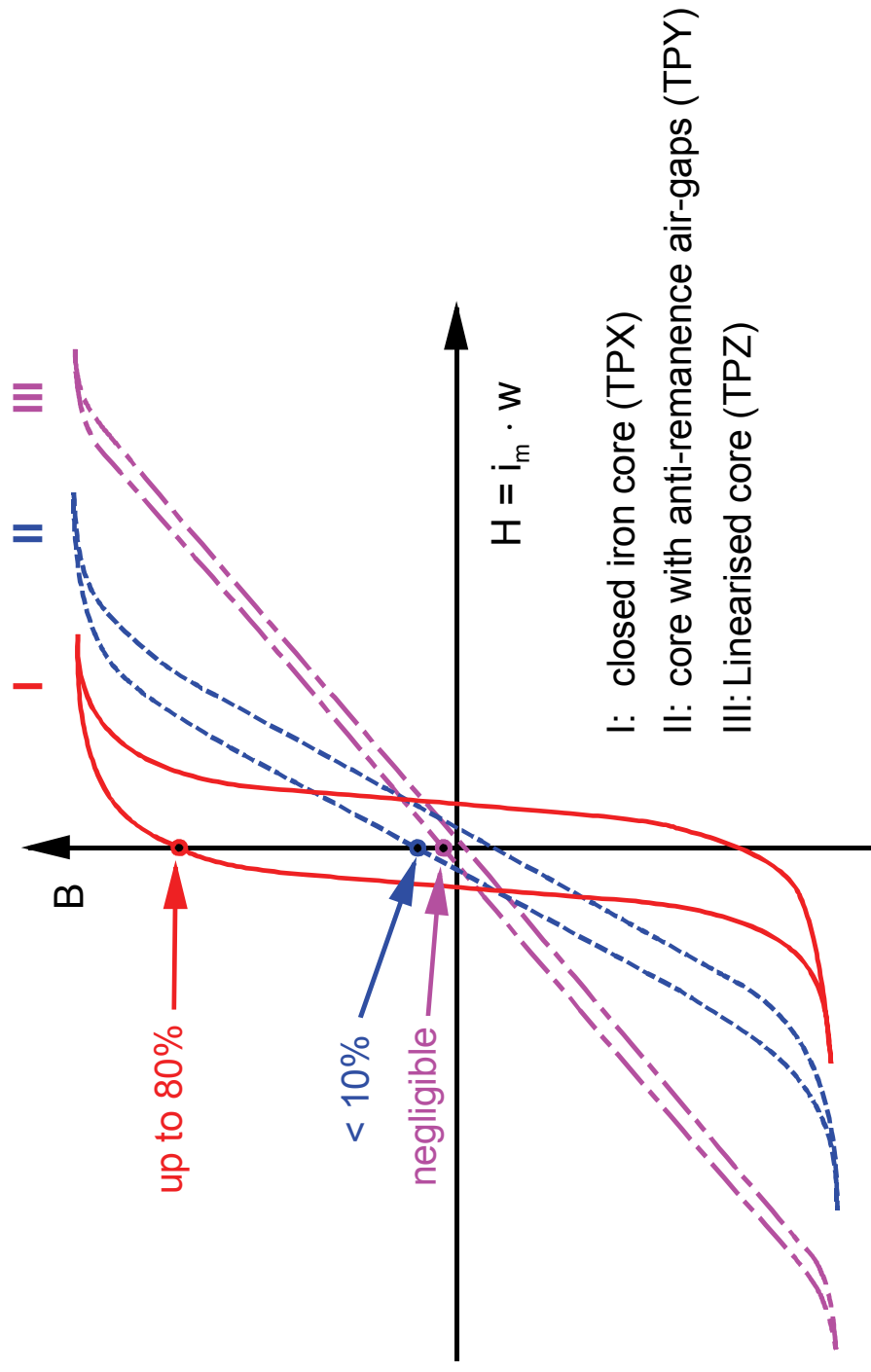
Current transformer magnetising and de-magnetising

SIEMENS



Course of flux in the case of non-successful auto-reclosure

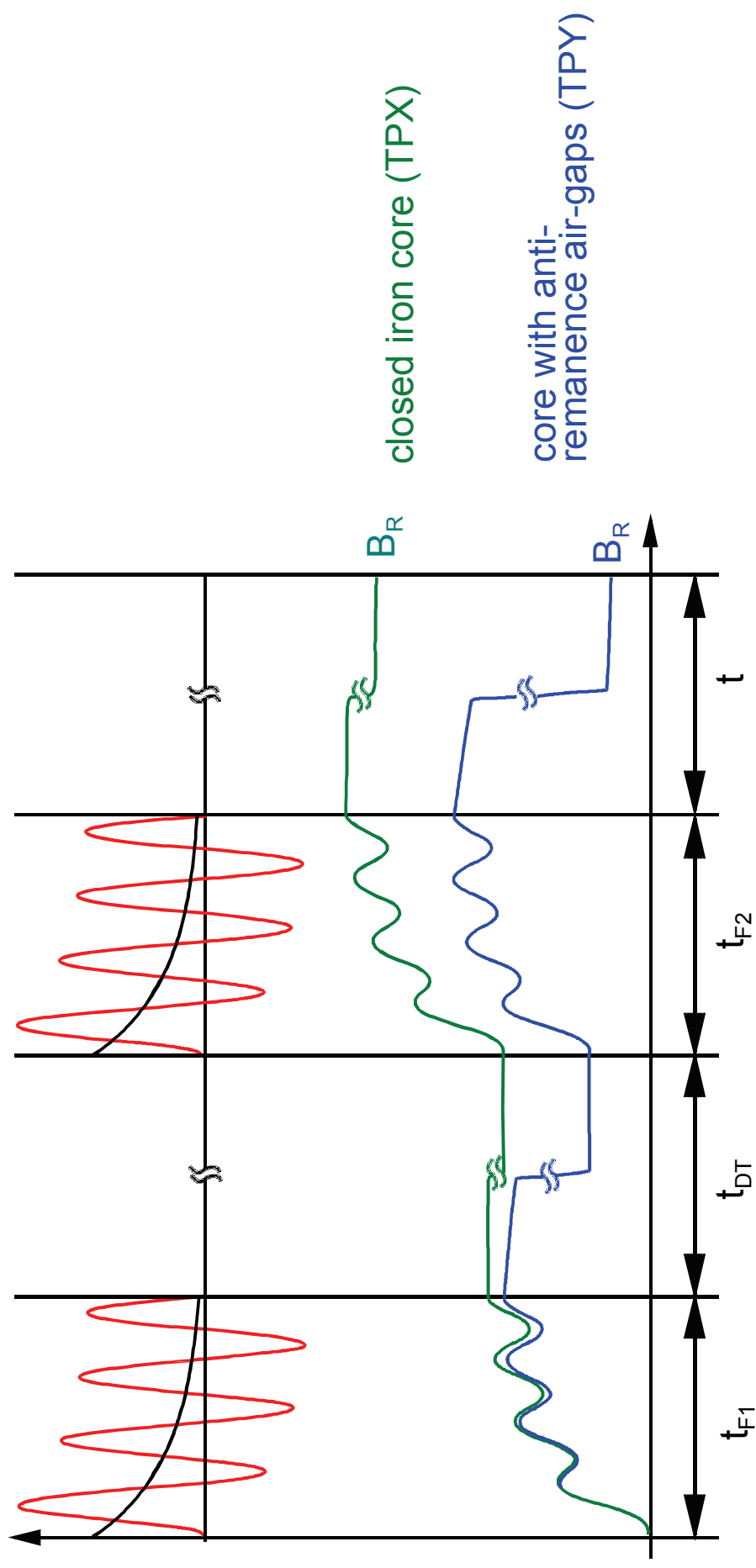




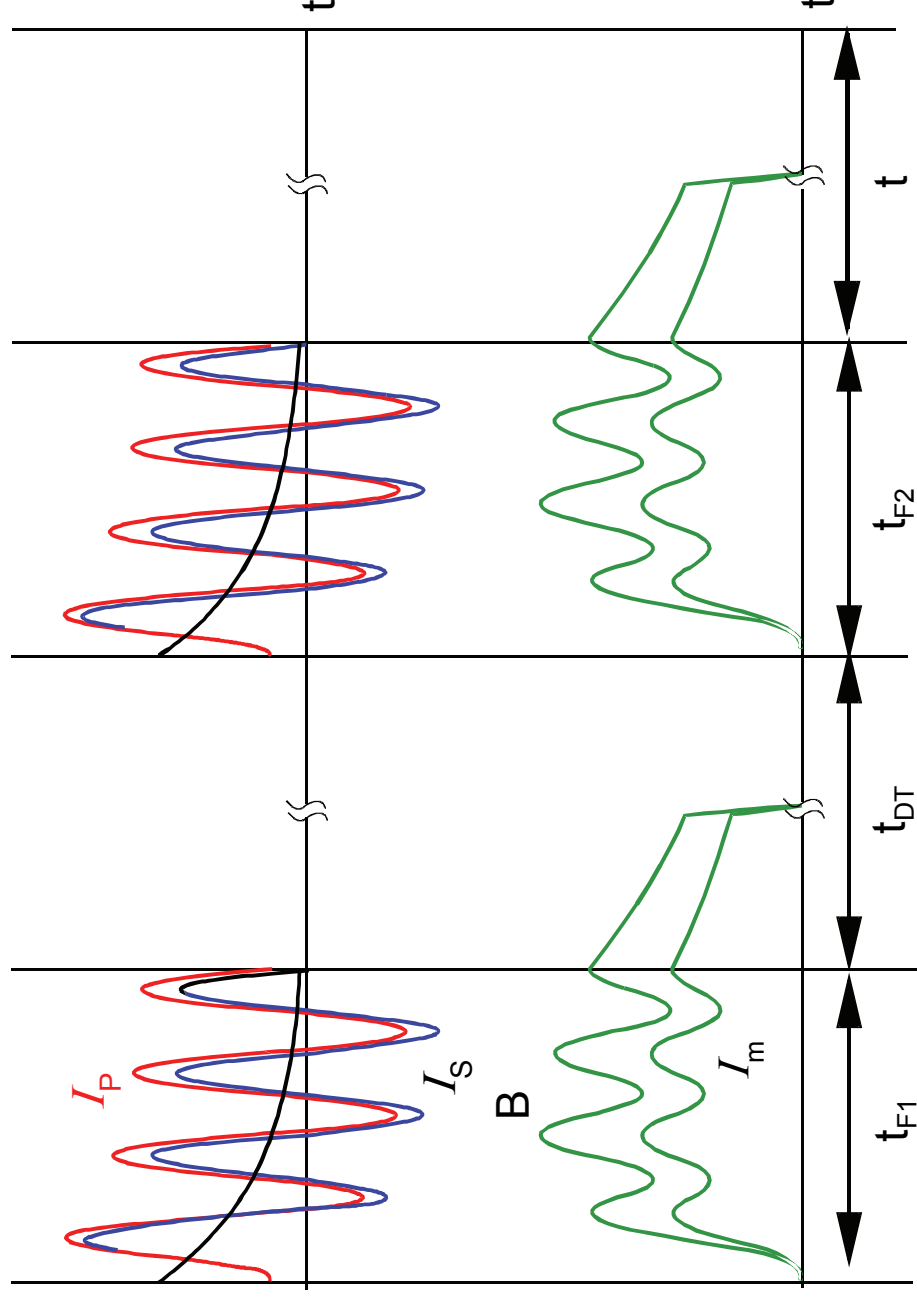
Current transformers TPX und TPY

SIEMENS

Course of the flux with non-successful auto-reclosure



Current transformer with linear core (TPZ), Course of the flux with non-successful auto-reclosure



Standards of voltage transformers

VT classes to IEC 60044-2

Class designation	Permissible error at $0.05 \cdot U_N$ and $1.0 \cdot U_N$	
	Voltage error F_U	Angle error δ
3P	$\pm 3.0 \%$	120 minutes
5P	$\pm 6.0 \%$	240 minutes

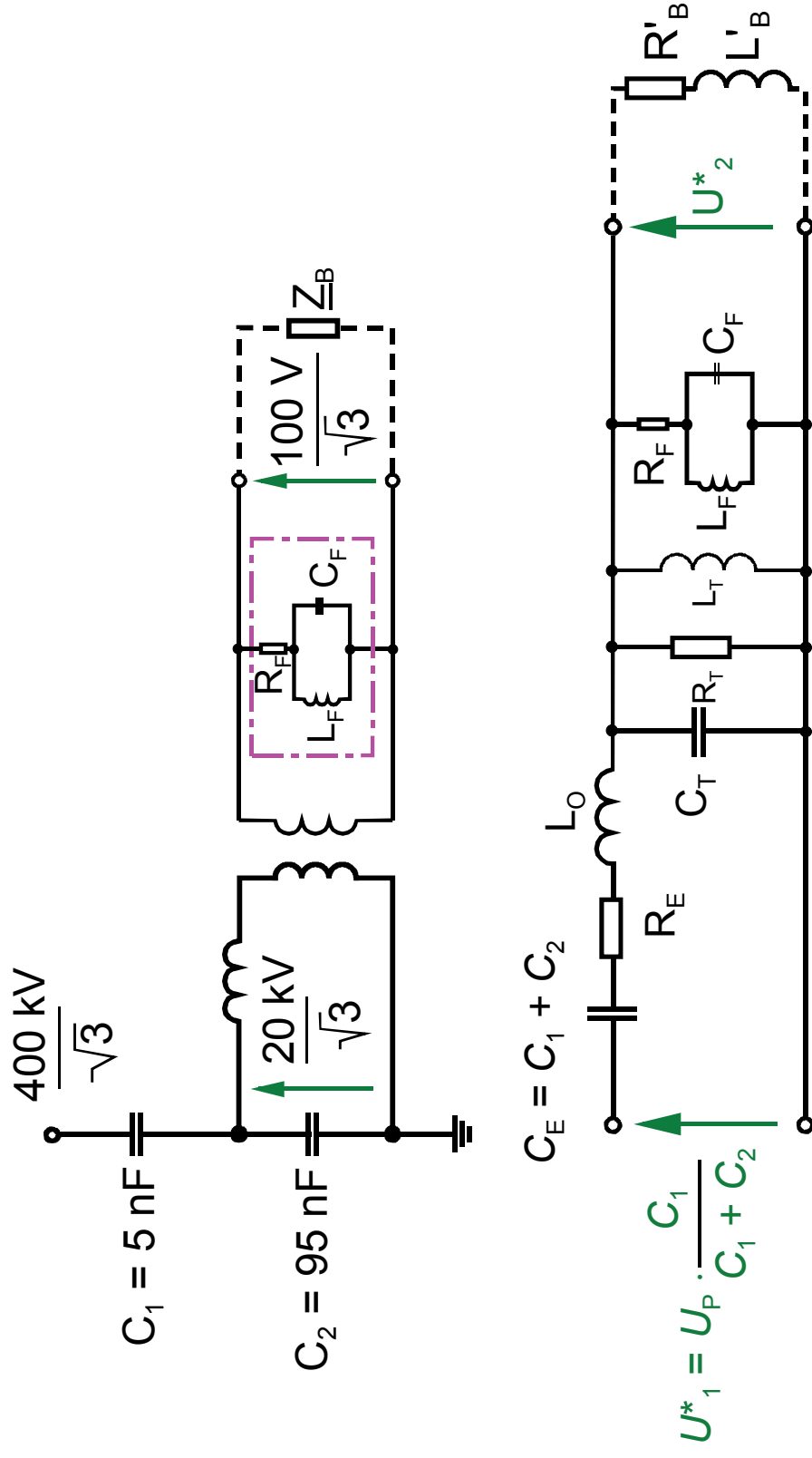
All 3P and 5P protection CTs must additionally comply with one of the below VT metering classes!

VT classes for measurement IEC 60044-2

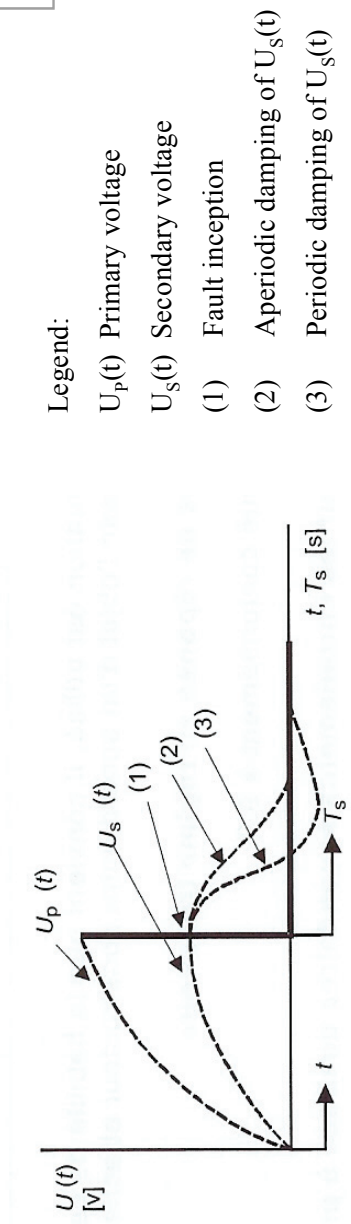
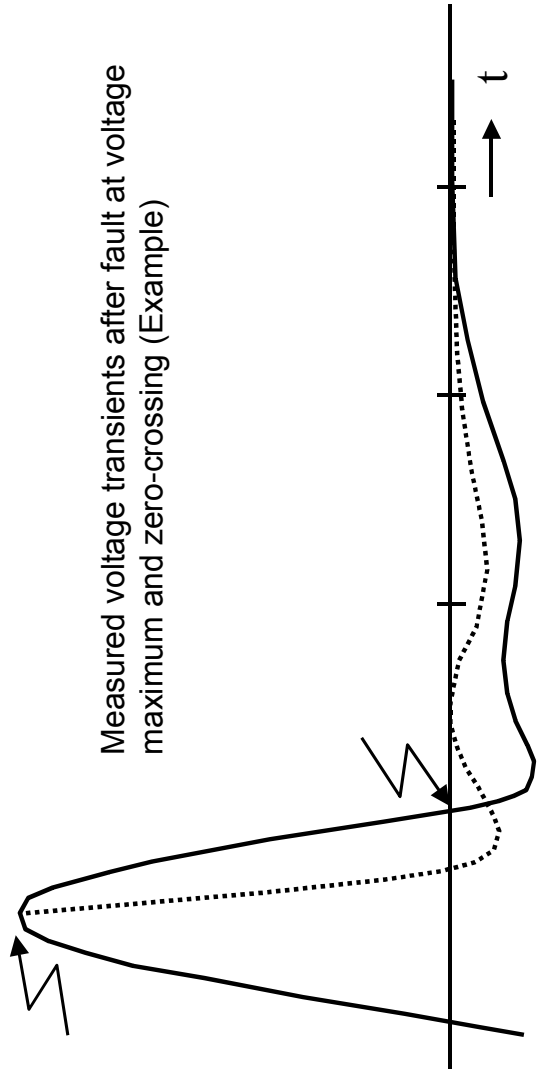
Class designation	Permissible voltage error in % at $1.0 \cdot U_N$	Permissible angle error in minutes at $1.0 \cdot U_N$
0.1	0.1	5
0.2	0.2	10
0.5	0.5	20
1	1	30
3	3	Not determined

Capacitive voltage transformer, Equivalent circuit

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Transient performance of CVTs, Recommendations acc. to IEC 60044-5



Recommendations to IEC 60044-5

Time T_s in ms	Ratio $\frac{U_s(t)}{\sqrt{2} \cdot U_s} \cdot 100\%$		
	Classes		
	3PT1 6PT1	3PT2 6PT2	3PT3 6PT3
10	---	≤ 25	≤ 4
20	≤ 10	≤ 10	≤ 2
40	≤ 10	≤ 2	≤ 2
60	≤ 10	≤ 0.6	≤ 2
90	≤ 10	≤ 0.2	≤ 2

CT dimensioning

$$ALF' = ALF \cdot \frac{P_i + P_{BN}}{P_i + P_B} = ALF \cdot \frac{R_{CT} + R_{BN}}{R_{CT} + R_B}$$

$$ALF = ALF' \cdot \frac{P_i + P_B}{P_i + P_{BN}} = ALF' \cdot \frac{R_{CT} + R_B}{R_{CT} + R_{BN}}$$

with $ALF' \geq K_{OD} \cdot \frac{I_K}{I_N}$

$$K_{OD} \geq K_{TF} \cdot K_{Rem}$$

$$K_{Rem} = \frac{1}{1 - \frac{\% \text{ Remanence}}{100}}$$

rated CT burden: P_{BN}
internal burden of the CT: $P_i = R_i \cdot I_{2N}^2$

Actual connected burden : $P_B = R_B \cdot I_{2N}^2$

$R_B = R_i + R_R$ = burden resistance
 R_i = resistance of connecting cables
 R_R = burden resistance of the relay

Theory:

No saturation for the total short-circuit duration:

$$K'_{TF} = \frac{B_{Max}}{\hat{B}} = 1 + \omega T_N = 1 + \frac{X_N}{R_N}$$

No saturation for the specified time t_M :

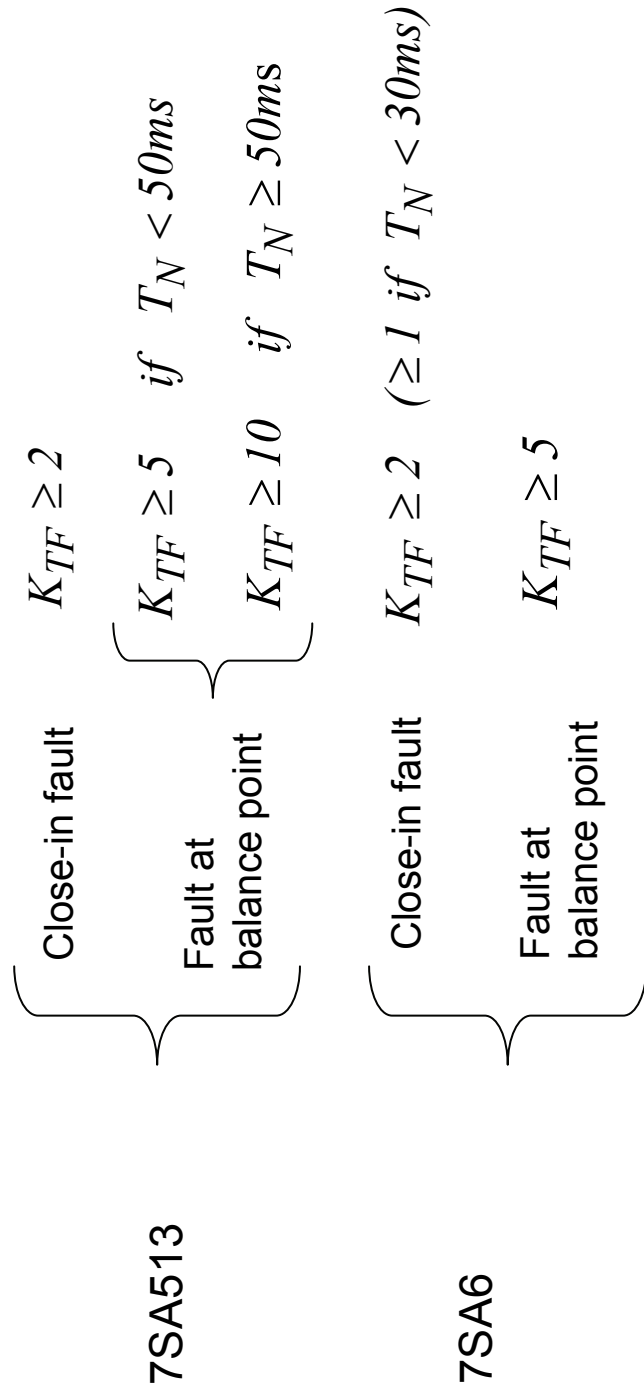
$$K''_{TF} = \left[1 + \frac{\omega \cdot T_N \cdot T_s}{T_N - T_s} (e^{\frac{t_M}{T_N}} - e^{\frac{t_M}{T_s}}) \right]$$

Practice: Use of K_{TF} - values recommended by vendors

Distance relays, practical CT requirements

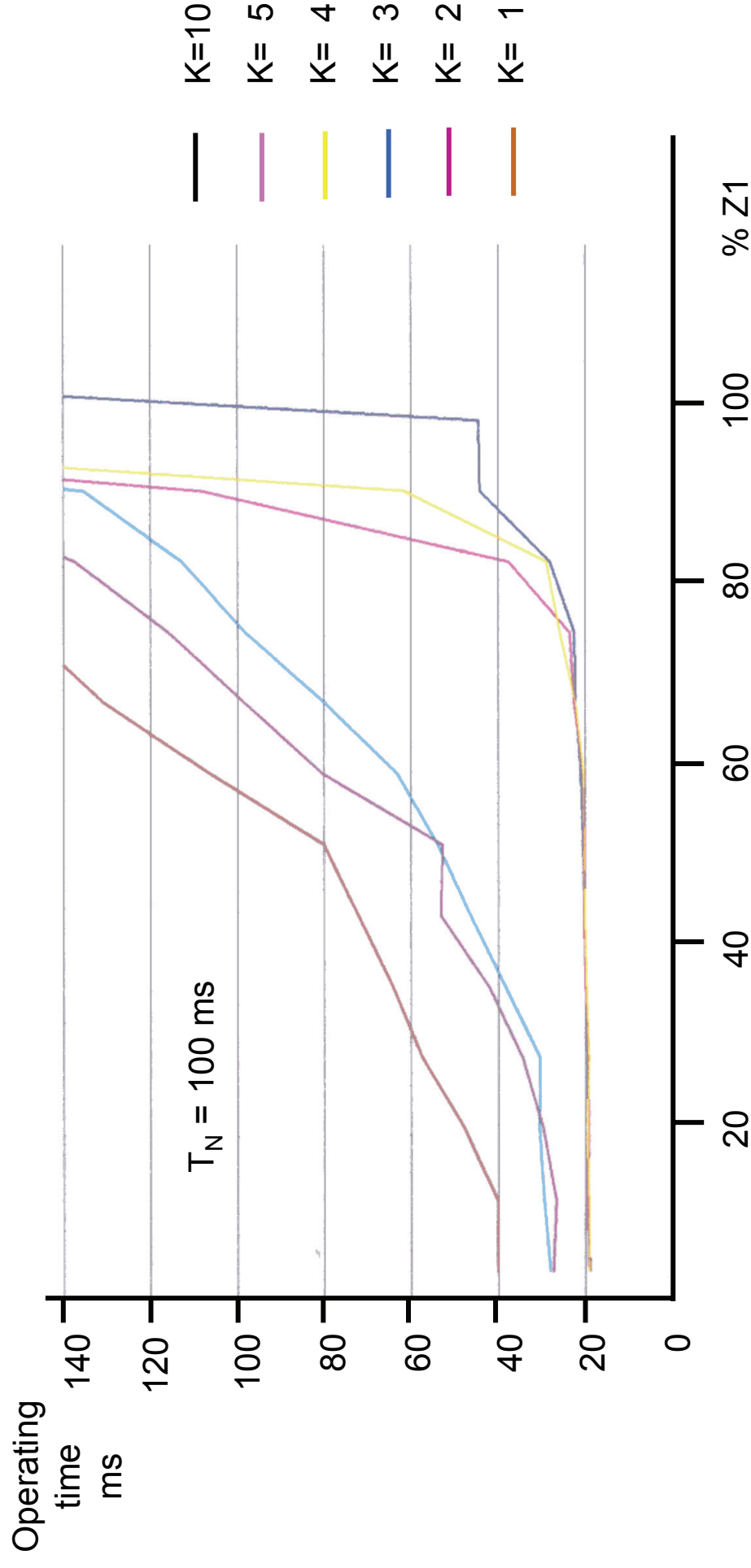
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Transient over-dimensioning factors K_{TF} (ARC not considered)



7SA6 / 7SA522: Operating time with CT saturation Influence of CT dimensioning

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Distance protection, practical CT requirements Over-dimensioning factor K_{TF} including ARC

General:

$$K_{TF-ARC} = \left[1 + \frac{\omega \cdot T_N \cdot T_S}{T_N - T_S} (e^{\frac{t_{F1}}{T_N} - e^{\frac{t_{F1}}{T_S}}}) \cdot e^{-\frac{t_{DT} + t_{F1}}{T_S}} + \left[1 + \frac{\omega \cdot T_N \cdot T_S}{T_N - T_S} (e^{\frac{t_{F2}}{T_N} - e^{\frac{t_{F2}}{T_S}}}) \right] \right]$$

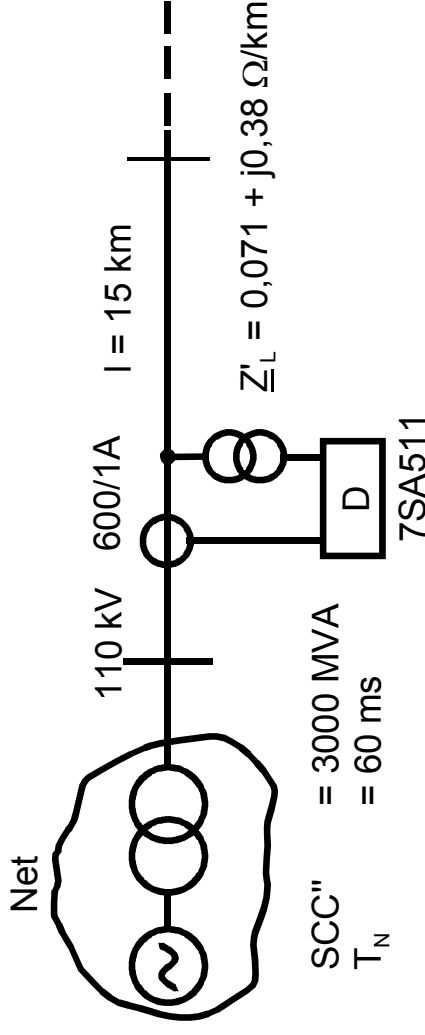
This formula is applicable **with TPY type CTs** where T_S is in the range of some 100 ms resulting in a considerable induction decay during the dead time. (see IEC 60044-6).

With TPZ type CTs, this formula is not applicable because T_S is only about 100 ms and the flux is completely decaying during the dead time. The auto-reclosure must therefore not be considered with dimensioning of TPZ current transformers.

With **closed iron core CTs** ($T_S > T_N$):

$$K'_{TF-ARC} = 1 + \omega \cdot T_N \cdot \left(1 - e^{-\frac{T_{F1}}{T_N}} \right) + K_{TF- \text{without ARC}}$$

CT dimensioning for distance protection Calculation example (1)



Given:

line-configuration, see above

CTs: 600/1

Connecting leads CT to relay: 80 m one way, 2,5 mm² Cu

Searched:

1. Rated accuracy limiting factor of the CTs (Type TPX, 5P, 30 VA)
2. Rated accuracy limiting factor when the auto-reclosure cycle COCO is considered (circuit breaker operating time: 60 ms, dead time: 0.4 s))

CT dimensioning for distance protection

Calculation example (2)

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Condition 1): Close-in faults without ARC

The maximum short-circuit current is:

$$I_{K_{Max.}} = \frac{S_N''}{1.1 \cdot \sqrt{3} \cdot U_N} = \frac{3000 \text{ MVA}}{1.1 \cdot \sqrt{3} \cdot 110} = 14.4 \text{ kA}$$

For relay 7SA511 with $T_N = 60 \text{ ms}$: $K_{TF} = 3$.
Therefore we get:

$$ALF' = 3 \cdot \frac{14400}{600} = 72$$

Condition 2): Fault near line end without ARC

The source impedance is

$$X_s \approx Z_s = \frac{1.1 \cdot U_s}{\sqrt{3} \cdot I_s} = \frac{1.1 \cdot 110 \text{ kV}}{\sqrt{3} \cdot 14.4 \text{ kA}} = 4.85 \Omega$$

$$T_N = \frac{L_s}{R_s} = \frac{X_s / \omega}{R_s}$$

$$\text{Herewith: } R_s = \frac{X_s}{\omega \cdot T_N} = \frac{4.85}{314 \cdot 0.06} = 0.26 \Omega$$

Fault at the balance point (85% line length):

$$X_L = 0.85 \cdot 15 \cdot 0.38 = 4.8 \Omega$$

$$R_L = 0.85 \cdot 15 \cdot 0.071 = 0.91 \Omega$$

The corresponding fault current is:

$$I_{F\text{-Balance point}} = \frac{1.1 \cdot U_N / \sqrt{3}}{Z_s + Z_L} \approx \frac{1.1 \cdot U_N / \sqrt{3}}{X_s + X_L} = \frac{1.1 \cdot 110 / \sqrt{3}}{4.85 + 4.8} = 7.24 \text{ kA}$$

Time constant of the short-circuit current:

$$T_N = \frac{(X_s + X_L) / \omega}{R_s + R_L} = \frac{(4.85 + 4.8) / 314}{0.26 + 0.91} = 26 \text{ ms}$$

$$K_{TF2}' = 1 + \omega \cdot T_N \cdot \left(1 - e^{-\frac{T_s}{T_N}} \right) = 7.0 \text{ and } ALF' = 7.0 \cdot \frac{7240}{600} = 84$$

The CT has to be designed for condition 2).

CT dimensioning for distance protection Calculation example (3)

Resistance of connecting leads CT to relay:

$$R_L = 2 \cdot \frac{\rho \cdot l}{Q} = \frac{0.0179 \cdot 80}{2.5} = 1.15 \Omega$$

Burden of relay 7SA511: $R_R = 0.1 \Omega$

Total burden: $R_B = 1.25 \Omega$

for the accuracy limit factor, we get:

$$ALF \geq \frac{6+1.25}{6+30} \cdot 84 = 16.9 \quad \text{Chosen: } n=20$$

Condition 3): Close-in fault with ARC

1st short-circuit duration (protection + breaker time: T_{F1} = 35+60 = 95 ms

Herewith and with $T_N = 60$ ms:

$$K_{TF3}' = 1 + \omega \cdot T_N \cdot \left(1 - e^{-\frac{T_{F1}}{T_N}} \right) + a = 16 + 3 = 119$$

$$ALF_3' = K_{TF3}' \cdot \frac{I_{F_max_line_beginning}}{I_N} = 19 \cdot \frac{14400}{600} = 456$$

Condition 4): Fault at balance point with ARC

With $T_{F1} = 95$ ms, $T_N = 26$ ms und $T_M = 35$ ms:

$$K_{TF4}' = 9 + 7 = 16$$

$$K_{TF4}' = \left[1 + \omega \cdot T_N \cdot (1 - e^{-\frac{T_{F1}}{T_N}}) \right] + \left[1 + \omega \cdot T_N \cdot (1 - e^{-\frac{T_M}{T_N}}) \right] = 9 + 7 = 16$$

$$ALF_4' \geq K_{TF4}' \cdot \frac{I_{F_max_line_end}}{I_N} = 16 \cdot \frac{7240}{600} = 193$$

Design for the case with ARC to condition 3), close in fault:

$$ALF \geq \frac{6+1.25}{6+30} \cdot 456 = 92$$

Here, a larger CT would have to be taken, e.g. 60 VA (15 VA internal burden) with a doubled ratio, e.g. 1200/1 A.

The accuracy limit factor would then be: $n > 49$ (50)

CT dimensioning for distance protection

Calculation example (4)

Design of TPY type CTs for the ARC C-O-C-O cycle

$$K_{TF-ARC} = \left[1 + \frac{\omega \cdot T_N \cdot T_S}{T_N - T_S} (e^{\frac{t_{F1}}{T_N} - e^{\frac{t_{F1}}{T_S}}}) \cdot e^{-\frac{t_{DT} + t_{F1}}{T_S}} + \left[1 + \frac{\omega \cdot T_N \cdot T_S}{T_N - T_S} (e^{\frac{t_M}{T_N} - e^{\frac{t_M}{T_S}}}) \right] \right]$$

It is sufficient when the short-circuit current is transmitted till the end of the relay measuring time T_M .

Given:

TPY type CT with $T_S = 0.5$ s

Dead time: $T_{DT} = 0.4$ s

Solution:

Condition 1): Close-in fault with ARC

With $T_N = 60$ ms, $T_{F1} = 95$ ms and $T_M = 35$ ms:

$$K_{TF1}' = [14.3] \cdot 0.42 + [9] = 15$$

$$ALF_1' = 5 \cdot \frac{14400}{600} = 360$$

Condition 2): Fault at balance point with ARC

With $T_N = 26$ ms, $T_{F1} = 95$ ms and $T_M = 35$ ms:

$$K_{TF2}' = [7.9] \cdot 0.42 + [6.8] = 10$$

$$ALF_2' = 10 \cdot \frac{7240}{600} = 121$$

The CT has to be designed for the close-in fault:

$$ALF \geq \frac{6 + 1.25}{6 + 30} \cdot 360 = 73 \quad (\text{chosen } 80)$$

Comparison with closed iron core CT, i.e. $T_S = 5.0$ instead of 0.5 s leads to the following result:

$$K_{TF1}' = [16] \cdot 1 + [9] = 25. \quad (40\% \text{ smaller core cross section})$$

CT dimensioning for distance protection

Calculation example (5)

Design of TPZ type CTs (linear CTs)

As a rule, the CT is dimensioned so that the maximum short-circuit current with d.c. offset can be transmitted saturation free:

$$K_{TF}^{**} = 1 + \omega \cdot T_s \cdot \left(\frac{T_N}{T_s} \right) \frac{T_s}{T_s - T_N}$$

Example:

The CT shall be designed to IEC 60044-6 with a phase displacement of $\delta=3^\circ$ at rated burden.

$$T_s = \frac{10900}{\delta_{[\min]}} = 61 \text{ ms}$$

The short-circuit time constant is: $T_N=60 \text{ ms}$.
Herewith we get: $K^{**}=7$.

It results a very low over-dimensioning factor, which is also valid for the non-successful ARC, as the CT is completely demagnetised during the dead time.
In comparison, the following reductions in core cross section can be achieved:
–by (1– 7/25), i.e. **72%** compared to the **TPX type CT**,
–by (1– 7/15), i.e. **53%** compared to the **TPY type CT**.
However, the higher core fixing cost have to be considered.

Distance Protection Setting

General objectives of distance zone grading:

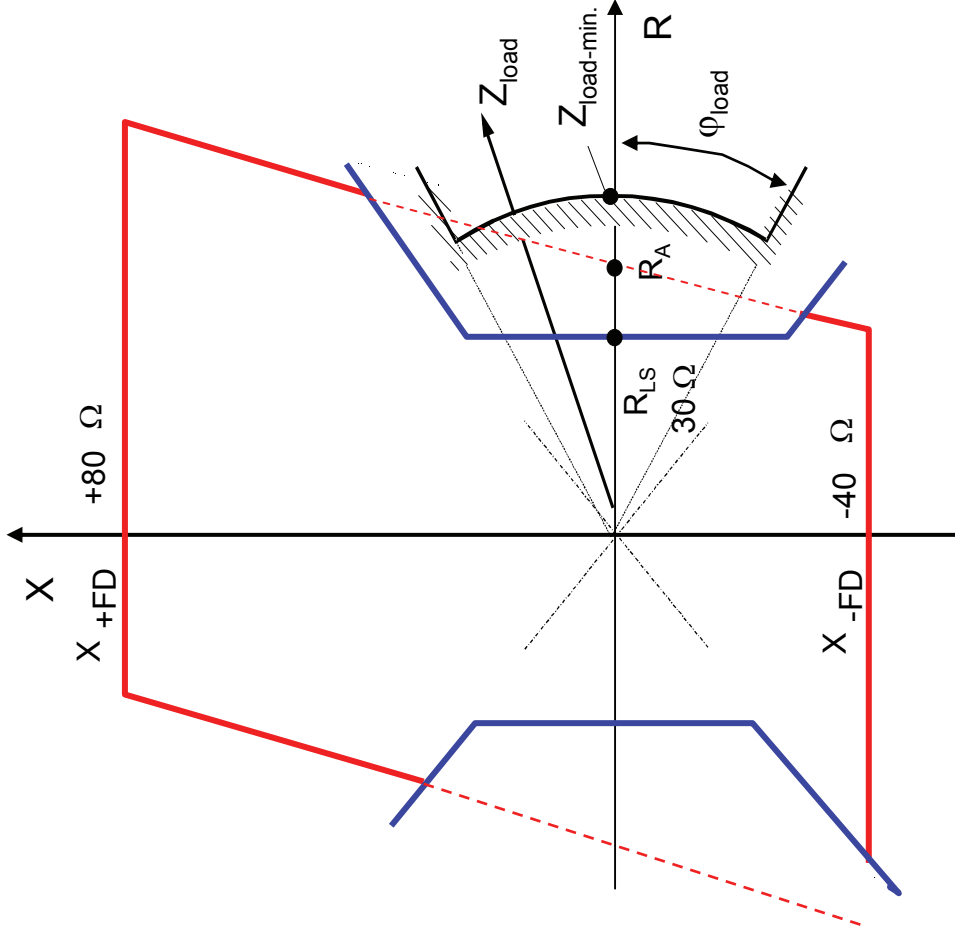
1st Zone: 85 to 90% of the protected line

Overreach zone : About 120% of the protected line (150% in case of parallel lines)

2. Zone: At least 15 - 20% over the following busbar (Busbar back-up protection), up to about 50% of the shortest following line

3. Zone: ♦ 10 to 20% over the longest following line considering intermediate infeeds
♦ R-reach must allow maximum emergency line loading according to NERC recommendations

Setting of impedance type fault detectors



$$Z_{\text{load}} = \frac{U_{N \text{ Ph-Ph}}}{I_{\text{load}} \cdot \sqrt{3}} = \frac{U_{N \text{ Ph-Ph}}^2}{P_{\text{app}}}$$

$$R_{\text{load}} = Z_{\text{load}} \cdot \cos \varphi_{\text{load}} = Z_{\text{load}} \cdot \frac{P_{\text{act}}}{P_{\text{app}}} = \frac{U_{N \text{ Ph-Ph}}^2 \cdot P_{\text{act}}}{P_{\text{act}}^2 + P_{\text{react}}^2}$$

$$X_{\text{load}} = Z_{\text{load}} \cdot \sin \varphi_{\text{load}} = Z_{\text{load}} \cdot \frac{P_{\text{react}}}{P_{\text{app}}} = \frac{U_{N \text{ Ph-Ph}}^2 \cdot P_{\text{react}}}{P_{\text{act}}^2 + P_{\text{react}}^2}$$

$$P_N = U_N \cdot I_N \cdot \sqrt{3}$$

Example :

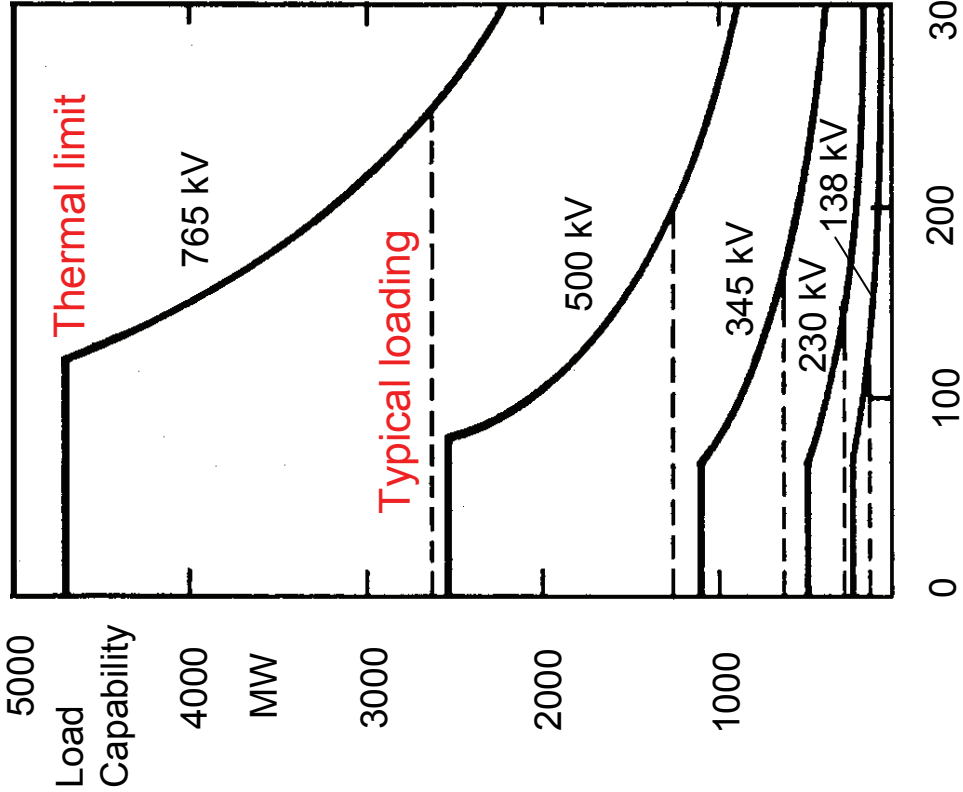
$U_N = 230 \text{ kV}$ and CT -ratio $1200/1$

$P_N = 230 \text{ kV} \cdot 1200 \text{ A} \cdot \sqrt{3} = 478 \text{ MVA}$

During this load, the relay measures a secondary load impedance of:

$$Z_{N(\text{Sec.})} = \frac{U_{N(\text{Sec.})} / \sqrt{3}}{I_{N(\text{Sec.})}} = \frac{100 \text{ V} / \sqrt{3}}{1 \text{ A}} = 57,7 \, \Omega$$

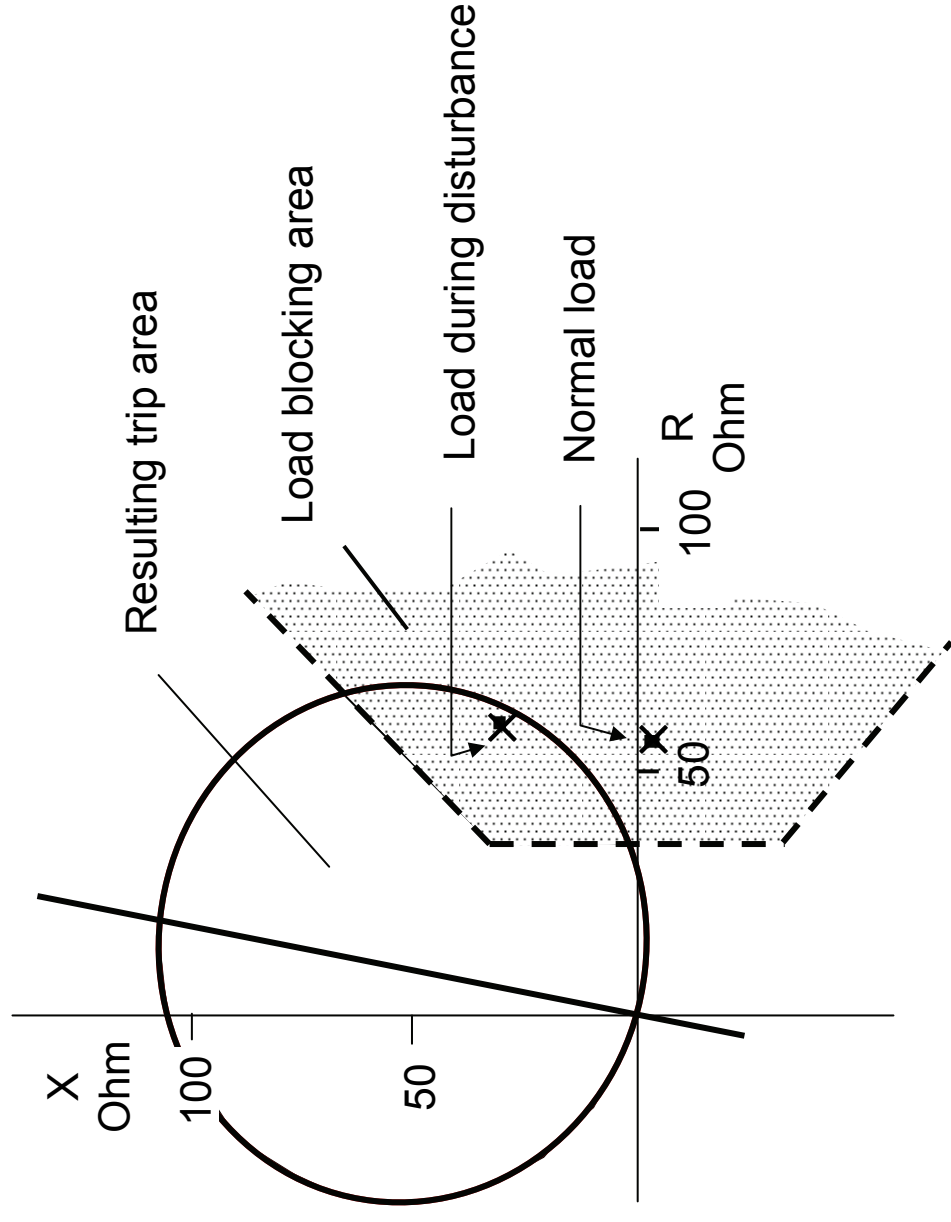
Line loading



Typical Line Capabilities (about natural load):

Voltage	Load		Impedance
	Capability		
138 kV	100 MW		190 Ohm
230 kV	250 MW		212 Ohm
345 kV	600 MW		198 Ohm
500 kV	1200 MW		208 Ohm
765 kV	2500 MW		234 Ohm

August 14, 2003 Northwest USA and Canada blackout Third zone tripping due to overload and undervoltage



August 14, 2003 Blackout

NERC Actions to prevent cascading blackouts (February 10, 2004)

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NERC (North American Electric Reliability Council):

Recommendation 8a:

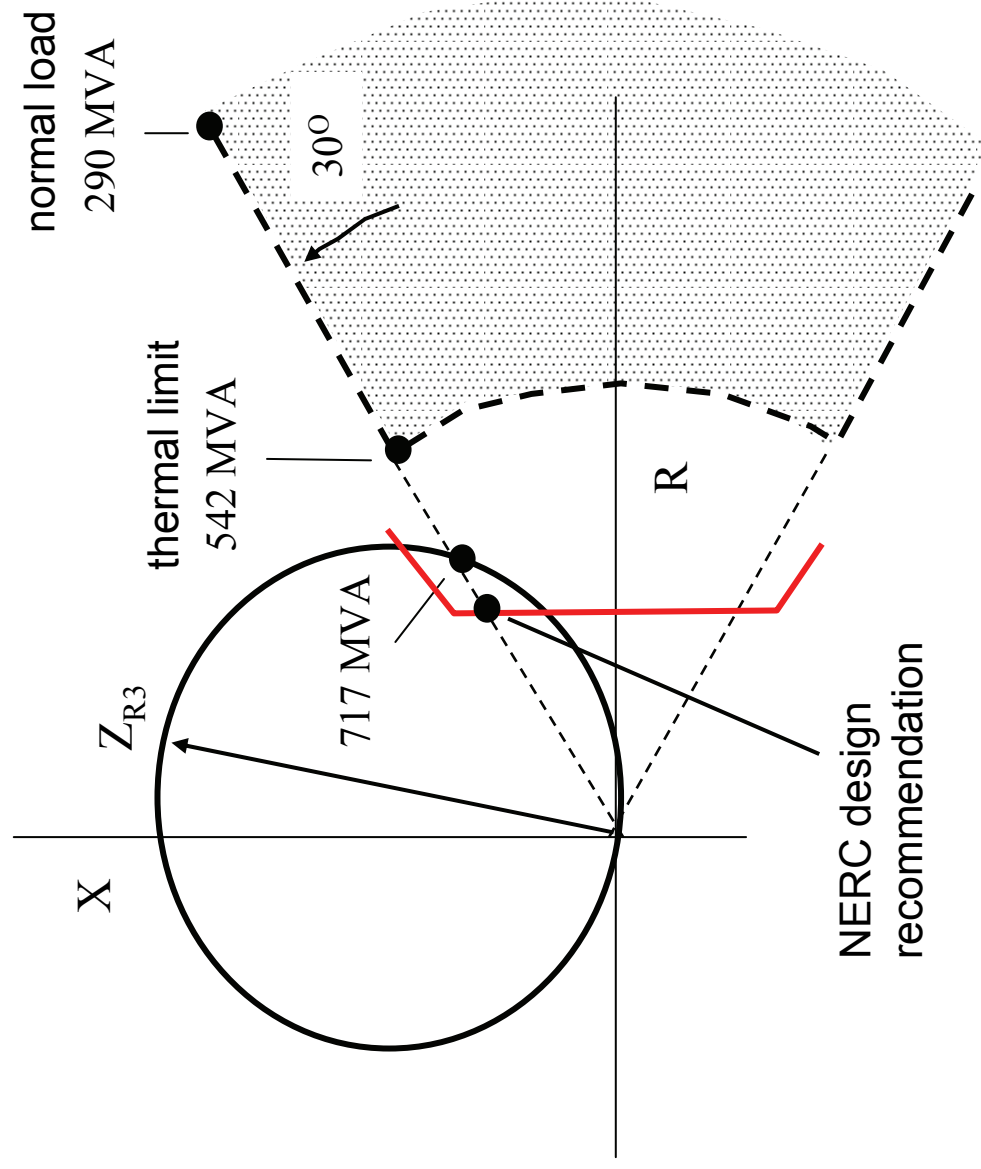
Evaluate zone 3 settings for the purpose of verifying that zone 3 relay is not set to trip on load under extreme emergency conditions. **)*

)* Zone 3 relay should not operate at or below **150% of the emergency ampere rating of a line, assuming **0.85** per unit voltage and a line phase angle of **30 degrees**

Set zone 3 relay to allow 20 min overloading (System operators need 20 min to shed load once a problem has been recognized.

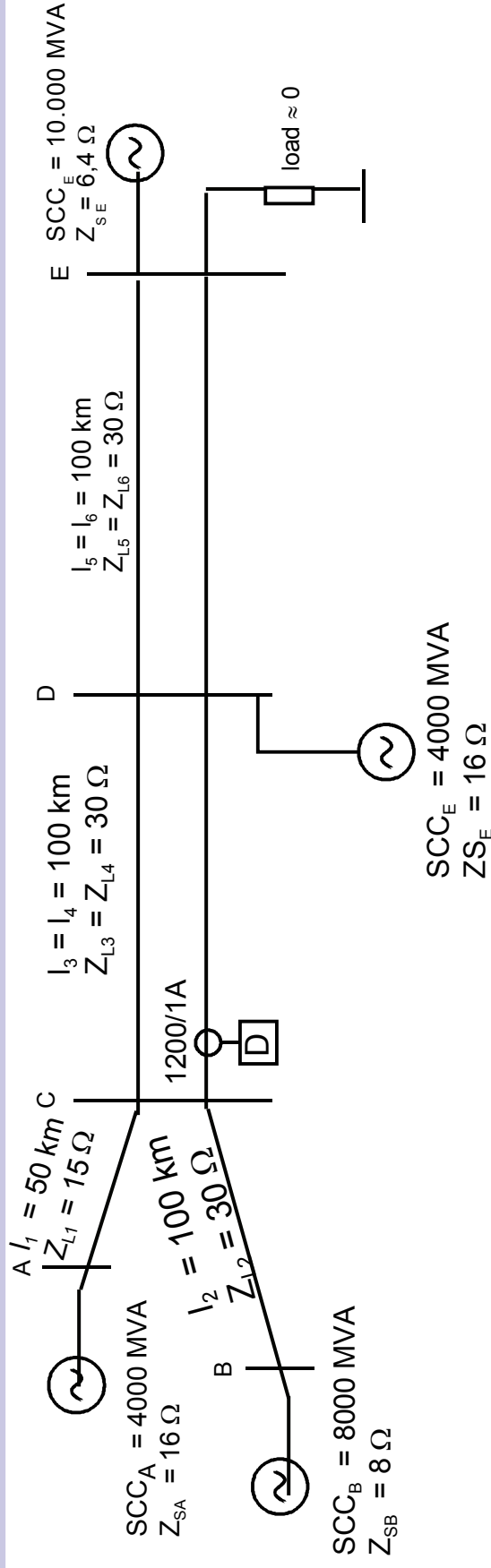
- Distance relays should **not** be used to provide overload protection
- Relay should be set to ride through all recoverable swings

Setting of load encroachment section



Setting of impedance fault detector

Example (1)



For each 400 kV single line from C to D,
the natural load is $P_{Nat} = 460 \text{ MW}$

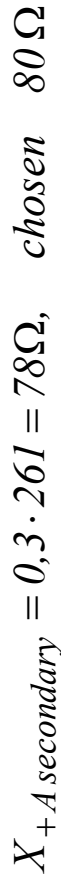
$$I_{load} = \frac{P_{Nat}}{\sqrt{3} \cdot U_N} = \frac{460 \text{ MW}}{\sqrt{3} \cdot 400 \text{ kV}} = 664 \text{ A}$$

$$Z_{load} = \frac{400.000 \text{ V} / \sqrt{3}}{664 \text{ A}} = 348 \text{ } \Omega$$

$$Z - ratio = \frac{CT - ratio}{VT - ratio} = \frac{1200/1}{400/0.1} = 0.3$$

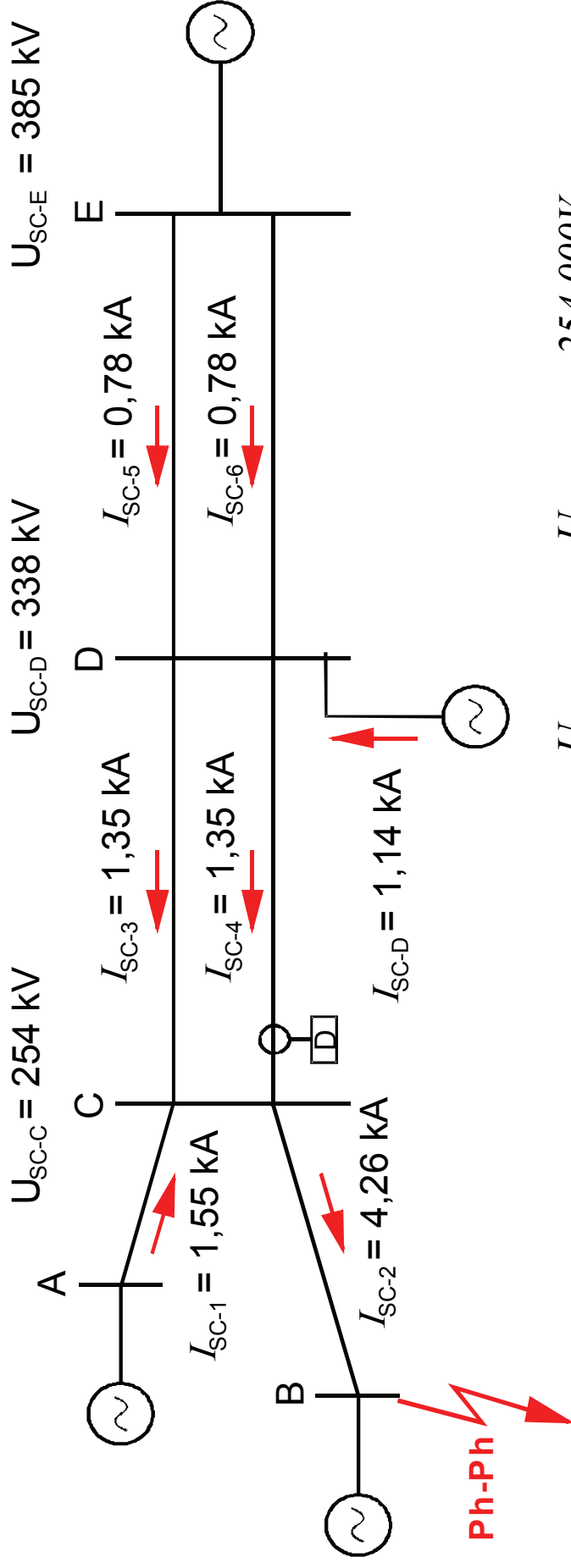
$$R_{FD \text{ secondary}} = 0.3 \cdot \frac{348}{2} = 36.5 \text{ } \Omega$$

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Setting of impedance fault detector Example (3)

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$$Z_{Ph-Ph} = \frac{U_{Ph-Ph}}{I_{Ph1} - I_{Ph2}} = \frac{U_{Ph-Ph}}{2 \cdot I_{Ph}} = \frac{254.000V}{2 \cdot 1350A} = -94\Omega$$

$$X_{-A \text{ secondary}} = 1,3 \cdot (-94) = -122 \Omega$$

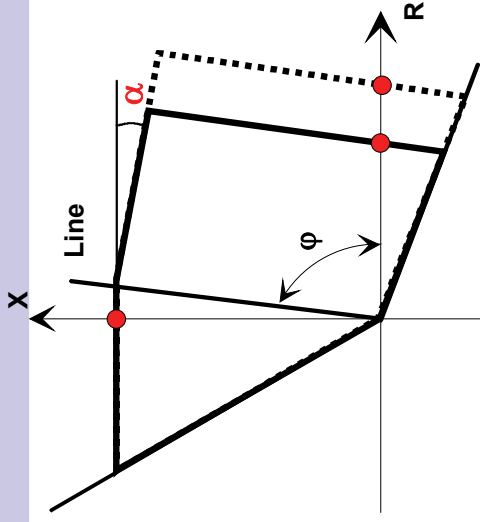
$$X_{+A \text{ secondary}} = 0,3 \cdot (-122) = -36,6 \Omega, \text{ chosen } -40\Omega$$

R-setting of distance zones (arc compensation)

Voltage level:	Average distance of ph-conductors	Arc resistance at $I_{SC}=1000\text{ A}$ at $I_{SC}=10.000\text{ A}$
380 kV	11 m	27,5 Ω 2,75 Ω
220 kV	7 m	17,5 Ω 1,75 Ω
110 kV	3,5 m	7,5 Ω 0,75 Ω
20 kV	<1 m	<2,5 Ω <0,25 Ω

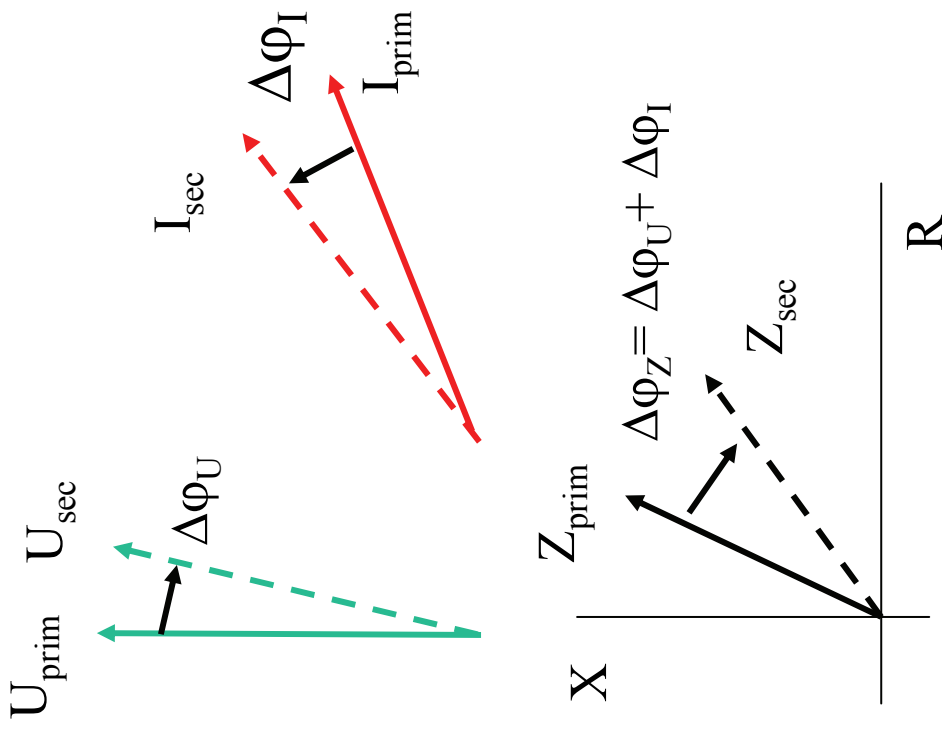
Protected cable/line	R/X-ratio of zone setting
Short cables (ca. 0.5 to 3 km)	3 to 5
Longer cables > 3km	2 to 3
Short overhead lines < 10 km	2 to 5
Overhead lines < 100 km	1 to 2
Long overhead lines 100 to 200 km	0.5 bis1
Long EHV lines >200 km	≤ 0.5

Influence of CT and VT errors on zone reach setting



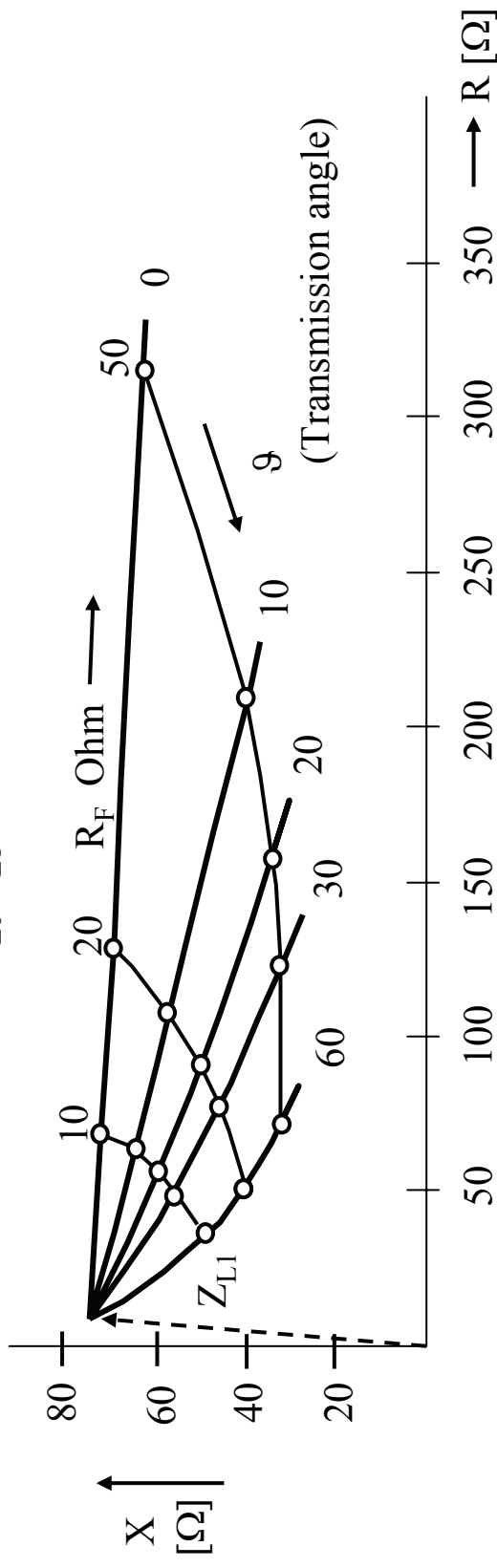
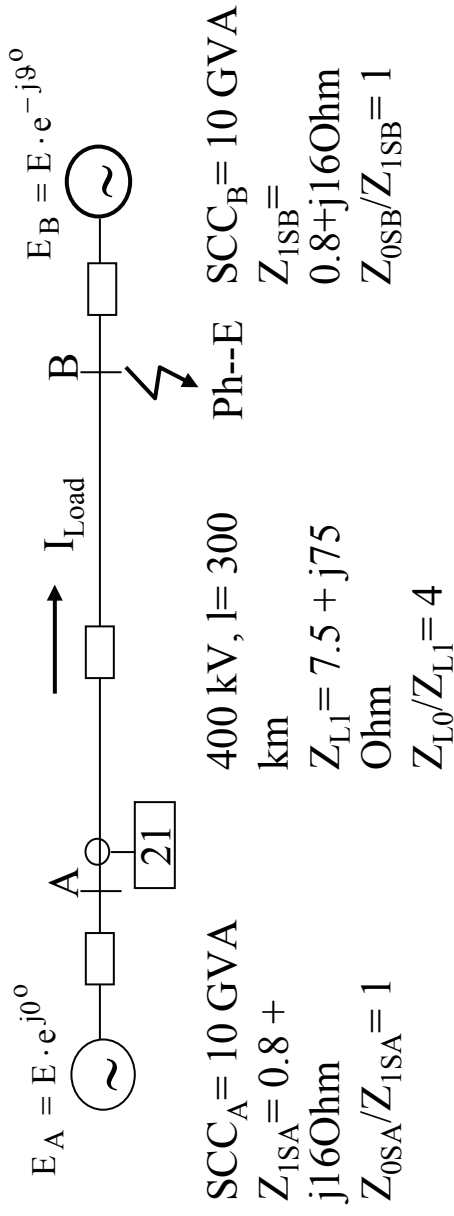
If setting $R/X > 1$:

- Reduce zone from 90 % to $STF \leq [1 - (R/X) \cdot \tan(\delta_U + \delta_I)] \cdot 93,5\%$ (e.g. with $R/X=3$ setting to 84% if $\Delta\phi_U=1^\circ$ and $\Delta\phi_I=1^\circ$)
- or setting of α to $-(\delta_U + \delta_I)$ (possible with 7SA522 and 7SA6)

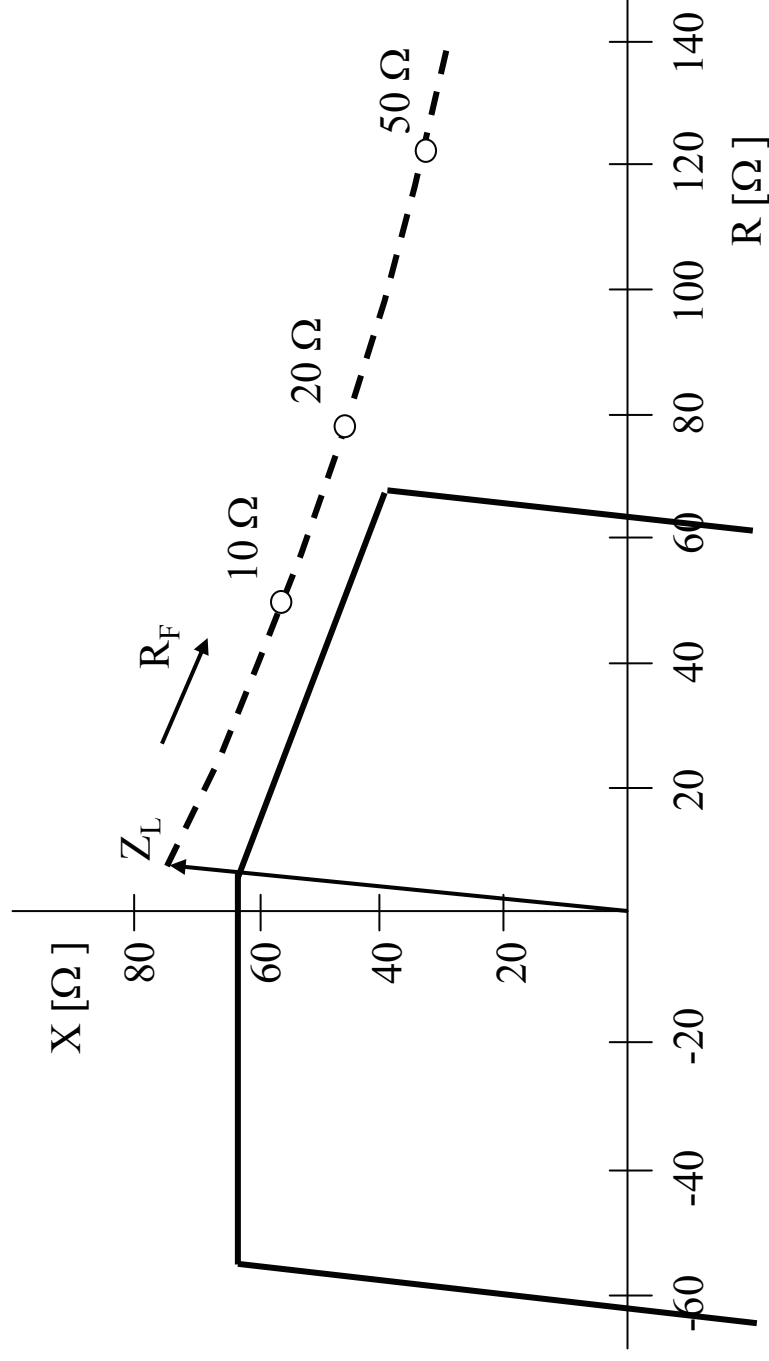


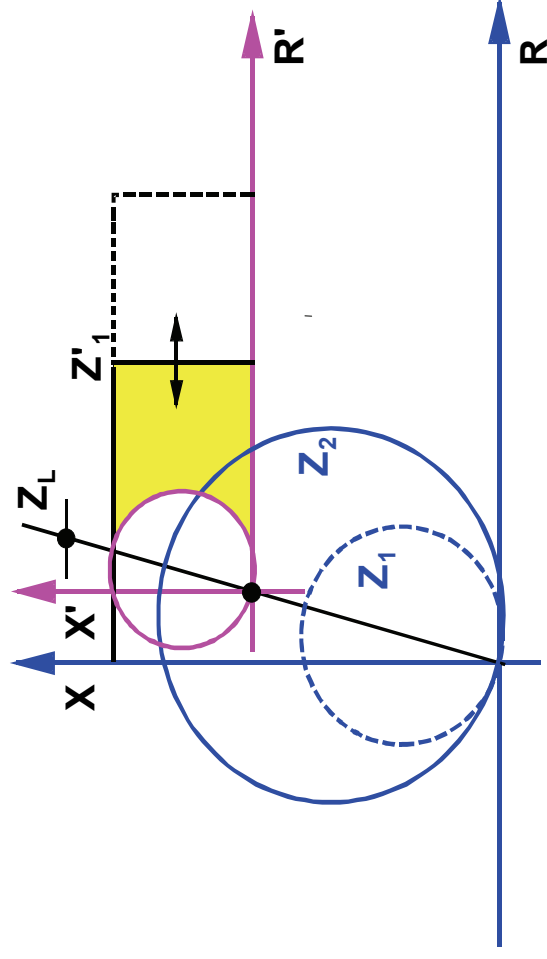
Resistive faults:

Impact of line loading on distance measurement



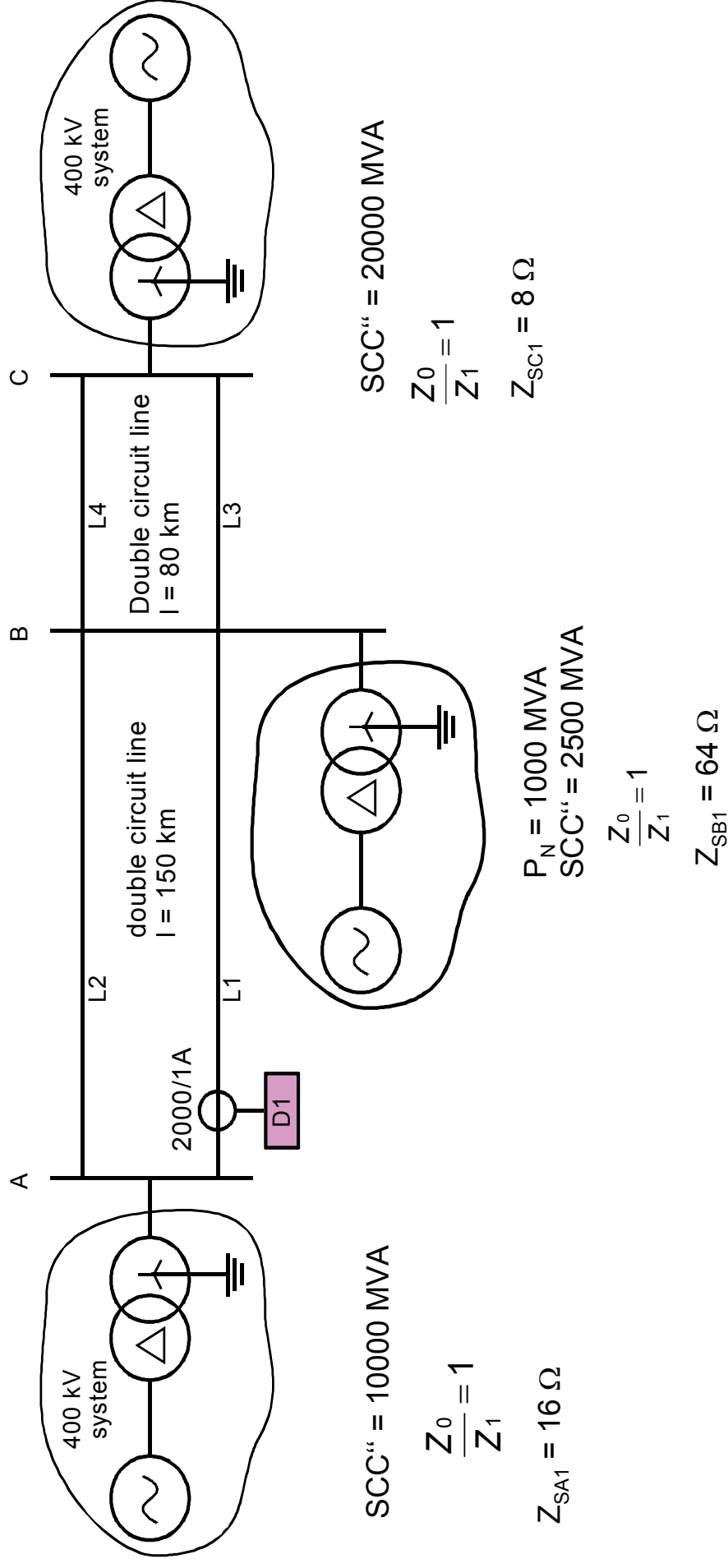
Tilting of 1st zone top line to avoid overreach in case of resistive faults with line loading (load exporting end)



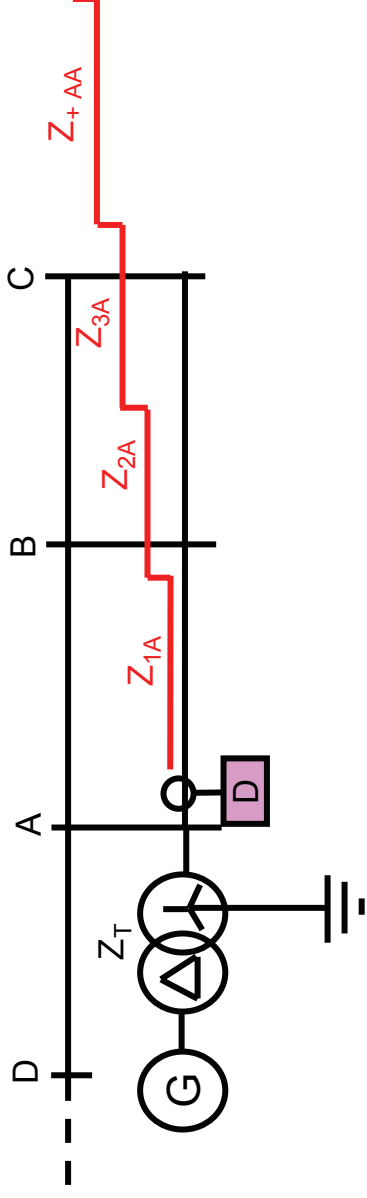


Difference of quadrilateral and MHO-circle in the 1st zone

Distance zone setting for a double-circuit line: System data for the calculation example



Distance zone setting for a double-circuit line: Classical setting of back-up zones



$$Z_{2A} = GF_2 \cdot (Z_{A-B} + 0.5 \cdot Z_{B-C})$$

$$Z_{3A} \geq 1.1 \cdot (Z_{A-B} + Z_{B-C})$$

$$Z_{+FD} \geq 1.1 \cdot (Z_{A-B} + 2 \cdot Z_{B-C})$$

$$Z_{-FD} \geq 1.1 \cdot Z_{A-D} \text{ or } 0.5 \cdot Z_T$$

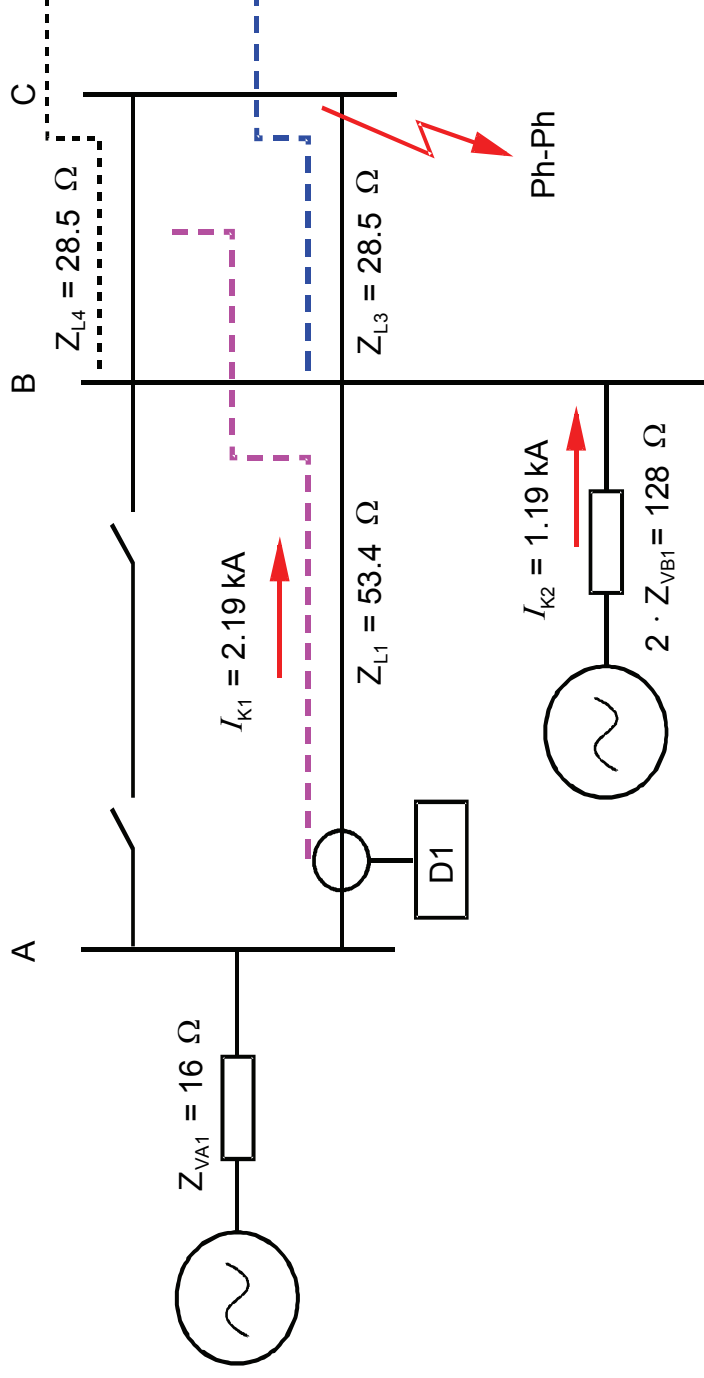
As a rule, high zone reach should be achieved even with intermediate infeed

Reach setting must consider load flow including a 20 - 30 % safety margin .

Double circuit line

Setting of the back-up zones

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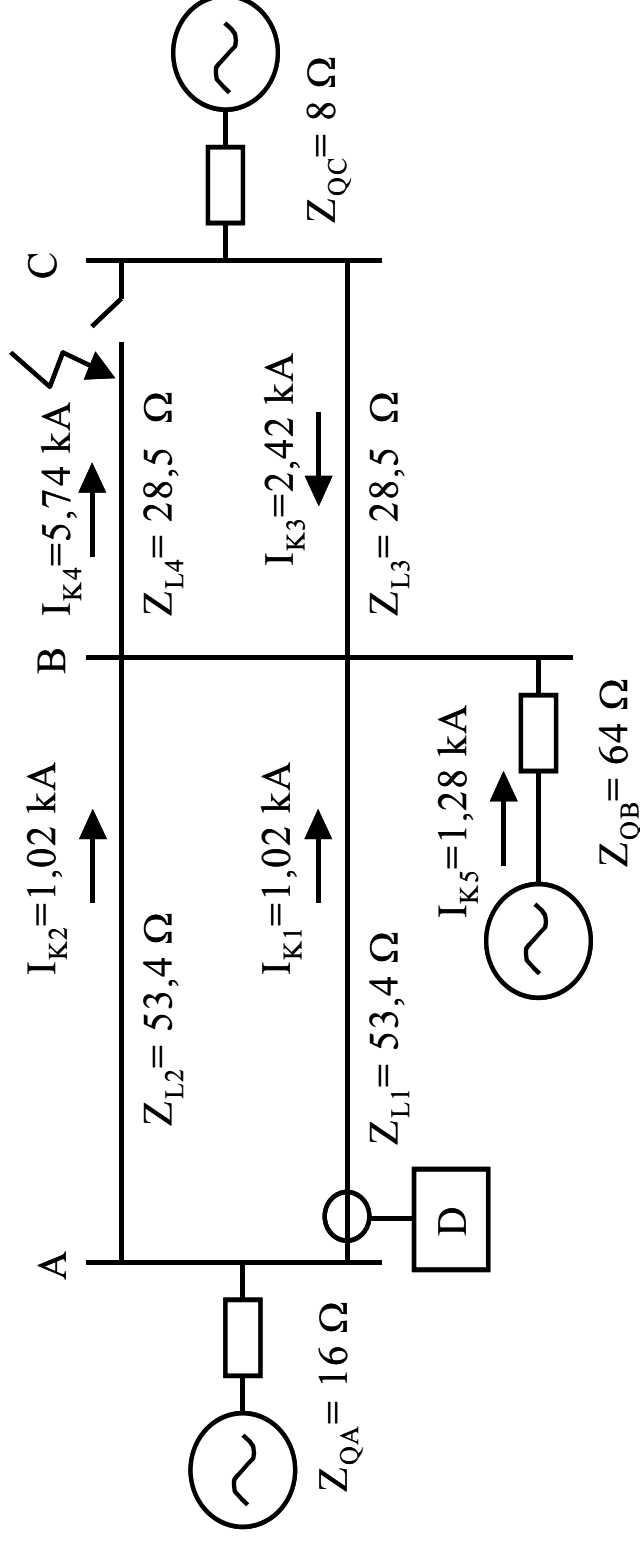
$$X_2 = \left[53.4 + \frac{28.5}{2} \cdot \left(1 + \frac{1.19}{2.19} \right) \right] \cdot 0.85 = 64 \Omega = 120\% X_{L1}$$

$$X_3 = (53.4 + 28.5) \cdot 1.1 = 90.1 = 169\% X_{L1}$$

Double circuit line

Setting of the fault detection zone

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$$X_{+A} = \left[53,4 + 28,5 \cdot \frac{5,74}{1,02} \right] \cdot 1,1 = 214 \Omega = 400\% X_{L1}$$

$$X_{-A} = X_{+A}$$

Double circuit line

Set zone characteristics

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$$Z_{Load-max.} = \frac{U_N^2}{P_{Nat.}} = \frac{400^2}{518} = 309 \Omega$$

$$R_{A1} = 0,8 \cdot \frac{309}{2} \cdot \cos 30^\circ = 107 \Omega$$

Expected fault resistances:

$$I_{SC-min.} = 1000 \text{ A}$$

Insulator Length: 4 m

Arc resistance:

$$2500 \text{ kV/m} \times 4 \text{ m} / 1 \text{ kA} = 10 \Omega$$

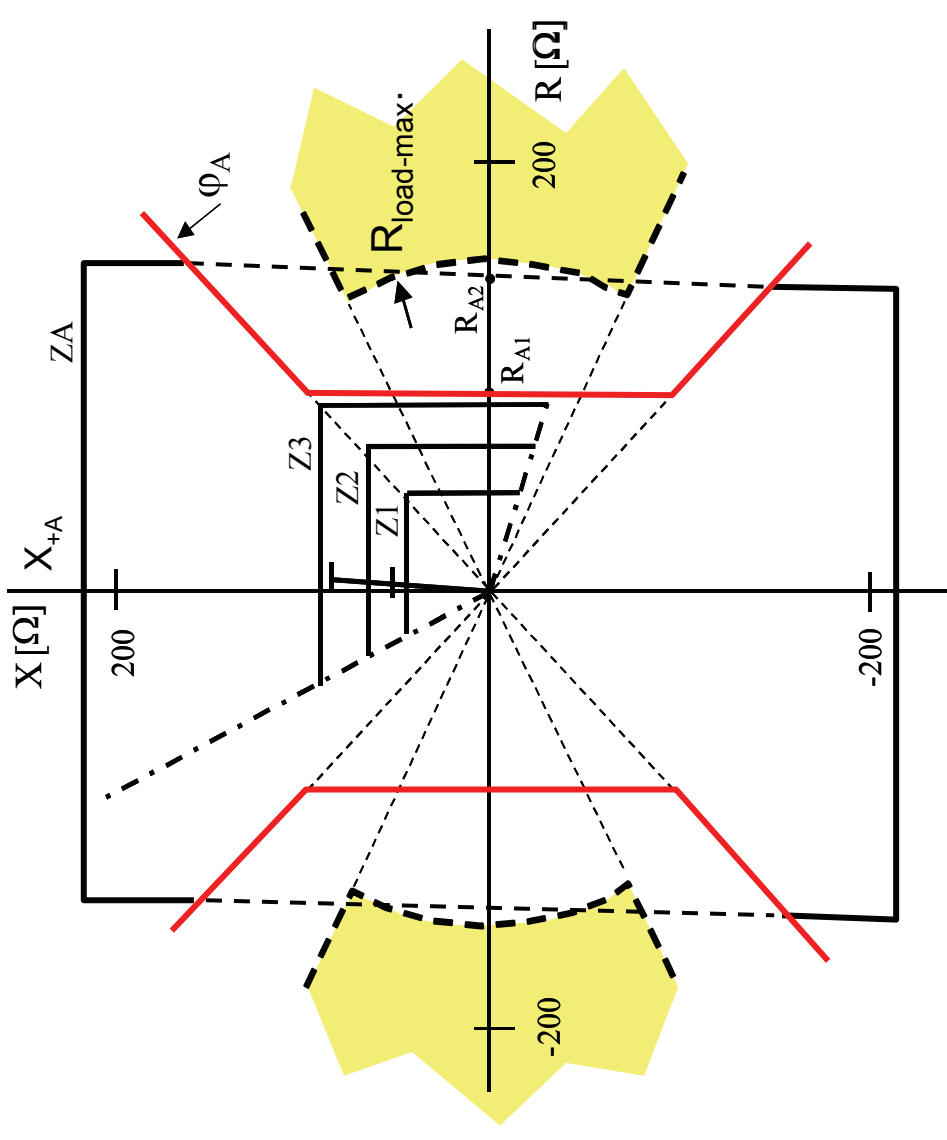
Tower footing resistance: $R_{TF} = 5 \text{ Ohm}$

$$I_{remote}/I_{local} = 5$$

$$\text{Apparent } R_{TF} = (1+5) \times 5 = 30 \text{ Ohm}$$

$$\text{Total Fault resistance } R_{F-tot} = 35 \text{ Ohm}$$

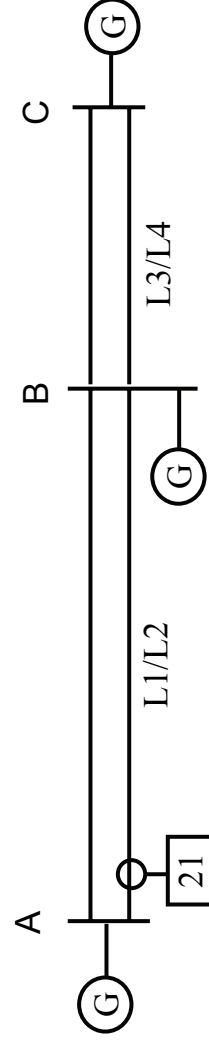
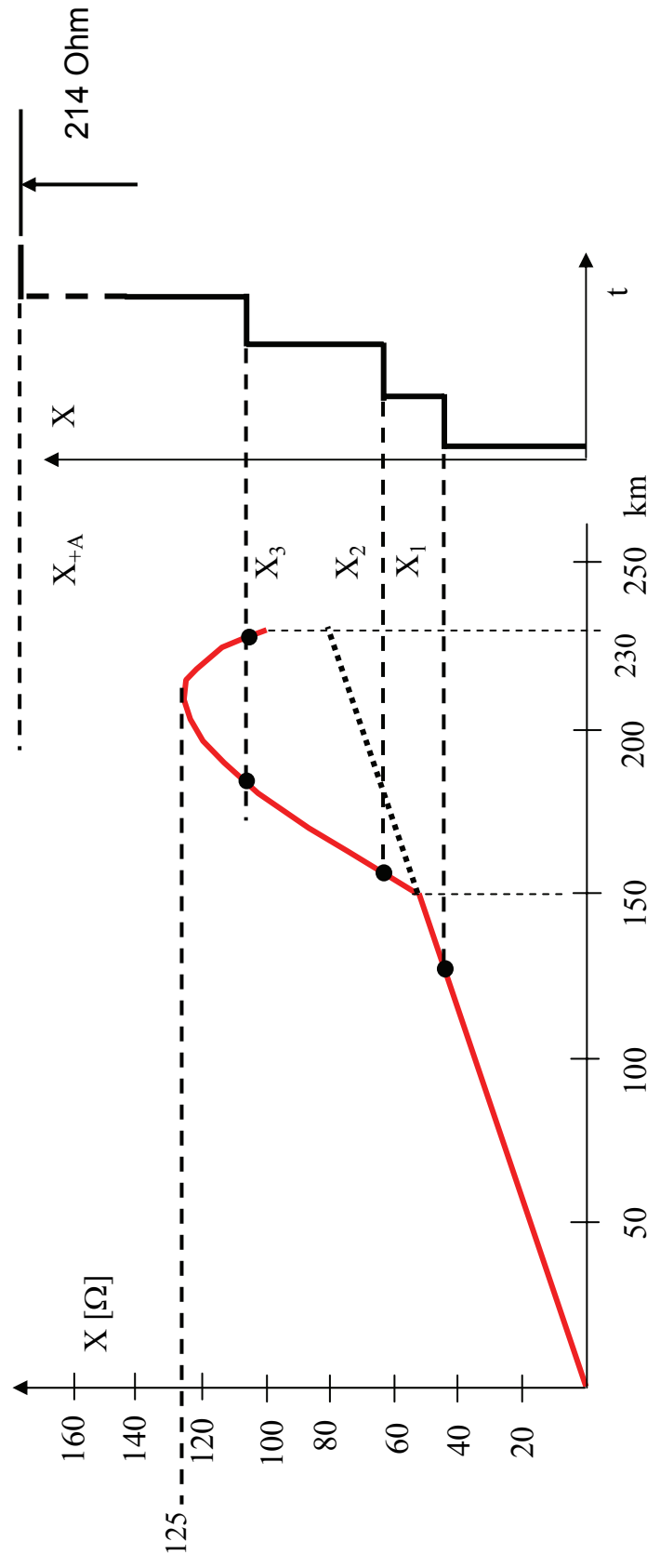
$$\text{Chosen: } R_{A1} = 100 \Omega$$



Double circuit line: Setting of the back-up zones

Reach check considering all infeeds

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Double circuit line, Distance measurement with earth faults: Reach dependent on setting of $k_{XER} = \left(\frac{X_E}{X_L} \right)_{\text{relay}}$

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a) valid for $\frac{x}{l} \leq 1$.
 If $\frac{x}{l} > 1$,

$$GF_1(1 + k_{XER}) + k_{XEM} \cdot \frac{X'_{0M}}{X'_{0L}}$$
 then : $\frac{1 + k_{XEL}}$

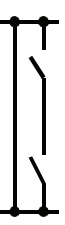
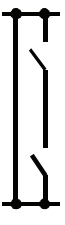
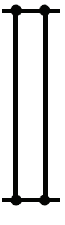
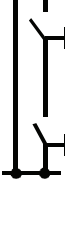
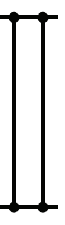
$X'_{0M} = 0.72 \text{ } \Omega/\text{km}$
 $X'_{0L} = 1.11 \text{ } \Omega/\text{km}$
 $X'_{1L} = 0.356 \text{ } \Omega/\text{km}$

$k_{XEL} = \left(\frac{X'_{EL}}{X'_{1L}} \right)_{\text{line}}$

$k_{XEL} = 0.71$

$k_{XEM} = \left(\frac{X'_{0M}}{3 \cdot X'_{0L}} \right)_{\text{line}}$

$k_{XEM} = 0.64$

Relay settings	Reach x/l in case of Ph-E faults		
$GF_1 = 0.85$ $k_{XER} =$  $k_{XER} = \frac{1 + k_{XEL} \cdot \frac{x}{l} \cdot -1}{GF_1} = 0.71 \text{ (0.5)}$	 $\frac{x}{l} = GF_1 \cdot \frac{1 + k_{XER}}{1 + k_{XEL}}$	 $\frac{x}{l} = \text{see Equ. (205)}$	 $\frac{x}{l} = \frac{(1 + k_{XER}) \cdot GF_1}{1 + k_{XEL} - k_{XEM} \cdot \frac{X'_{0M}}{X'_{0L}}}$
$k_{XER} =$  $k_{XER} = \frac{1 + k_{XEL} \cdot \frac{x}{l} \cdot -1}{GF_1} = 1.18$	85% (75%)	71% (64%)	108% (98%)
$k_{XER} =$  $k_{XER} = \frac{1 + k_{XEL} + k_{XEM} \cdot \frac{x}{l}}{GF_1} = 1.18$	108%	85%	132%
$k_{XER} =$  $k_{XER} = \frac{1 + k_{XEL} + k_{XEM} \cdot \frac{X'_{0M}}{X'_{0L}} \cdot \frac{x}{l} \cdot -1}{GF_1} = 0.31$	65%	56%	85%

Double circuit line, Distance measurement with earth faults Reach in case of single side infeed

$$\underline{U}_{Ph-E} = \frac{x}{l} \underline{Z}_L \cdot \underline{I}_{Ph} + \frac{x}{l} \underline{Z}_E \cdot \underline{I}_E + \frac{x}{l} \frac{\underline{Z}_{0M}}{3} \cdot \underline{I}_{EP}$$

With single side infeed:

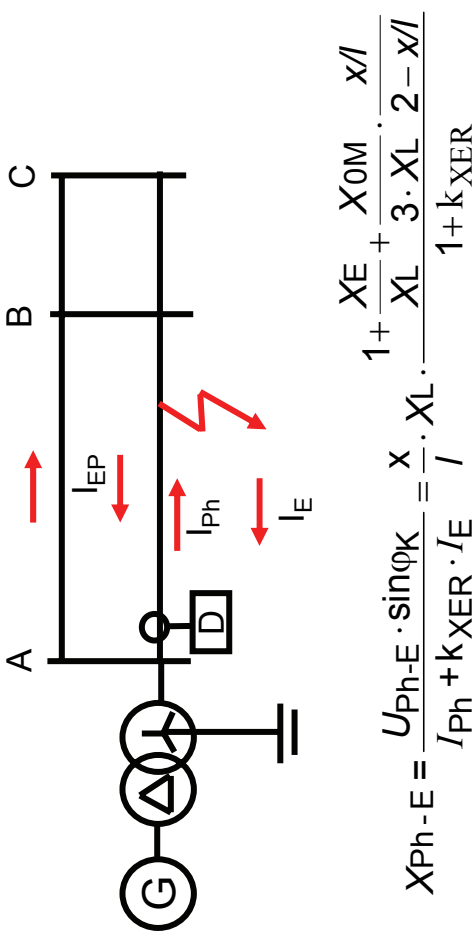
$$\underline{I}_{Ph} = \underline{I}_E \quad \text{and} \quad \underline{I}_{EP} = \frac{x/l}{2 - x/l} \cdot \underline{I}_E$$

$$\underline{Z}_{Ph-E} = \frac{\underline{U}_{Ph-E}}{\underline{I}_{Ph} + \underline{k}_{XER} \cdot \underline{I}_E} = \frac{x}{l} \cdot \frac{\underline{Z}_L + \underline{Z}_E + \frac{\underline{Z}_{0M}}{3} \cdot \frac{x/l}{2 - x/l}}{1 + \underline{k}_{XER}}$$

With : $\underline{X}_{Ph-E} = \underline{X}_{Ph-Ph} = \underline{X}_1 = \underline{SF}_1 \cdot \underline{X}_L$, and $\underline{k}_{XEL} = \frac{\underline{X}_E}{\underline{X}_L}$ und $\underline{k}_{XEM} = \frac{\underline{X}_{0M}}{3 \cdot \underline{X}_L}$:

$$\underline{k}_{XER} = \frac{1 + \underline{k}_{XEL} + \underline{k}_{XEM} \cdot \frac{x/l}{2 - x/l} \cdot \frac{x}{l}}{\underline{SF}_1} - 1$$

$$x/l = \frac{[\underline{SF}_1 \cdot (1 + \underline{k}_{XER}) + 2(1 + \underline{k}_{XEL})] - \sqrt{[.]^2 - 8(1 + \underline{k}_{XEL} - \underline{k}_{XEM}) \cdot (1 + \underline{k}_{XER})} \cdot \underline{SF}_1}{2 \cdot (1 + \underline{k}_{XEL} - \underline{k}_{XEM})}$$



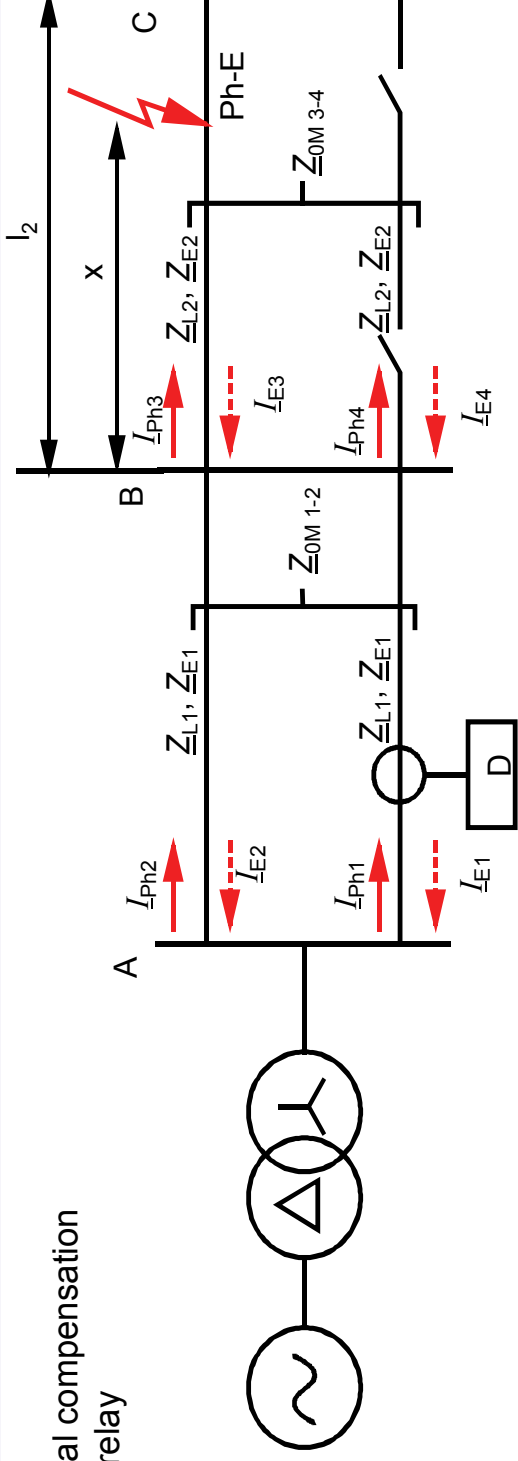
$$\underline{X}_{Ph-E} = \frac{\underline{U}_{Ph-E} \cdot \sin \varphi_K}{\underline{I}_{Ph} + \underline{k}_{XER} \cdot \underline{I}_E} = \frac{x}{l} \cdot \underline{X}_L \cdot \frac{1 + \frac{\underline{X}_E}{\underline{X}_L} + \frac{\underline{X}_{0M}}{3 \cdot \underline{X}_L} \cdot \frac{x/l}{2 - x/l}}{1 + \underline{k}_{XER}}$$

Double circuit line:

Zone reach with earth fault on following line (single side infeed)

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k_{XER} is the residual compensation factor, set at the relay



$$\underline{U}_{Ph-E} = \underline{Z}_{L1} \cdot \underline{I}_{Ph1} + \underline{Z}_{E1} \cdot \underline{I}_{E1} + \frac{\underline{Z}_{OM1-2}}{3} \cdot \underline{I}_{E2} + \frac{x}{l_2} \underline{Z}_{L2} \cdot \underline{I}_{Ph3} + \frac{x}{l_2} \underline{Z}_{E2} \cdot \underline{I}_{E3}$$

with : $k_{XEL1} = \frac{\underline{X}_{E1}}{\underline{X}_{L1}}$, $k_{XEM1-2} = \frac{\underline{X}_{OM1-2}}{3 \cdot \underline{X}_{L1}}$ and $k_{XEL3} = \frac{\underline{X}_{E2}}{\underline{X}_{L2}}$ and $\underline{I}_{Ph1} = \underline{I}_{E1} = \underline{I}_{E2} = \underline{I}_k$ und $\underline{I}_{Ph3} = \underline{I}_{E3} = 2 \cdot \underline{I}_F$:

$$\underline{X}_{Ph-E} \text{ (measured)} = \frac{\underline{U}_{Ph-E} \cdot \sin \varphi_K}{\underline{I}_{Ph1} + k_{XER} \cdot \underline{I}_{E1}} = \frac{1 + k_{XEL1} + k_{XEM1-2}}{1 + k_{XER}} \cdot \underline{X}_{L1} + 2 \cdot \frac{x}{l_2} \cdot \frac{1 + k_{XEL3}}{1 + k_{XER}} \cdot \underline{X}_{L2}$$

With $\underline{X}_{Ph-E} \text{ (measured)} = \underline{X}_{\text{Zone}}$ (zone limit):

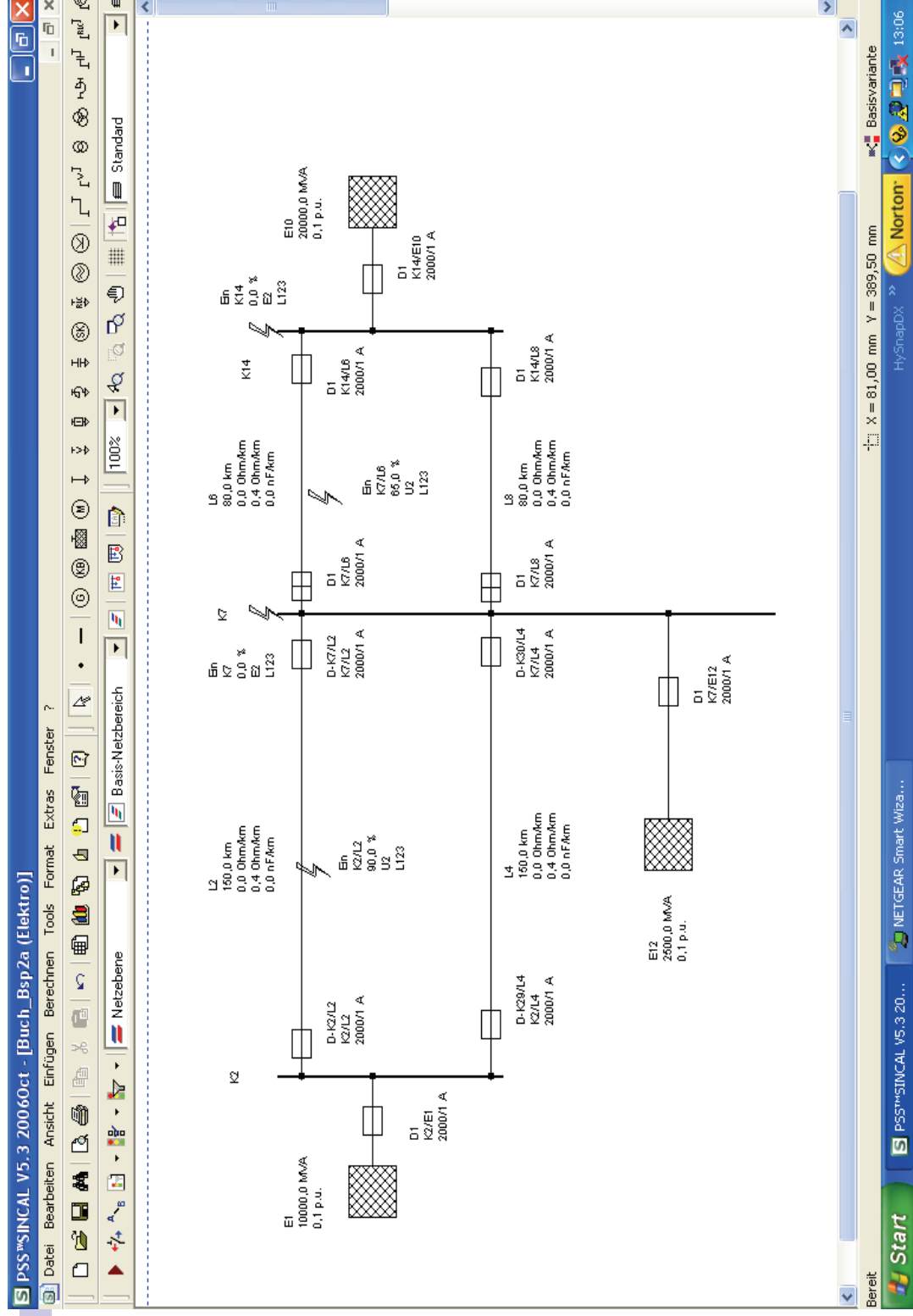
$$\frac{x}{l_2} = \frac{(1 + k_{XER}) \cdot \underline{X}_{\text{Zone}} - (1 + k_{XEL1} + k_{XEM1-2}) \cdot \underline{X}_{L1}}{2 \cdot (1 + k_{XEL2}) \cdot \underline{X}_{L2}}$$

In the example: at $x/l=0$: $\underline{X}_{Ph-E} = \frac{1 + 0.71 + 0.64}{0.71} = 1.37 \cdot \underline{X}_{L1}$

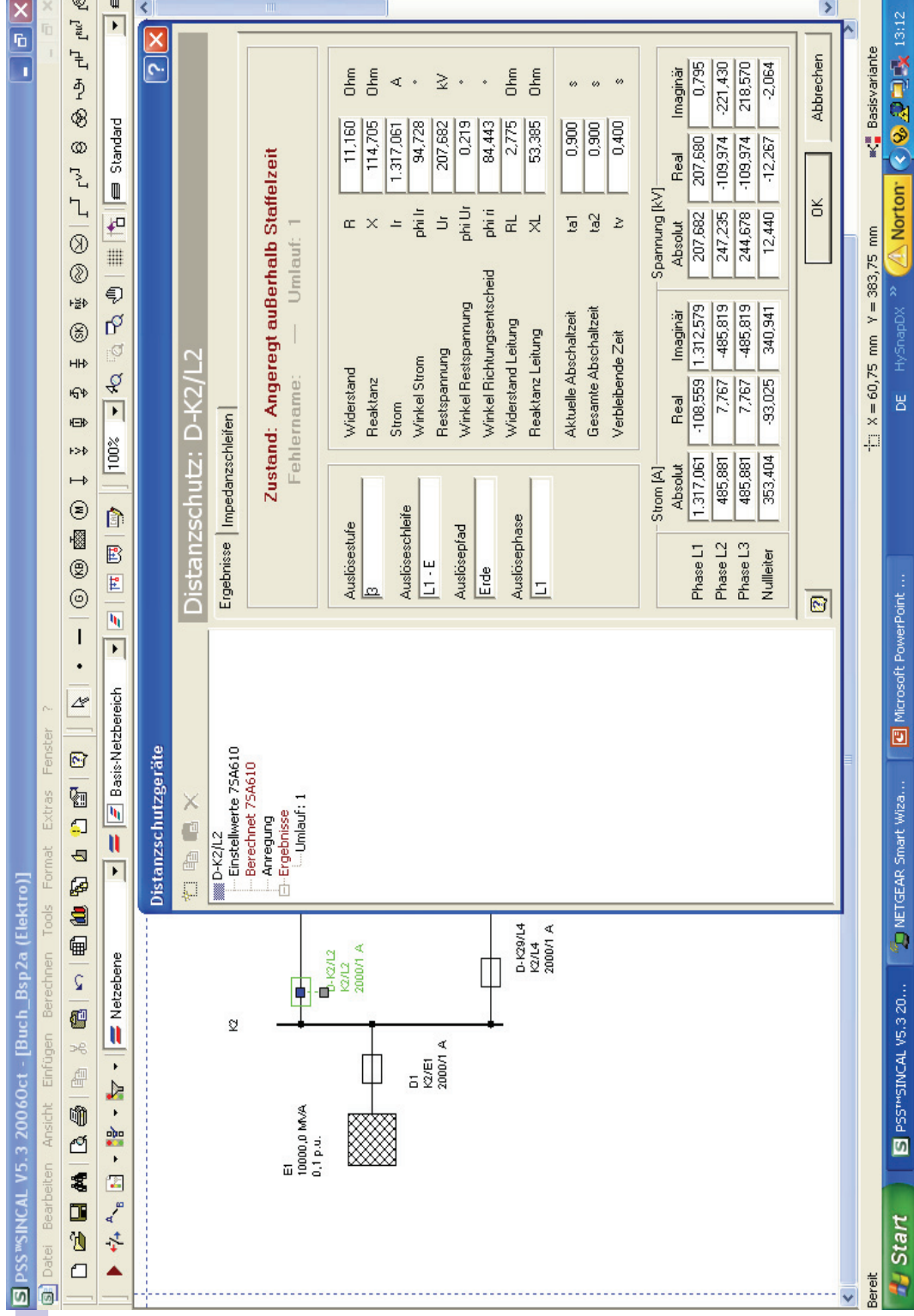
In the example: with $\underline{X}_3 = 169\% \underline{X}_1$: $x/l = 29\%$!

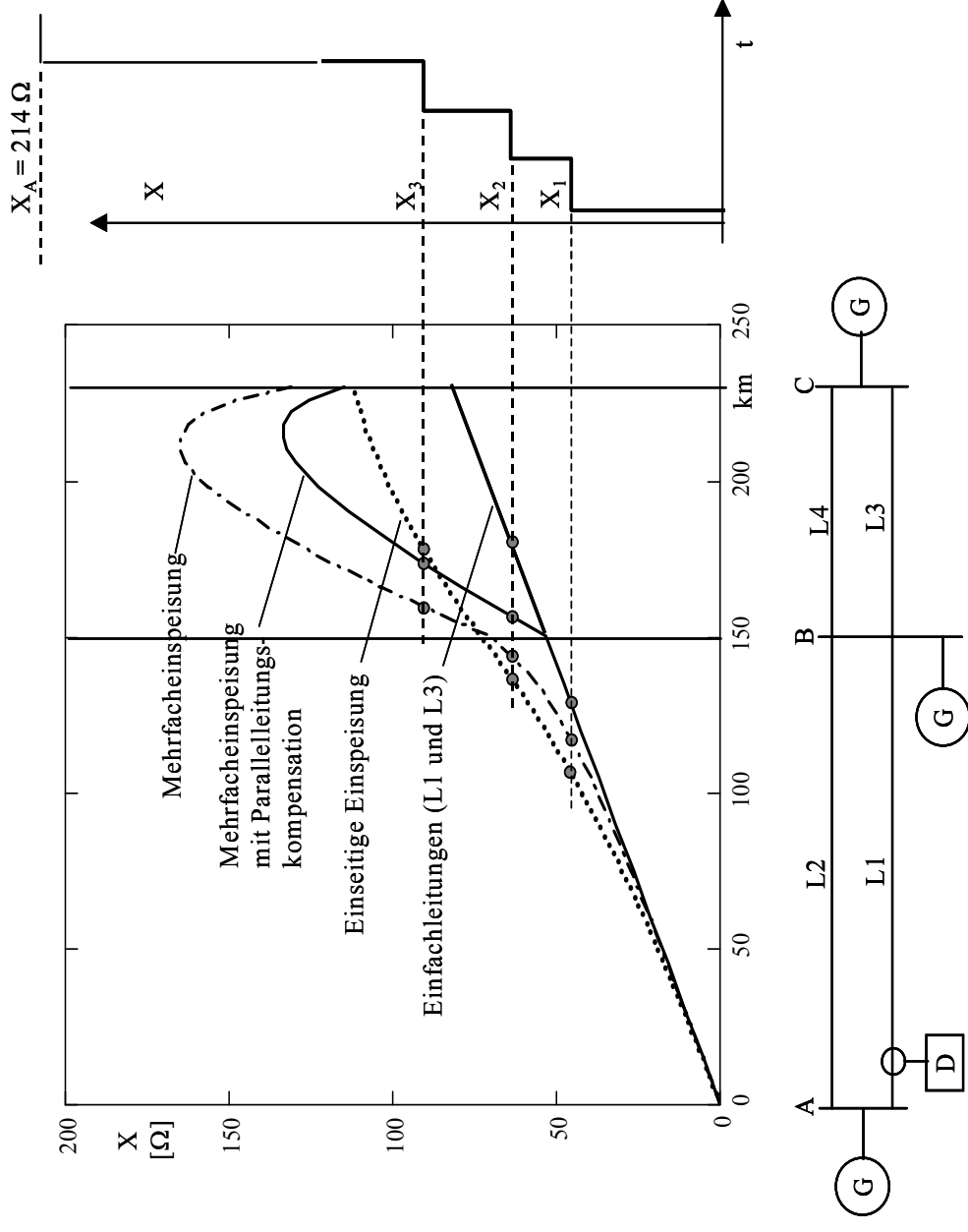
Load-flow and short-circuit calculation based relay coordination (Program SINCAL)

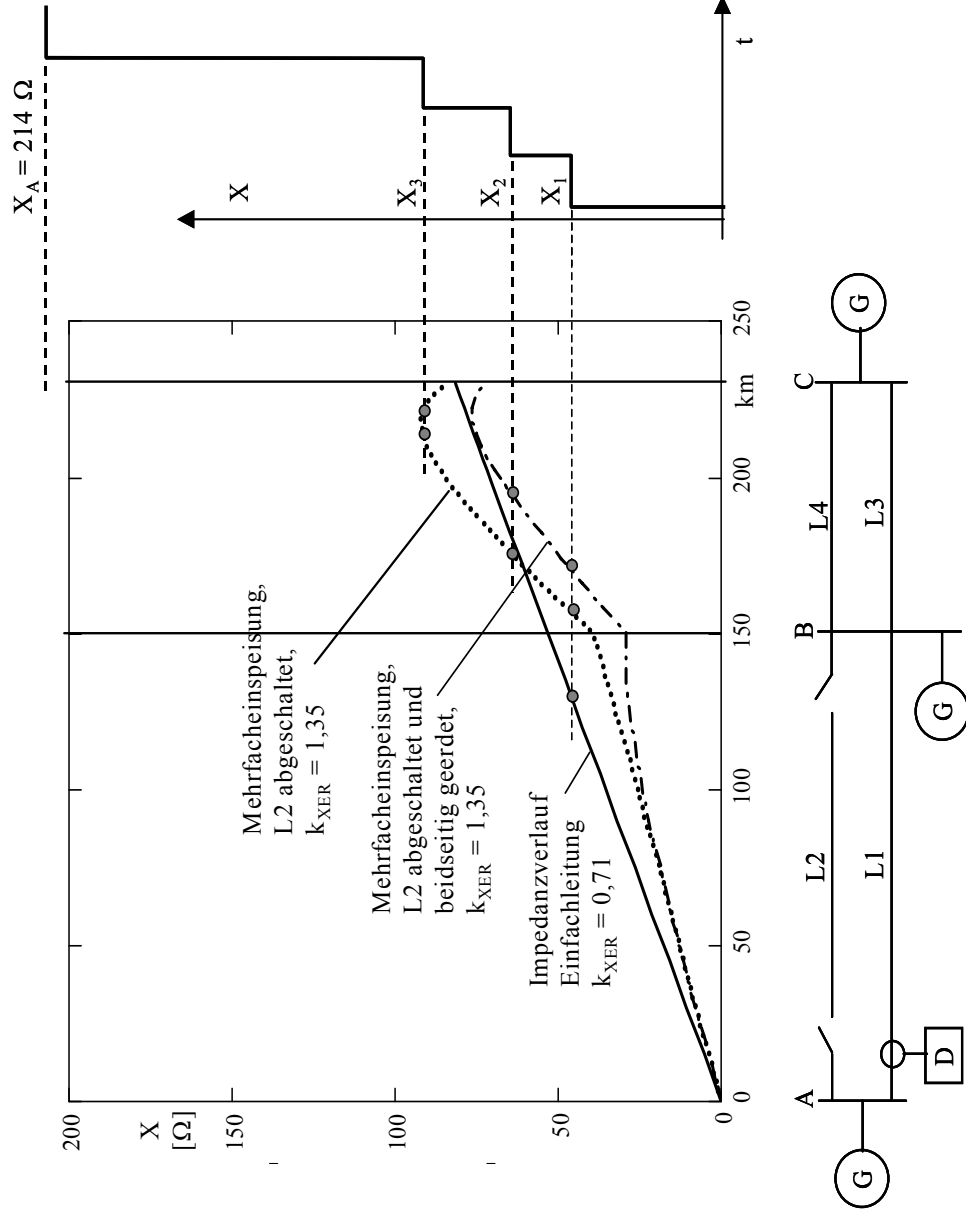
(1)



Load-flow and short-circuit calculation based relay coordination (Program SINCAL) (2)



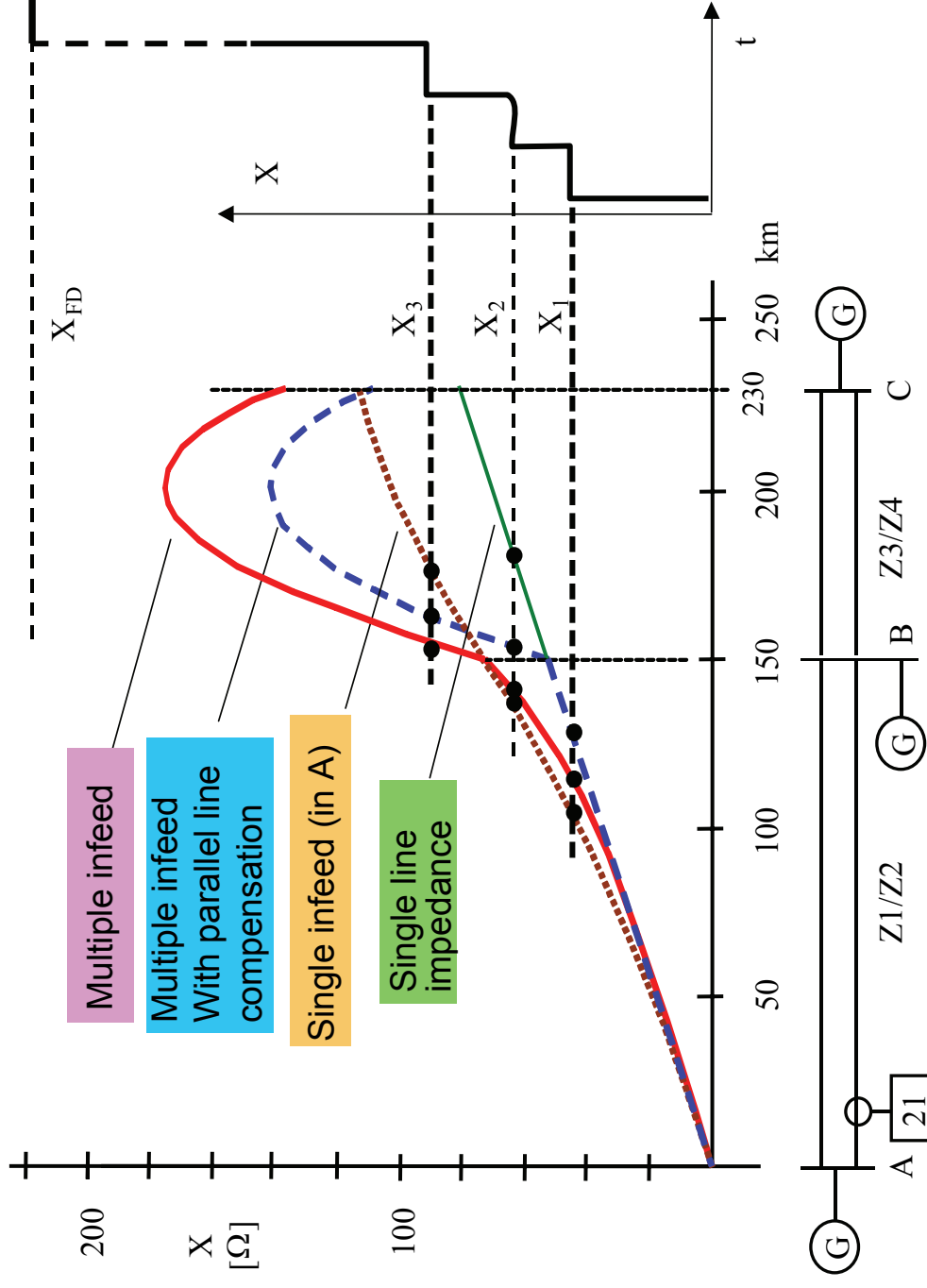




Double circuit line protection:

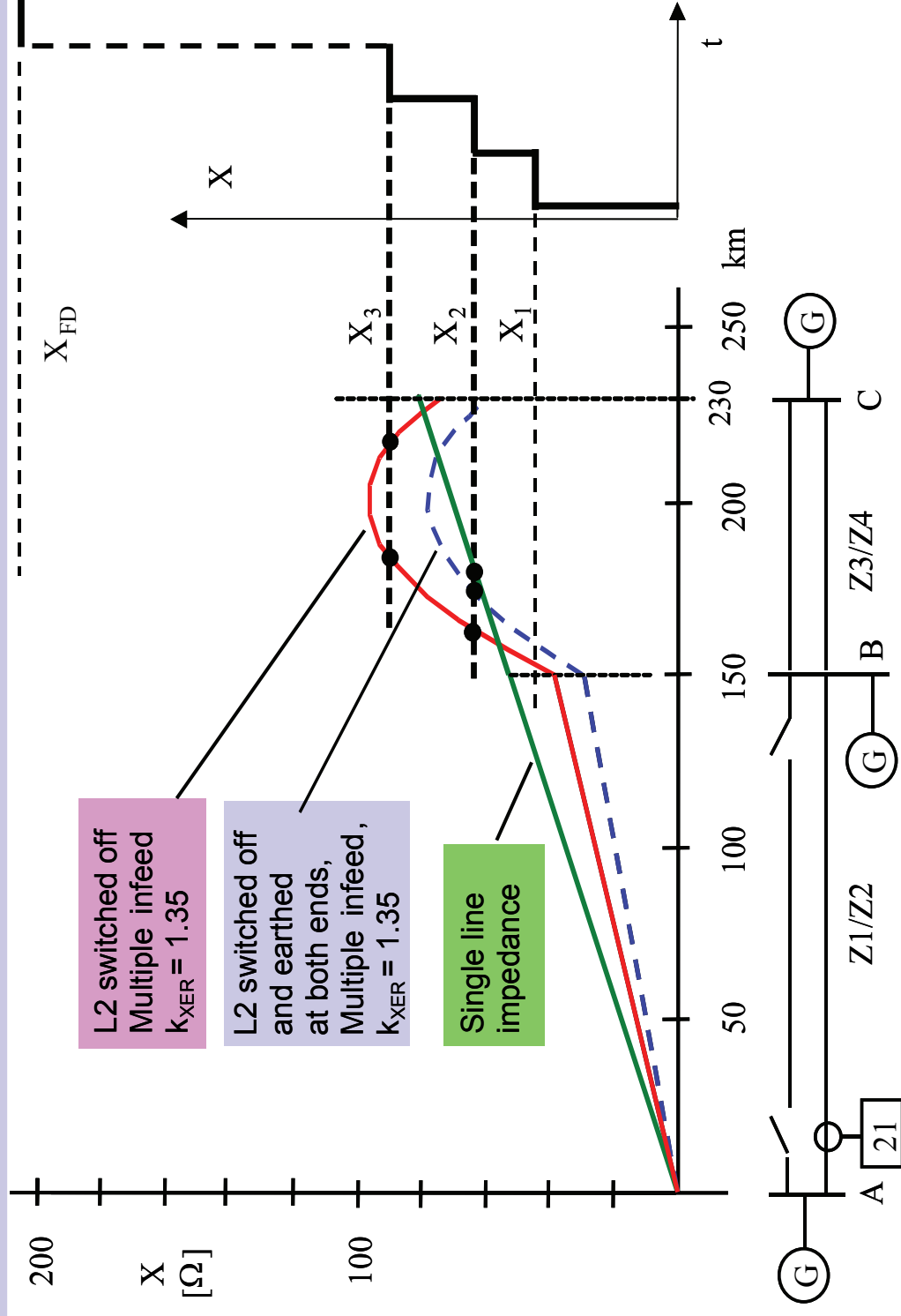
Check of zone reach for earth faults considering all infeeds

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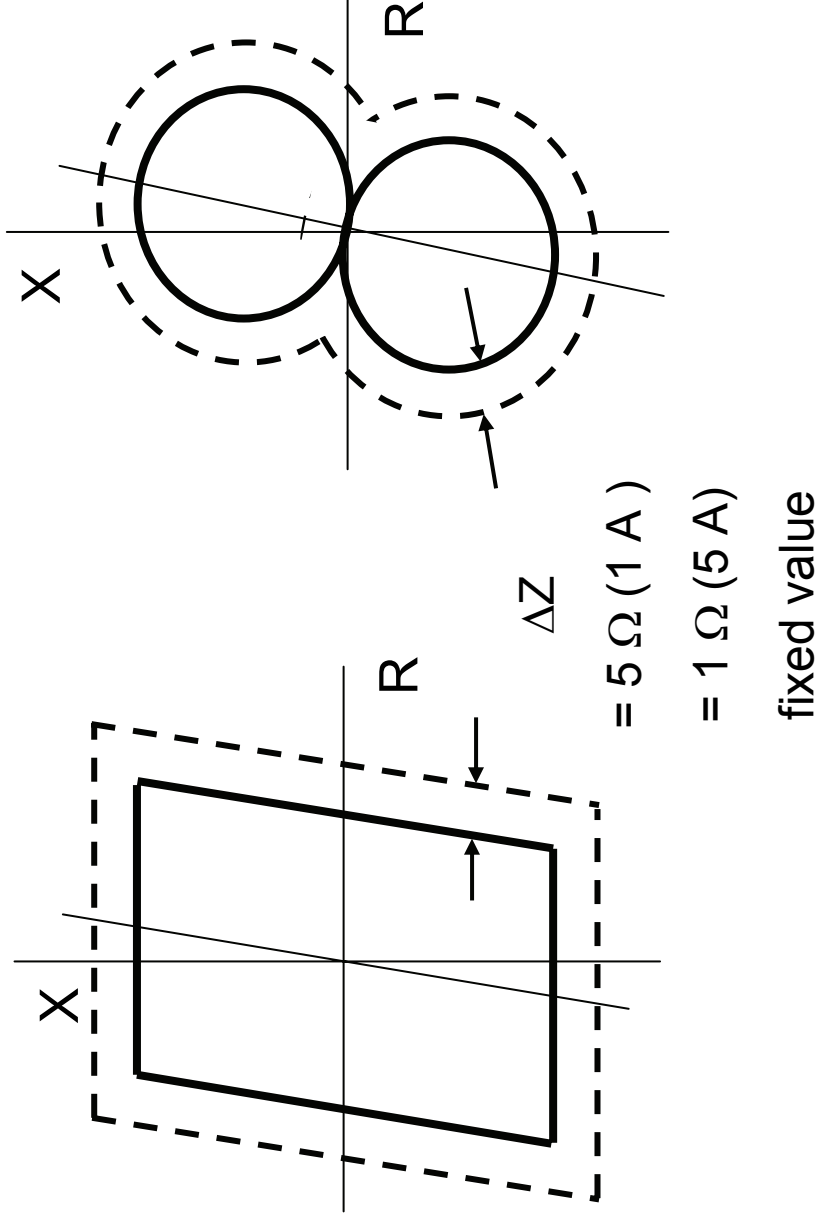


Setting of a separate $k_{XE2} = k_{XE1} + k_{XEM} = 1.35$ instead of $k_{XE1} = 0.71$ would have the same influence on overreaching zones as parallel line compensation.

Check of zone reach for earth faults considering all infeeds Use of the independent k_{XER} -factor for overreaching zones



Setting free power swing blocking function



Auto-reclosing (ARC)

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Fault Statistics

Relative number of different type of faults
on transmission lines:

Fault type	H.V. Percent	E.H.V. (500 kV)
single phase-to-earth	70	93
phase-to-phase	15	4
double phase-to-earth	10	2
Three-phase	5	1
Total	100	100

Autoreclosure Practised Versions

High speed three-pole AR

- typical dead time: 0.3...0.5 s
- synchro-check normally not required

Single-pole AR

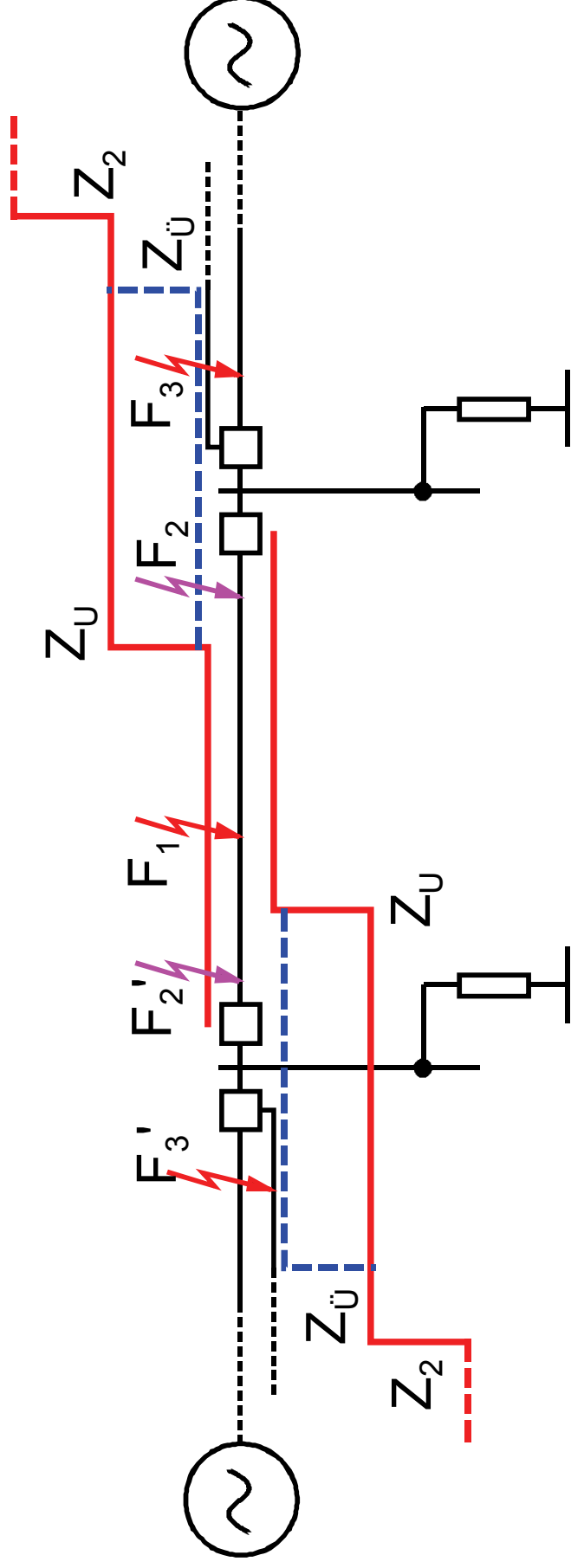
- always high speed
- typical dead time: 0.6...1.2 s
- AR only with single phase-to-earth faults
- some times also with phase-to-phase faults
- C.B.'s must have phase segregated trip mechanisms
- Protection must operate phase selective

Single- and three-pole AR

- single-pole AR with single-phase-to-earth faults
- tree-pole AR with all other faults
- in case of sequential faults during the single-pole dead time: change-over to three-pole AR or definite three-phase tripping

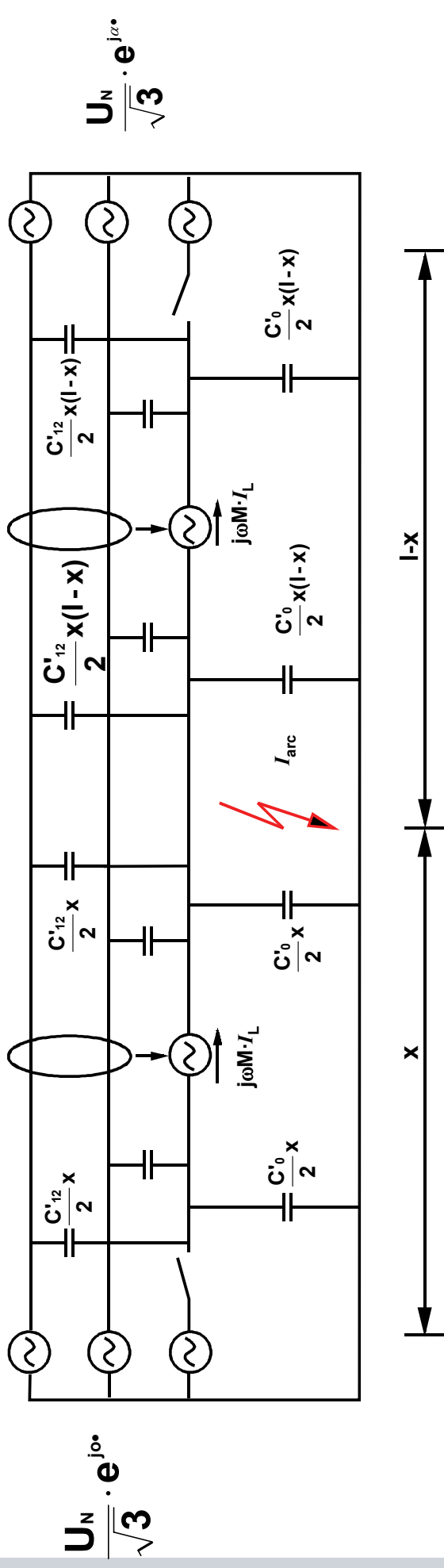
Delayed AR

- only three-pole for all fault types
- dead-time: 5 s and more
- requires synchro-checking function



Single-pole auto-reclosure Influenced and induced secondary arc currents

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$$I_{ARCc} \approx \frac{U_N}{\sqrt{3}} \cdot \omega \cdot C'_{12} \cdot l$$

$$I_{ARCL} \approx I_L \cdot \omega M' \left(\frac{1}{2} - x \right) \cdot \omega \cdot (C'_0 + 2 \cdot C'_{12}) \cdot l$$

De-ionizing times

Three-pole reclosing

$$t_{3\text{-pole}} > 10.5 + \frac{\text{kV}}{34.5} \text{ cycles}$$

50Hz:

$$t_{3\text{-pole}} > 210 + 0.58 \cdot \text{kV} \cdot [\text{ms}]$$

500 kV (50 Hz): $t = 0.5 \text{ s}$

Single-pole reclosing

for lines up to about 500 km:

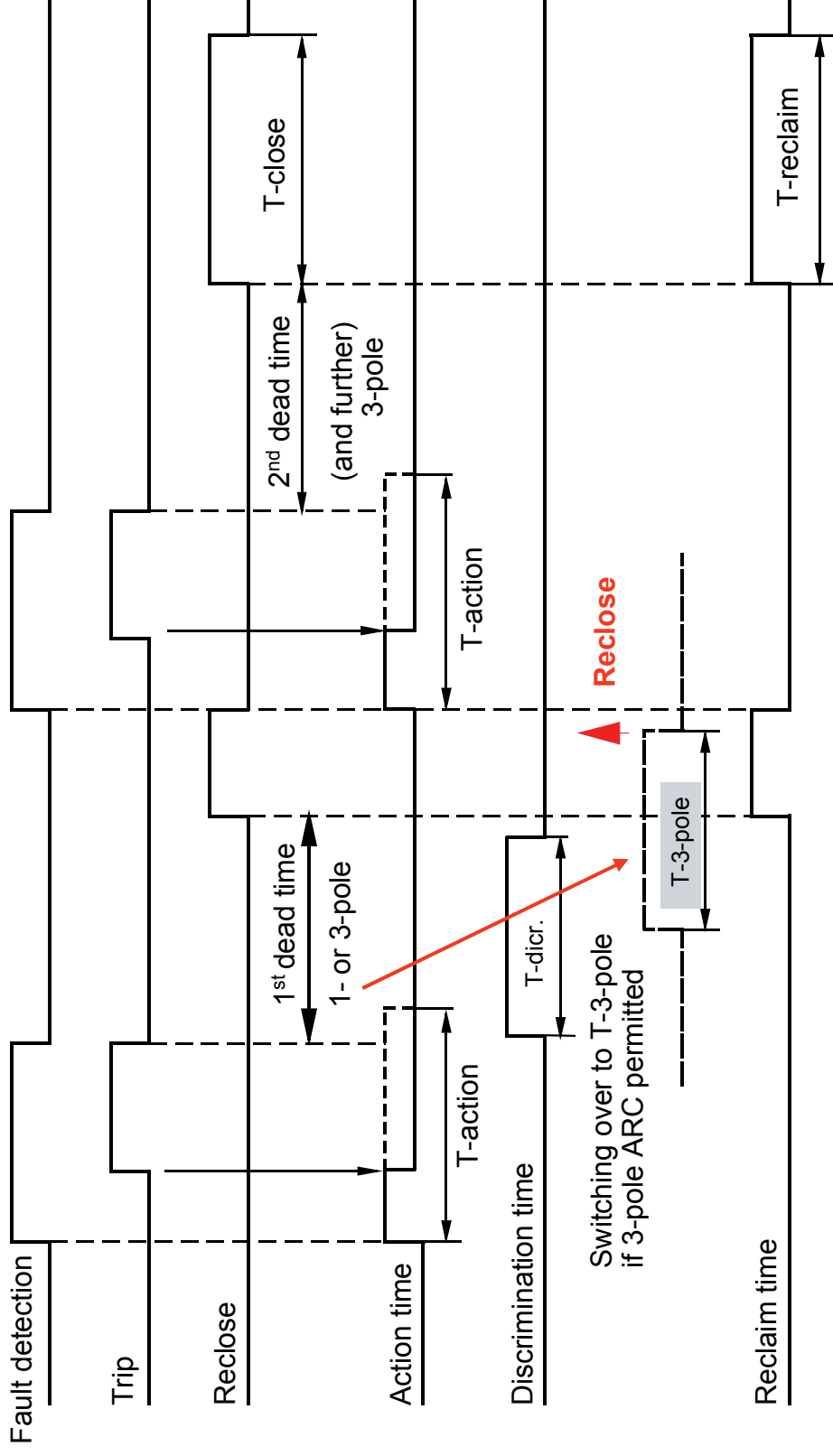
The AR will be successful with high probability if the secondary arc current is kept below following value

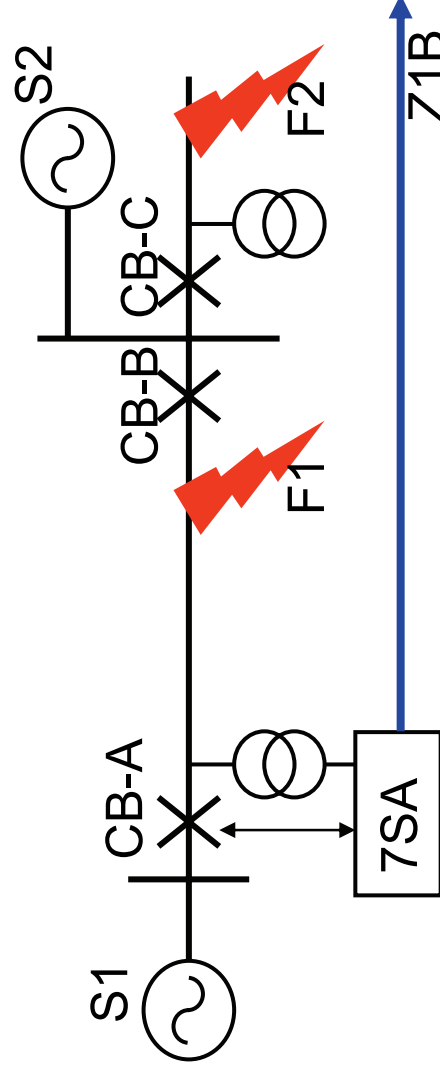
$$\frac{I_{\text{Arc}}}{\text{A}} = 43 \left(\frac{t_{\text{dead-time}}}{\text{s}} - 0.2 \right)$$

Line lengths for single-pole AR without supplemental arc extinction devices, e.g. shunt reactors

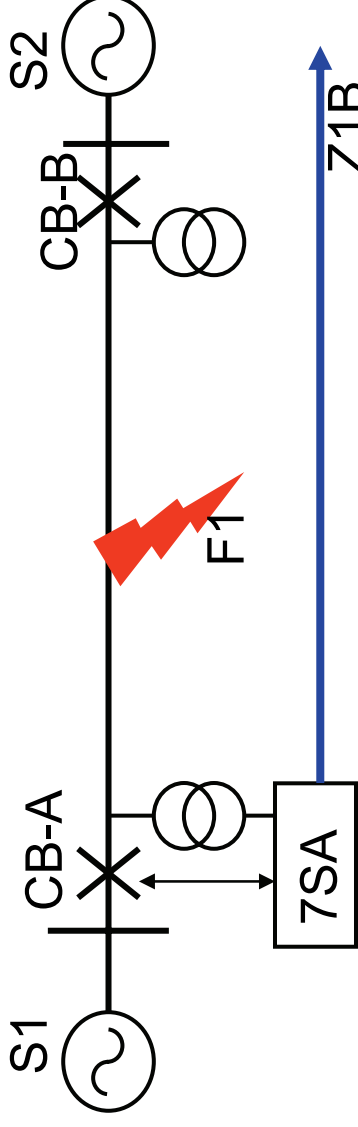
Line-to-line Voltage (kV)	Successful Range (km)	doubtful Range (km)
765	0-80	80-130
500	0-100	100-160
345	0-230	230-420
230	0-480	480-800

Auto-reclosure, Signal Sequence

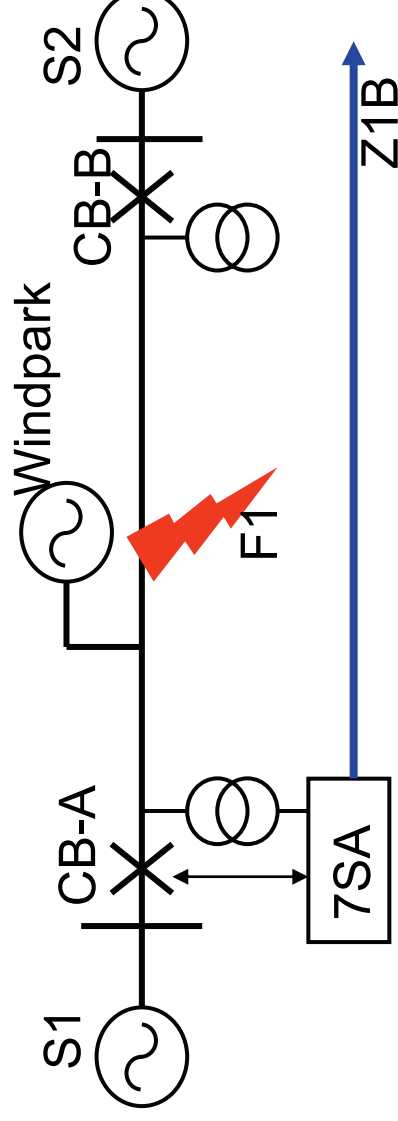




- At A the Z1B is released prior to 1st AR cycle (para 1357)
- All faults (F1) along line A-B are tripped without delay with Z1B at CB-A
- Non-selective trip for external fault (F2) is possible, but AR will be carried out
- With RDT, the dead time following non-selective trip can be minimised. CB-A is reclosed when return voltage from S2 via CB-B is detected at A after CB-C opens.



- At A and B faults along the line are cleared by stepped distance and tele-protection
- At B the AR is applied with a fixed dead time
- At A the AR is applied with ADT
- When return voltage is detected at A from S2 via CB-B following successful reclosure at B, the reclose command to CB-A is given
- If the AR at B is not successful because fault F1 is permanent, the ADT will not detect return voltage at A and reclosure onto the fault is prevented at A



- The Fault F1 is cleared by the protection at A and B. The Windpark must disconnect itself by undervoltage detection.
- Reclosure at A and B may only occur if the Windpark is disconnected – un-synchronised closure will damage Windpark
- At A and B the DLC feature will only allow reclosure following a dead line condition (no voltage) for set time (para 3438)

Distance Protection of Three-terminal

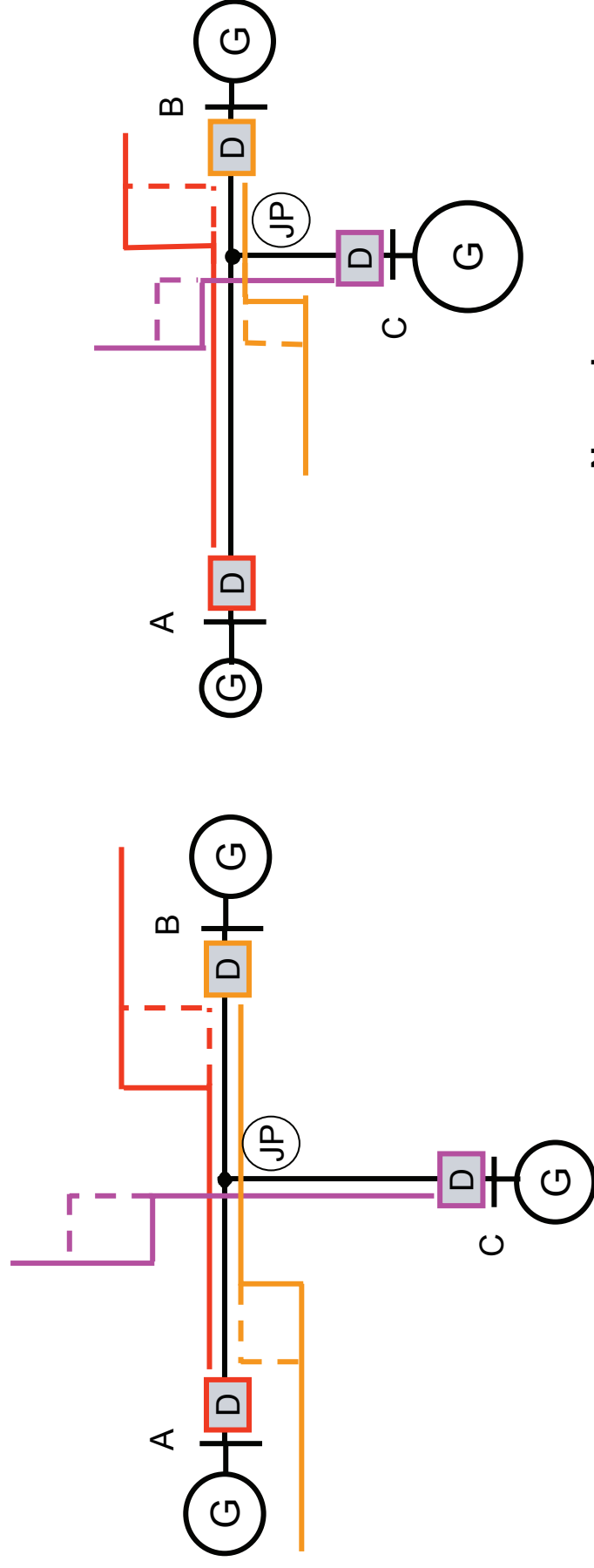
Lines



Three-terminal line

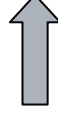
Distance protection without communication

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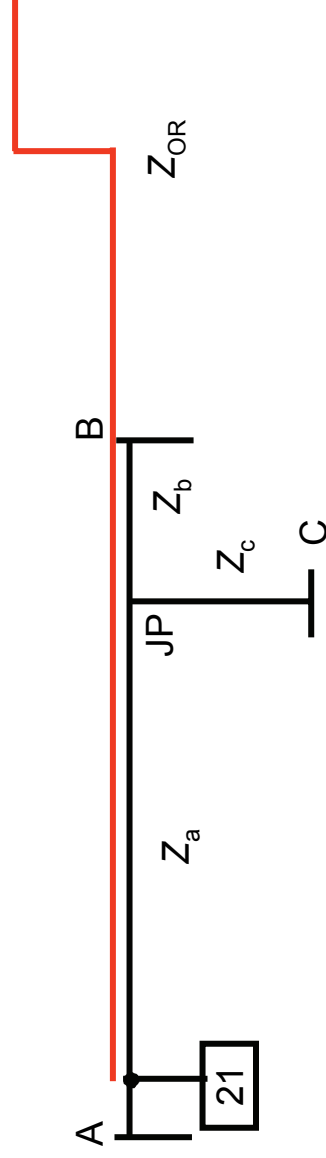
Normal case:

Unequal line lengths
Unequal infeeds (SCCs“)



Reach of zones too short!

Three-terminal-lines Setting of overreaching zones



Factor-2 Formula:

$$Z_{OR} = (Z_X + 2 \cdot Z_Y) \cdot k_{OR}$$

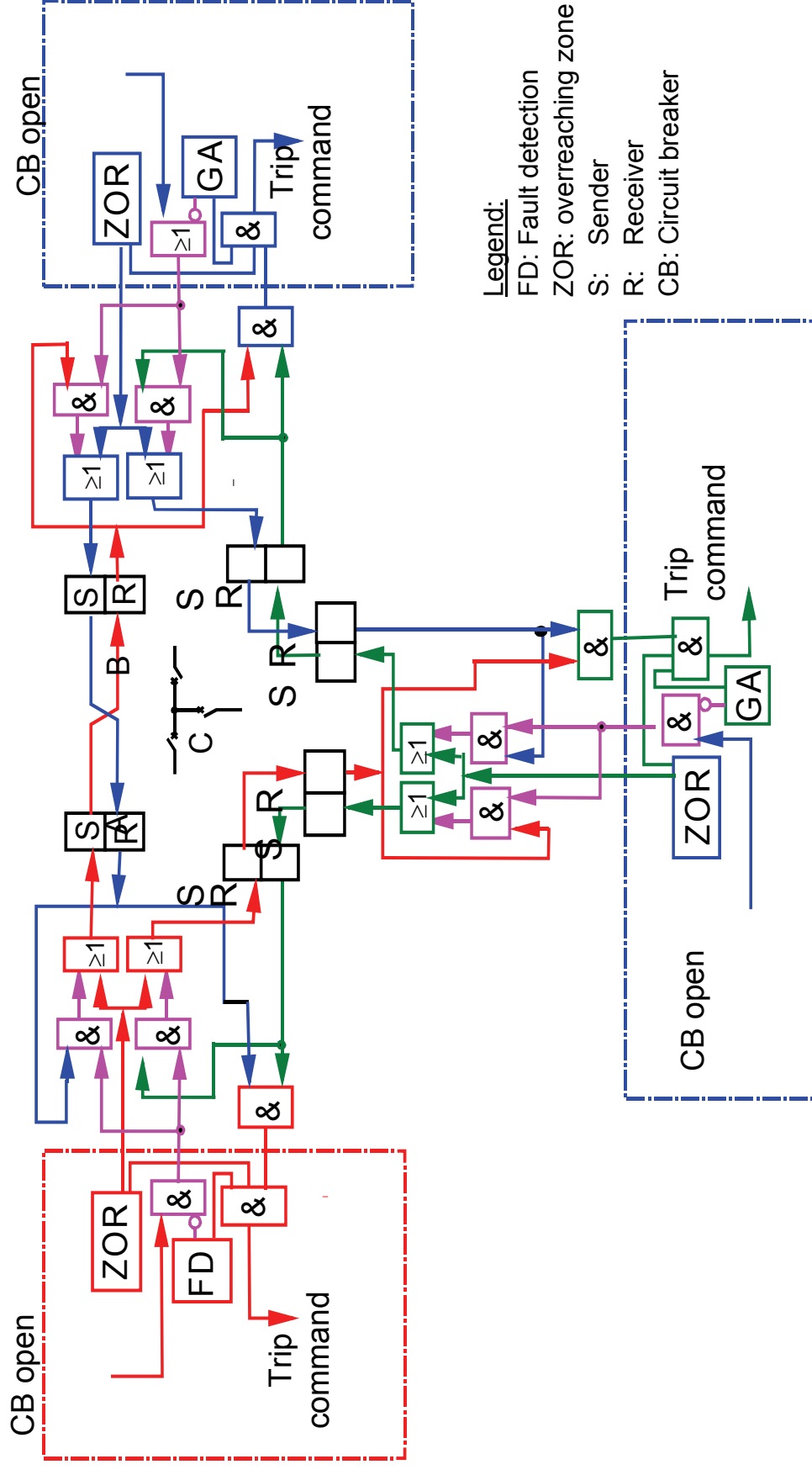
with:

Z_X = Impedance from relay to junction point (JP)

Z_Y = Impedance from junction point to (JP) to farthest line end

k_{OR} = Grading factor (z.B. 1,2)

Three-terminal line Teleprotection in POTT mode



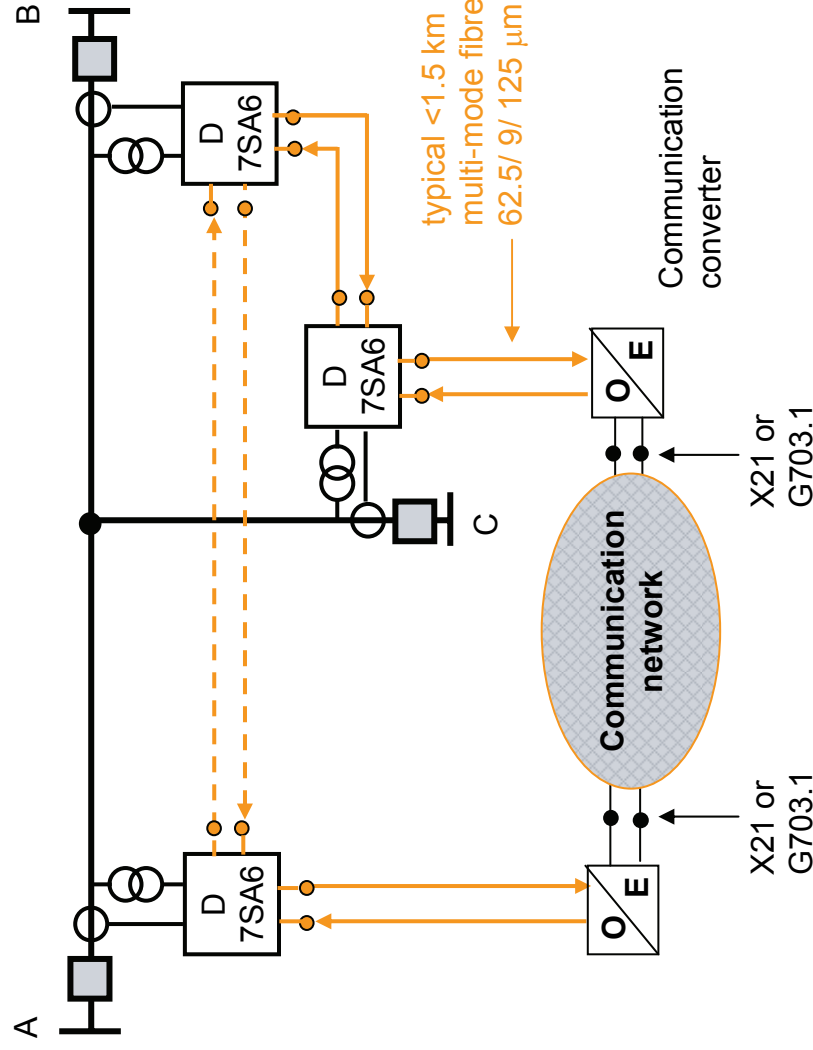
Distance protection of a three-terminal line PUTT or POTT scheme using digital communication

SIEMENS

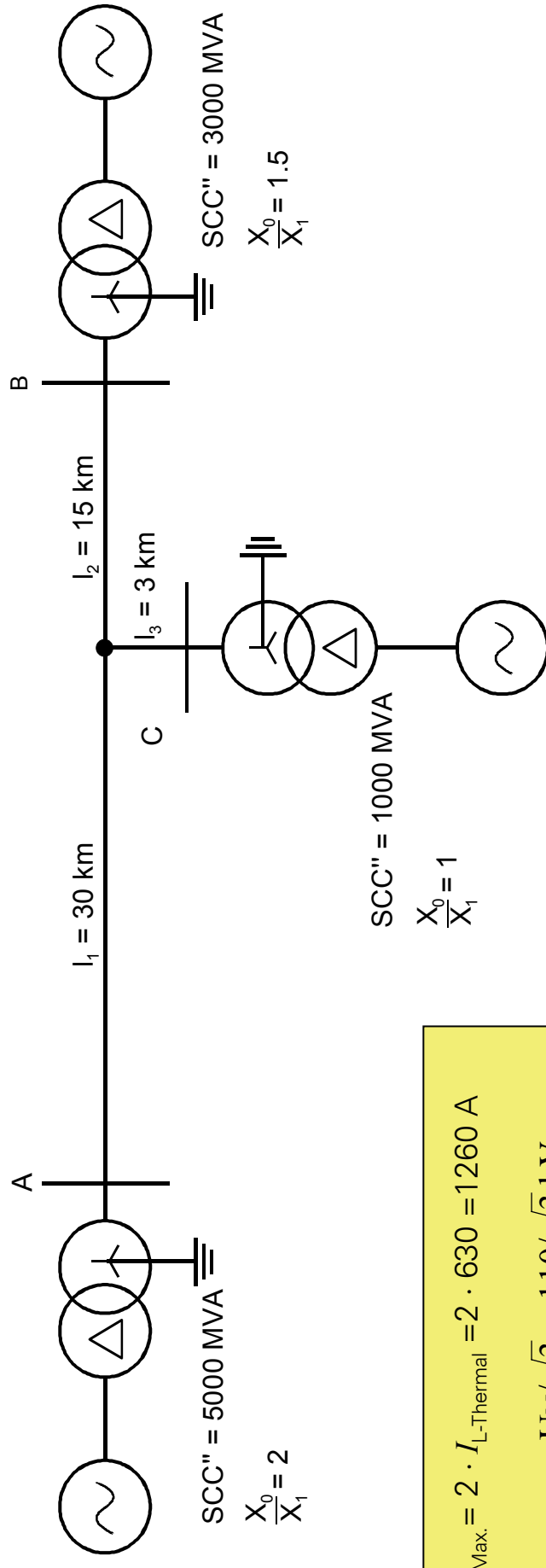
Chain topology or
redundant ring topology

Communication via direct relay-relay connection

Fibre type	optical wave length	permissible attenuation	maximum distance
Multi-mode 62.5/125 μm	820 nm	16 dB	ca. 3.5 km
Mono-mode 9/ 125 μm	1300 nm	18 dB	ca. 35 km



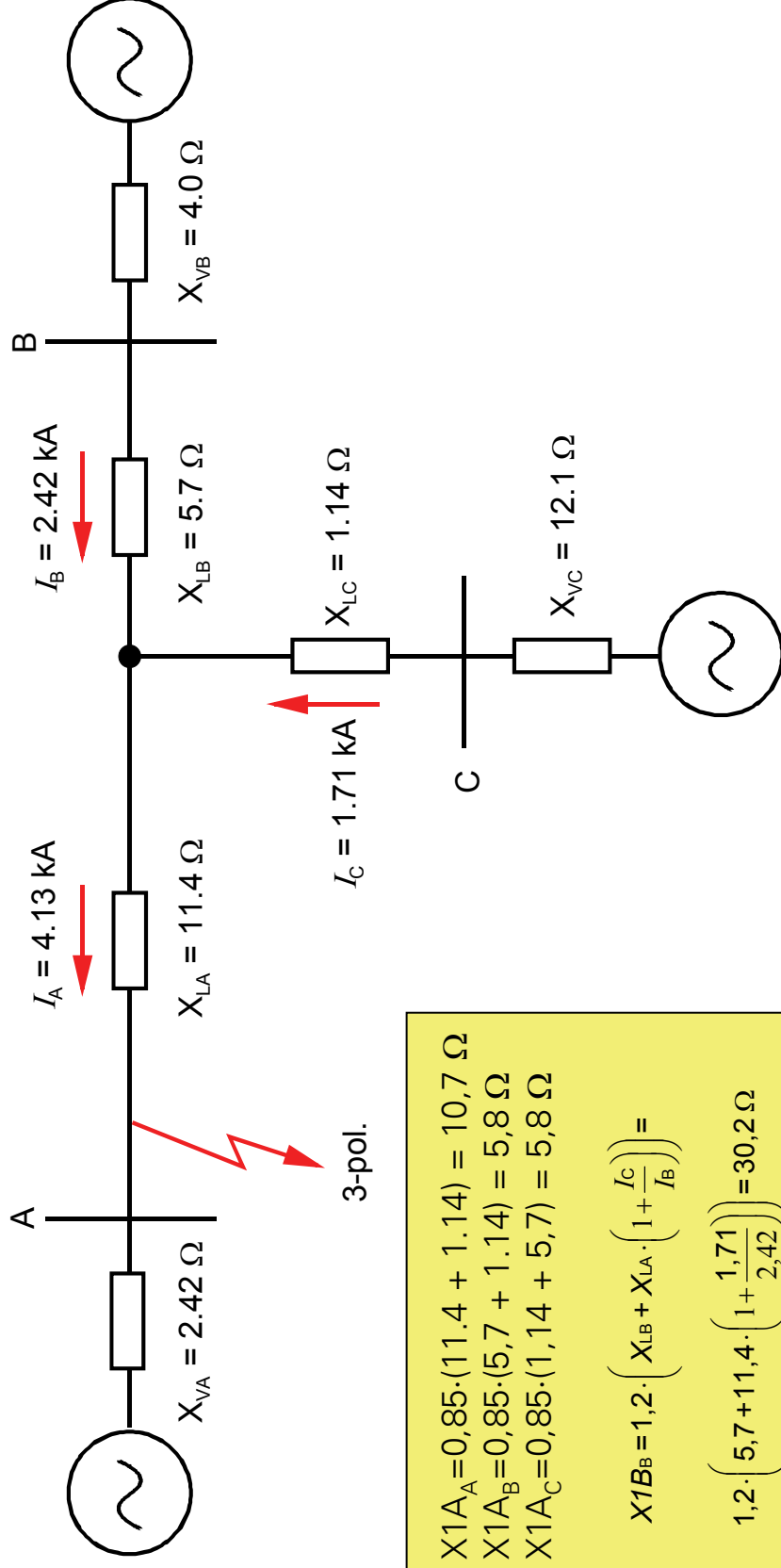
Distance protection of three-terminal lines (1) Computation example



$$I_{L-\text{Max.}} = 2 \cdot I_{L-\text{Thermal}} = 2 \cdot 630 = 1260 \text{ A}$$

$$Z_{\text{load - min.}} = \frac{U_N / \sqrt{3}}{I_{L-\text{max.}}} = \frac{110 / \sqrt{3} \text{ kV}}{1,260 \text{ kA}} = 50 \Omega$$

Distance protection of three-terminal lines Computation example (2)



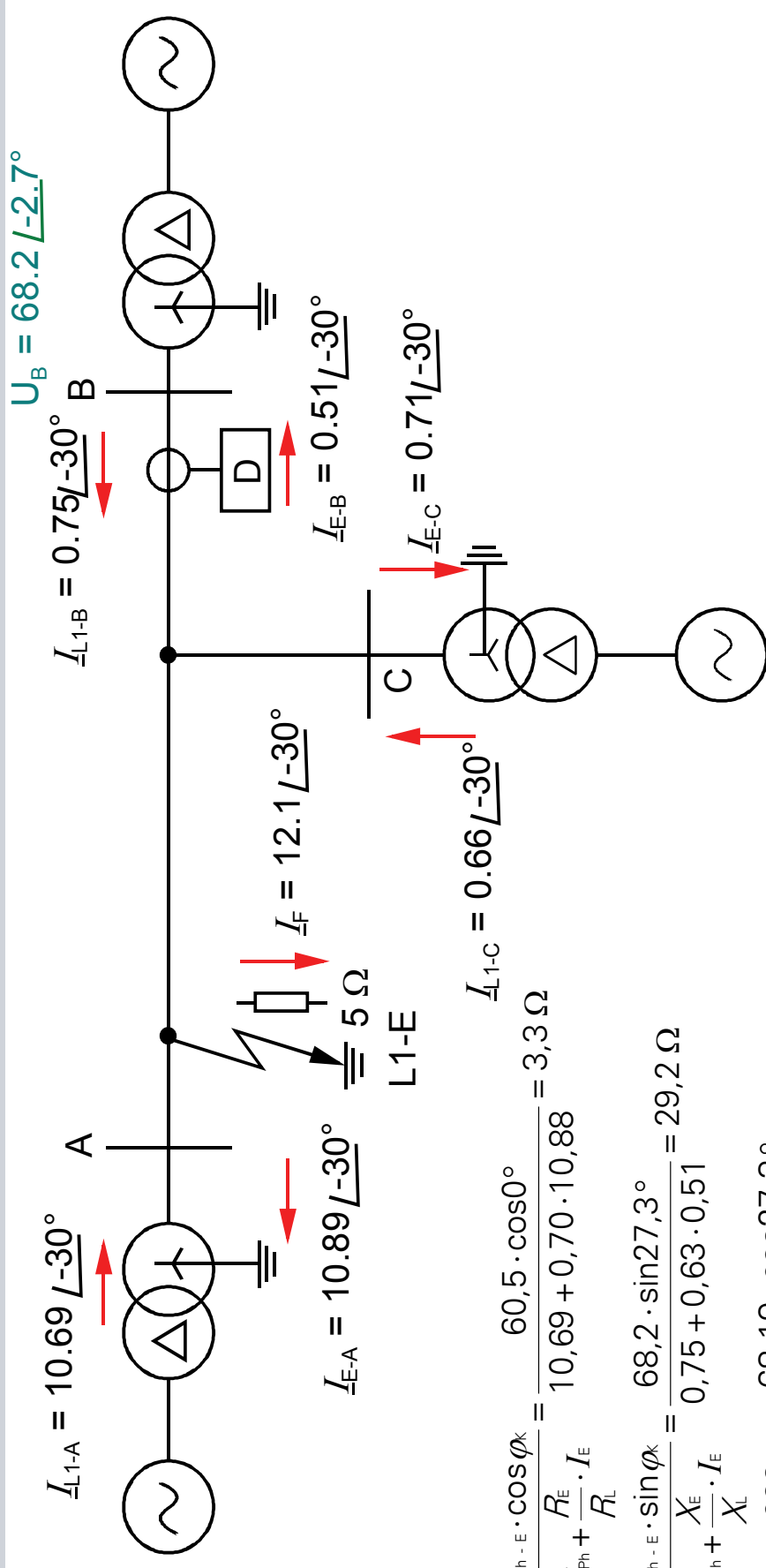
$$\begin{aligned} X1A_A &= 0,85 \cdot (11,4 + 1,14) = 10,7 \Omega \\ X1A_B &= 0,85 \cdot (5,7 + 1,14) = 5,8 \Omega \\ X1A_C &= 0,85 \cdot (1,14 + 5,7) = 5,8 \Omega \end{aligned}$$

$$X1B_B = 1,2 \cdot \left(X_{LB} + X_{LA} \cdot \left(1 + \frac{I_C}{I_B} \right) \right) =$$

$$1,2 \cdot \left(5,7 + 11,4 \cdot \left(1 + \frac{1,71}{2,42} \right) \right) = 30,2 \Omega$$

Distance protection of three-terminal lines

Computation example (3)



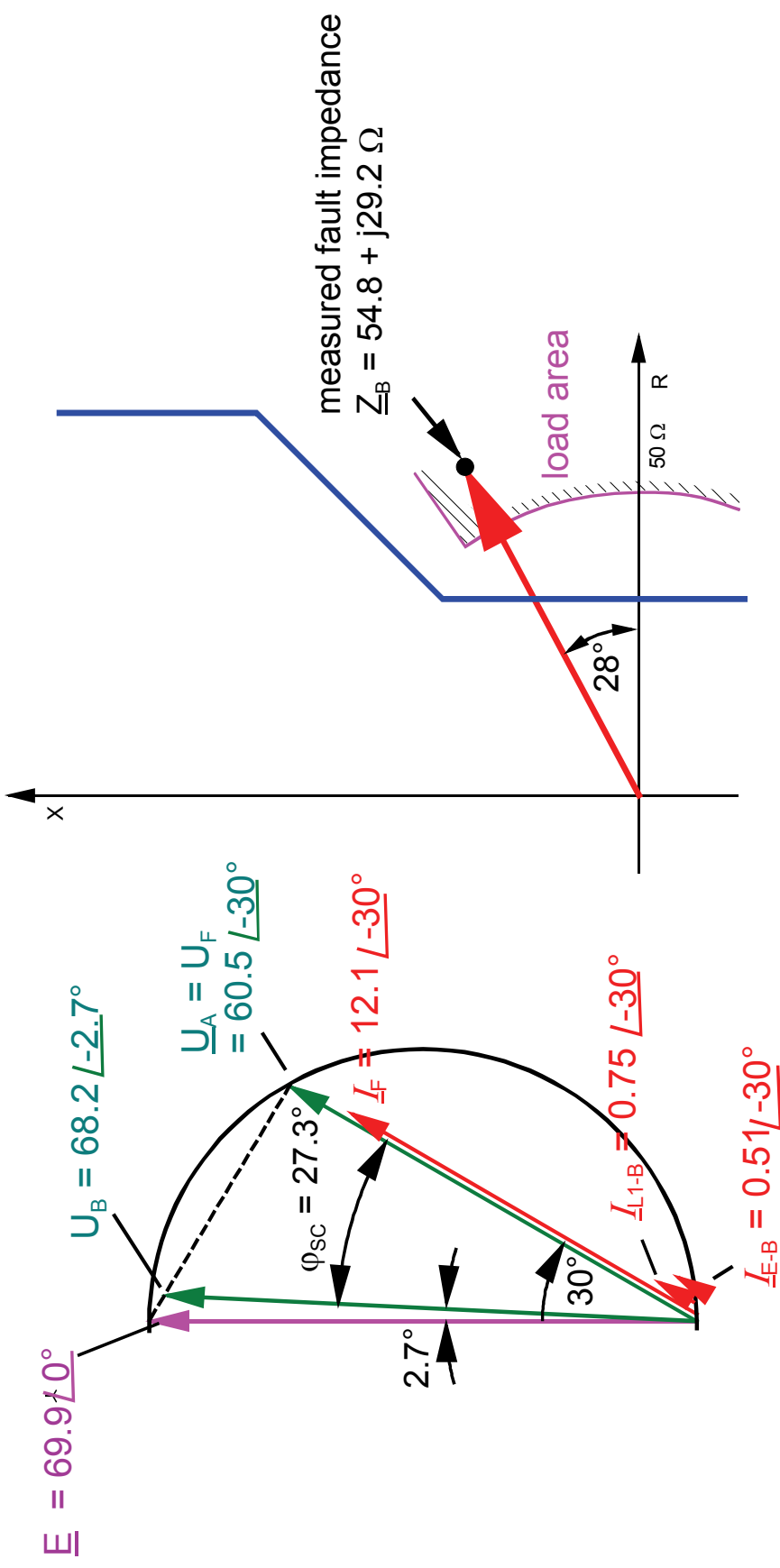
$$(X_{L^1-E})^A = 0$$

$$(R_{L1-E})_A = \frac{U_{Ph-E} \cdot \cos \varphi_K}{I_{Ph} + \frac{R_E \cdot I_E}{R_I}} = \frac{60,5 \cdot \cos 0^\circ}{10,69 + 0,70 \cdot 10,88} = 3,3 \Omega$$

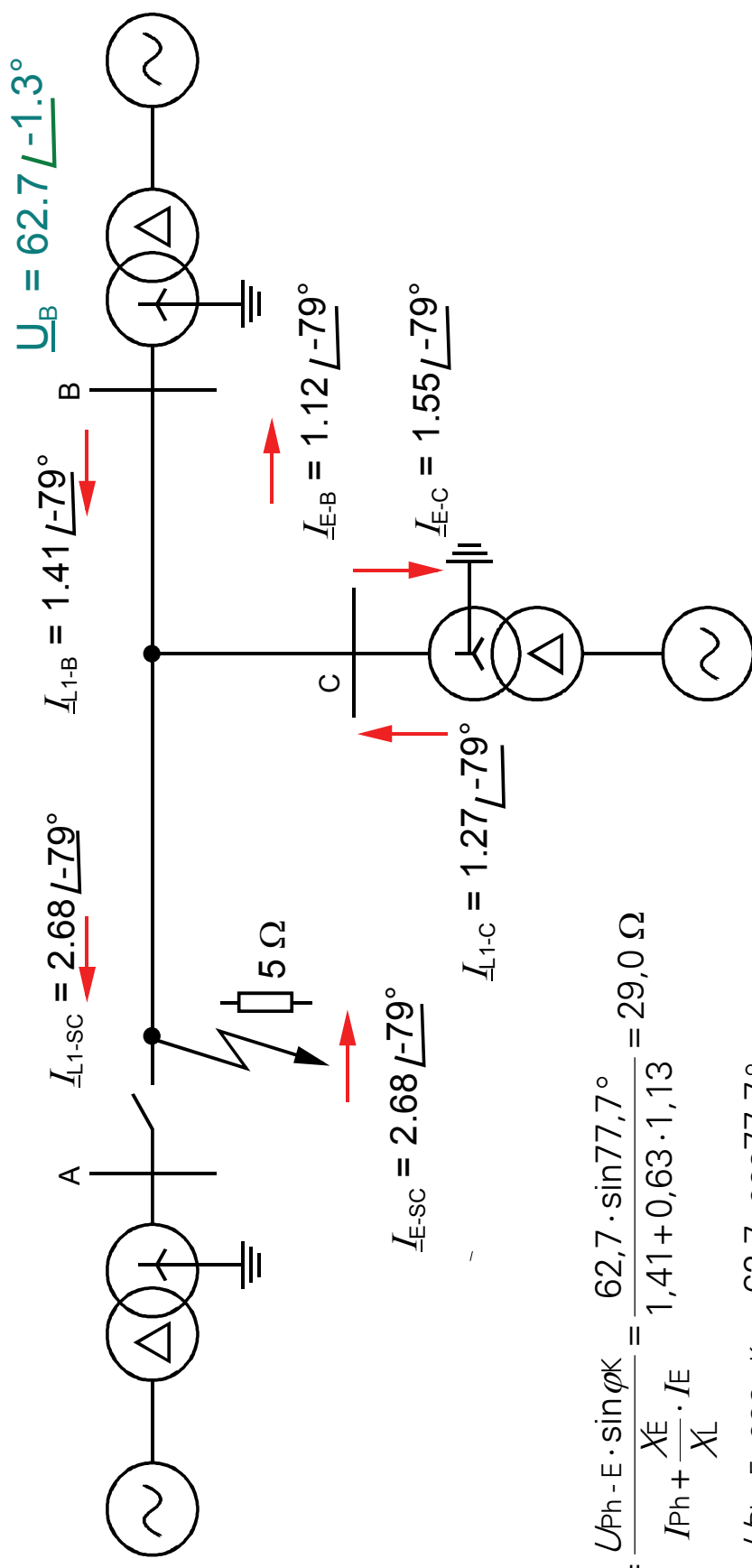
$$(X_{L1-E}^B) = \frac{U_{Ph-E} \cdot \sin \varphi_K}{I_{Ph} + \frac{X_E \cdot I_E}{X}} = \frac{68,2 \cdot \sin 27,3^\circ}{0,75 + 0,63 \cdot 0,51} = 29,2 \, \Omega$$

$$(R_{\text{L1-E}})_{\text{B}} = \frac{U_{\text{ph-E}} \cdot \cos \varphi_{\text{K}}}{I_{\text{ph}} + \frac{R_{\text{E}}}{R_{\text{I}}}} = \frac{68,19 \cdot \cos 27,3^{\circ}}{0,75 + 0,70 \cdot 0,51} = 54,8 \Omega$$

Distance protection of three-terminal lines, Computation example (4) Fault Ph-E with R_F , measured values after fault inception



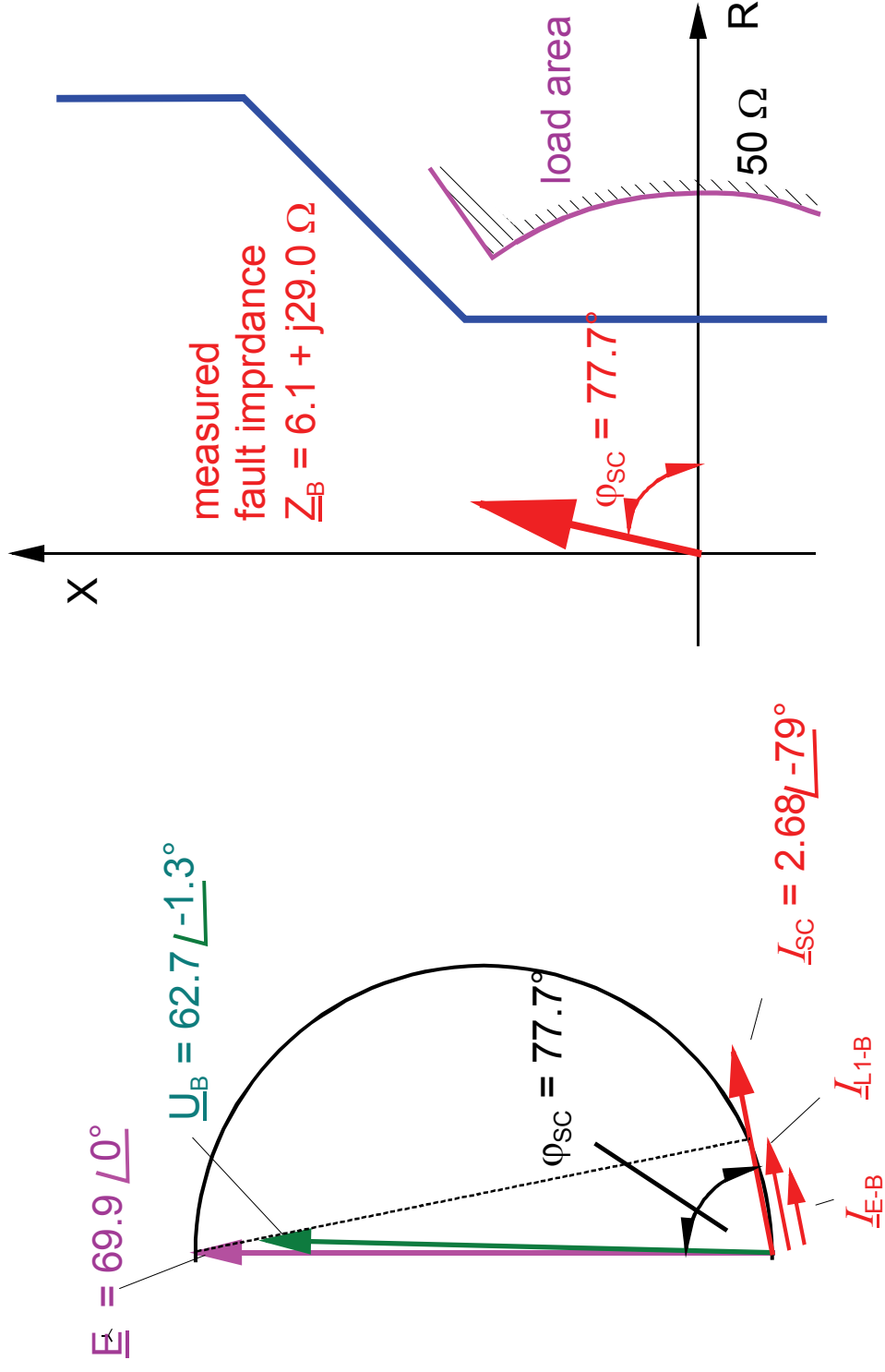
Distance protection of three-terminal lines, computation example (5) Fault Ph-E with R_F , measured values at B after tripping at A



$$(X_{Ph-E})_B = \frac{U_{Ph-E} \cdot \sin \varphi_K}{I_{Ph} + \frac{X_E}{X_L} \cdot I_E} = \frac{62,7 \cdot \sin 77,7^\circ}{1,41 + 0,63 \cdot 1,13} = 29,0 \, \Omega$$

$$(R_{Ph-E})_B = \frac{U_{Ph-E} \cdot \cos \varphi_K}{I_{Ph} + \frac{R_E}{R_L} \cdot I_E} = \frac{62,7 \cdot \cos 77,7^\circ}{1,41 + 0,70 \cdot 1,13} = 6,1 \, \Omega$$

Distance protection of three-terminal lines, computation example (6) Fault Ph-E with R_F , measured values at B after tripping A



Distance Protection of Series Compensated

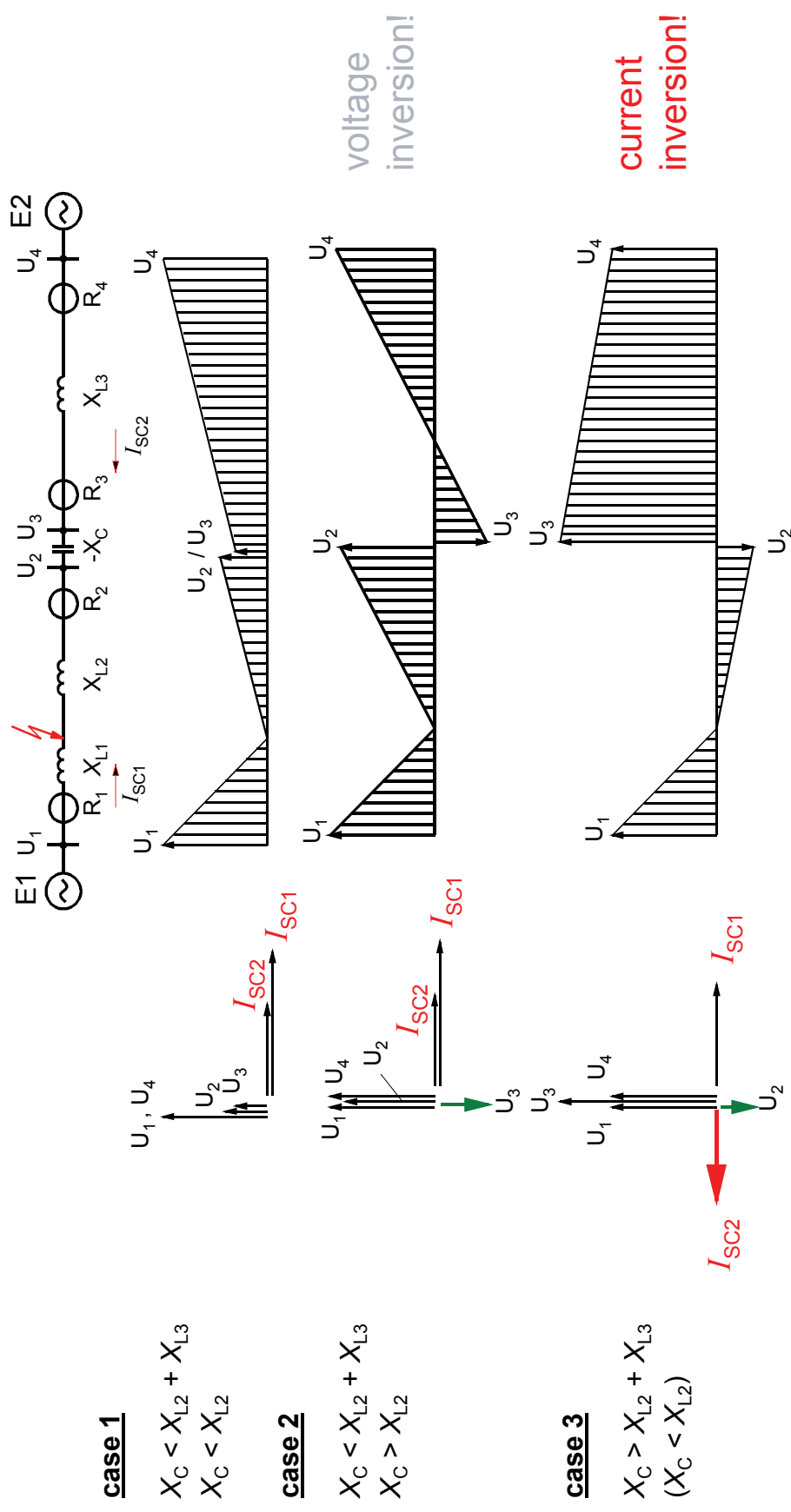
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Lines



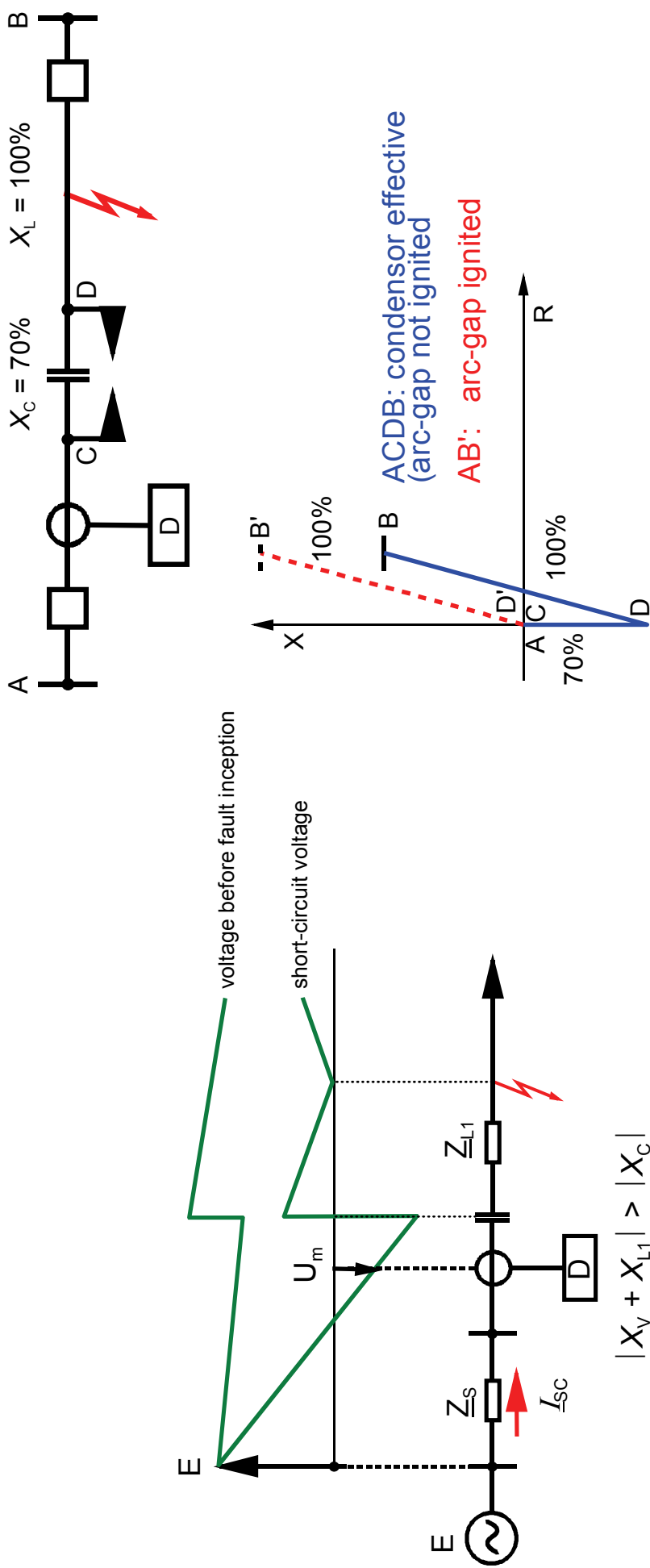
© Siemens AG 2006

Short-circuit voltage and current on series compensated lines



Distance protection of series compensated lines

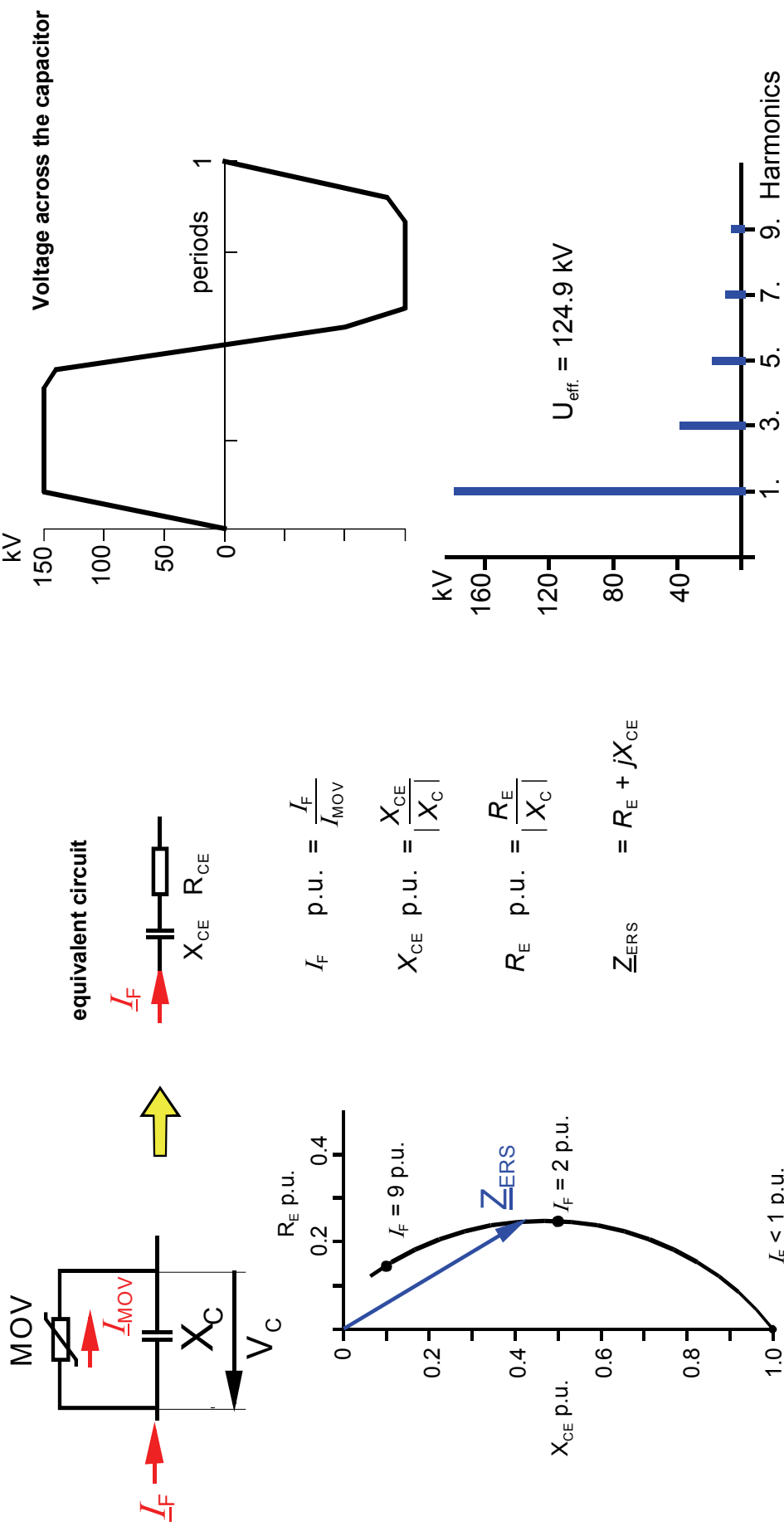
Voltage inversion and apparent impedances



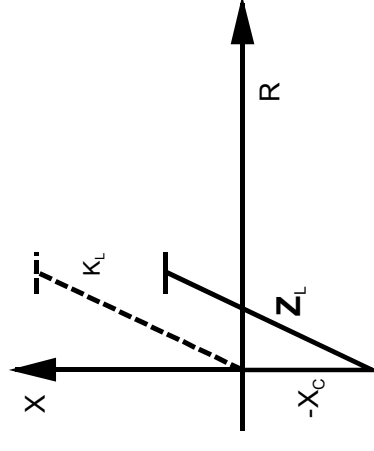
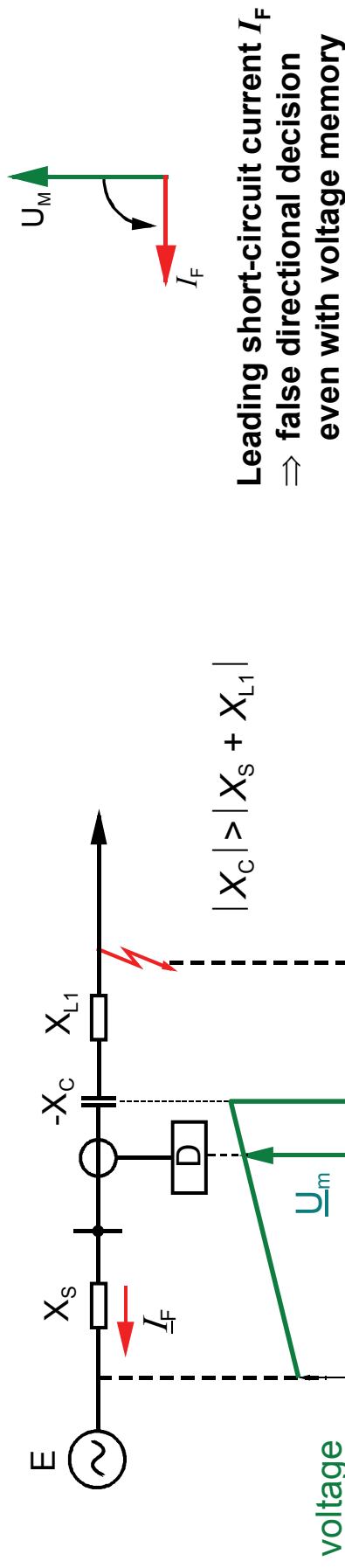
Voltage inversion!

**Measured relay impedances
(condensor at the beginning of the line)**

Distance protection of series compensated lines Influence of the voltage limiter (MOV) at the series capacitor

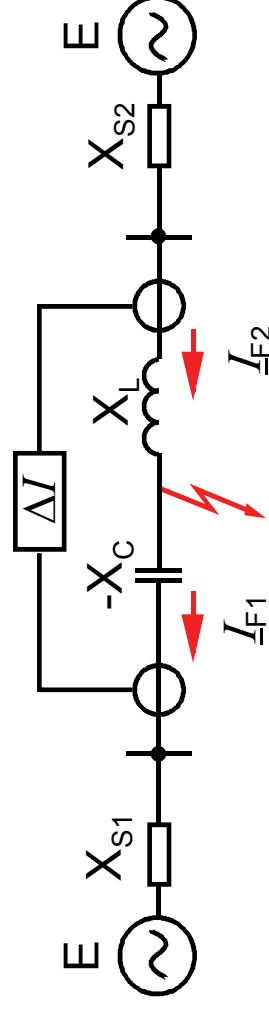


Distance protection of series compensated lines impact of current inversion

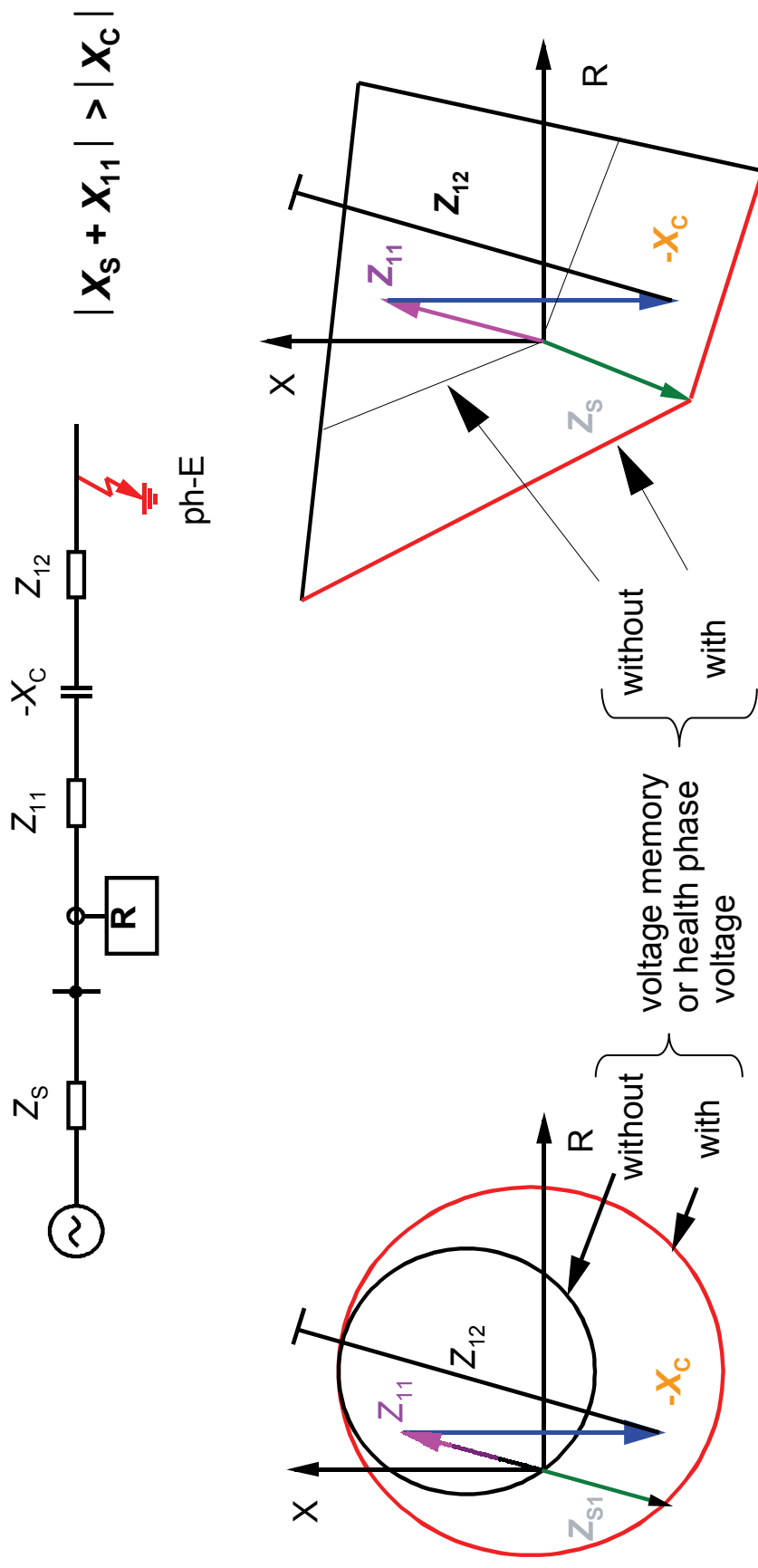


**False through fault condition appears!
 Even differential protection may not operate!**

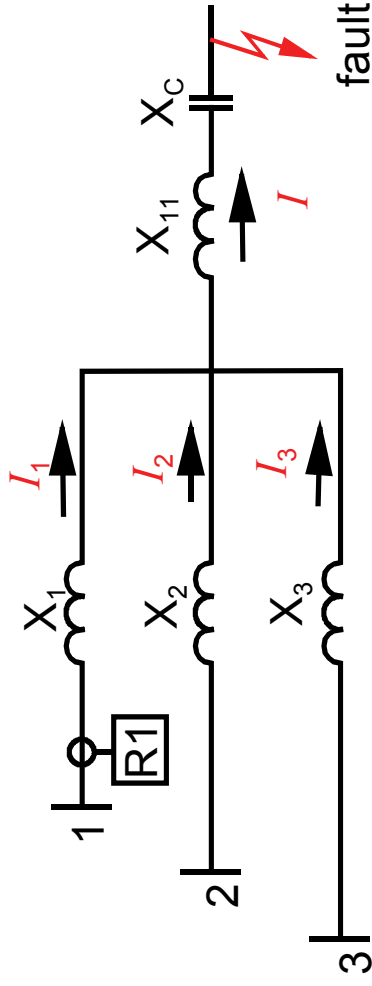
relay measures negative impedance



Protection of series compensated lines Use of healthy phase / memorised voltages



Distance protection of series compensated lines Impact of series capacitors on adjacent lines



With: $[X_C] > [X_{11}]$:

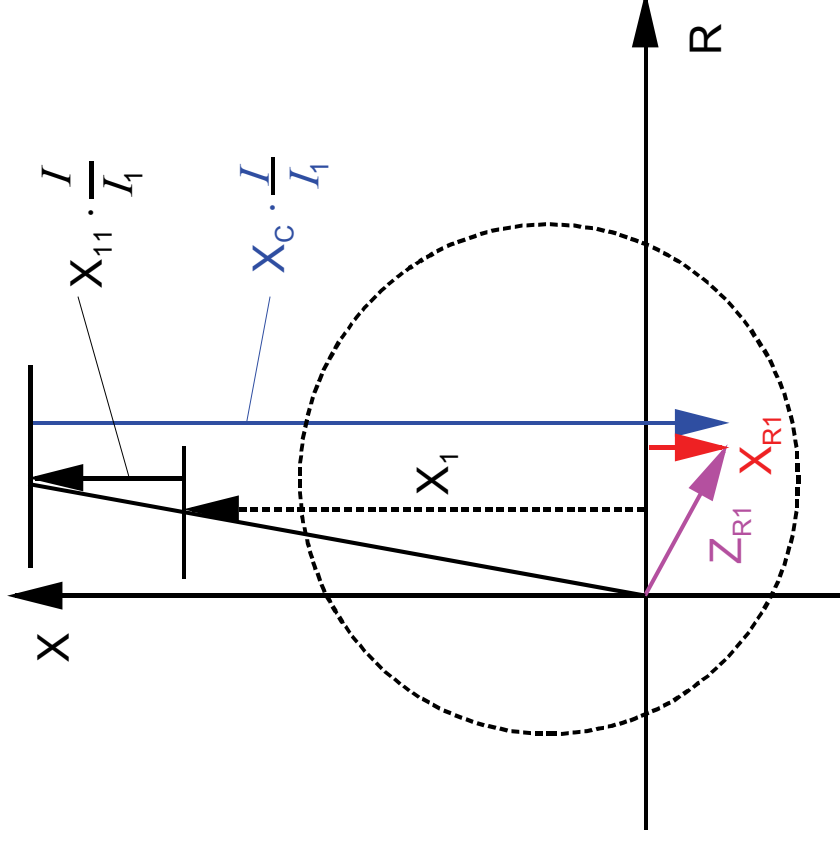
$$X_{R1} = X_1 - \frac{I}{I_1} \cdot (X_C - X_{11})$$

$$X_{R2} = X_2 - \frac{I}{I_2} \cdot (X_C - X_{11})$$

$$X_{R3} = X_3 - \frac{I}{I_3} \cdot (X_C - X_{11})$$

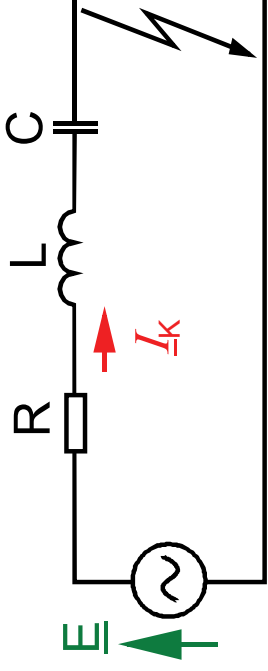
$$I_1 + I_2 + I_3 = I$$

$X_{R1,2,3}$ = reactances seen by the relays
in station 1, 2 and 3



X_{R1} : reactance seen by relay in station 1

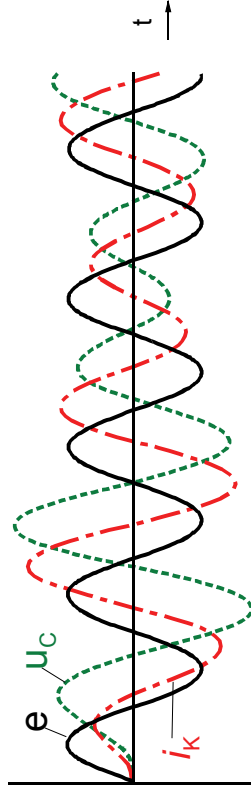
Series compensated lines Transient fault current



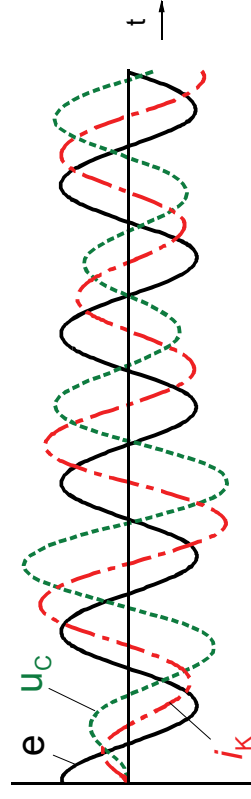
Short-circuit loop of a series compensated line

$$\hat{E} \cdot \sin(\omega t + \lambda) = L \frac{di_{sc}}{dt} + R \cdot i_{sc} + \frac{1}{C} \int i_{sc} dt$$

$$i_{sc} = \hat{I} \cdot \sin(\omega t + \lambda - \Theta) + e^{-\alpha t} (K_1 \cos \beta t + K_2 \sin \beta t)$$



Short-circuit at voltage
zero crossing



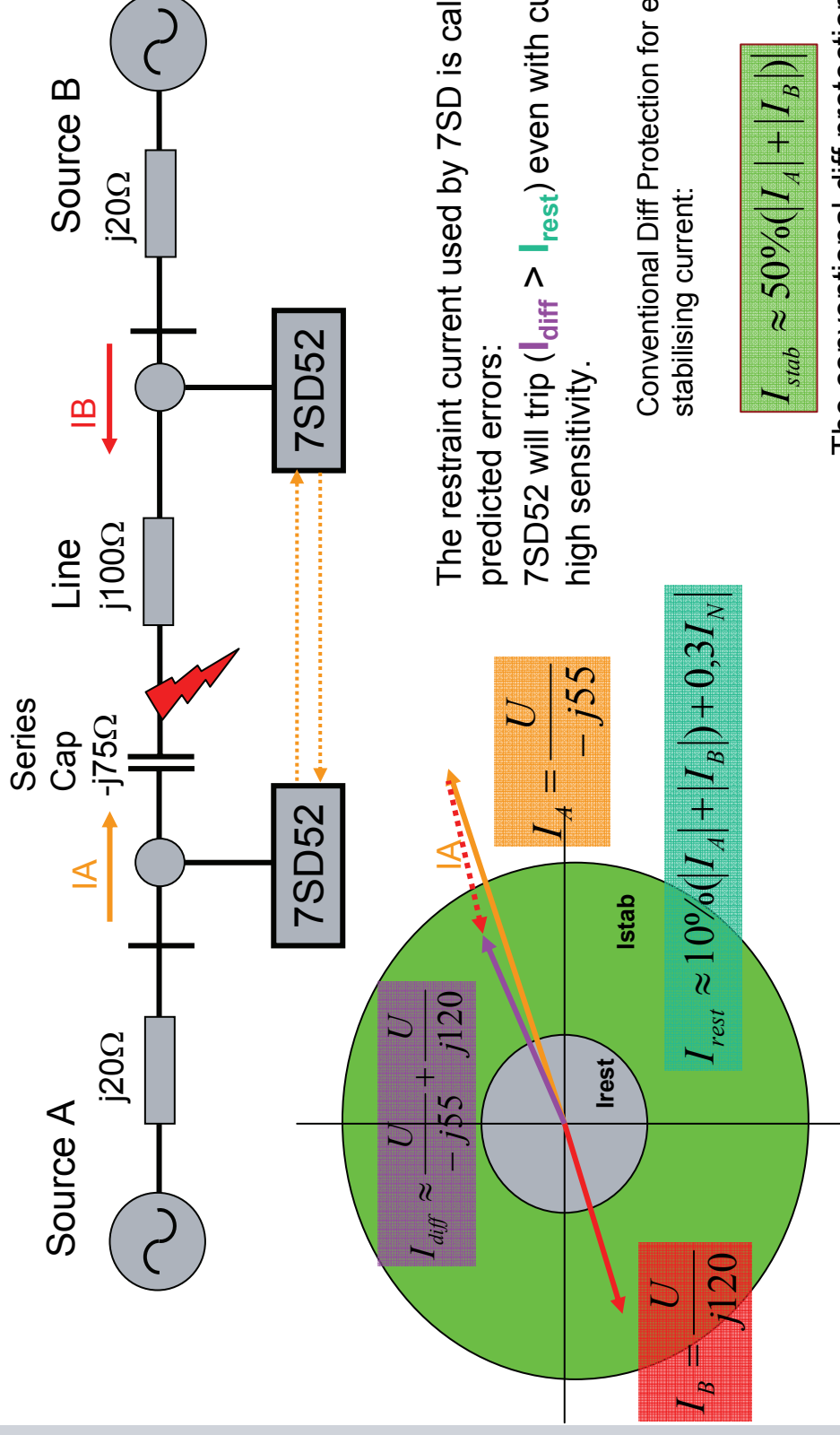
Short-circuit at voltage
maximum

compensation degree :

$$k_C = \frac{X_C}{X_L} = 50\%$$

$$k_{Trans} = \frac{1}{1 + \hat{U}_{gap} / (\sqrt{2} * E)}$$

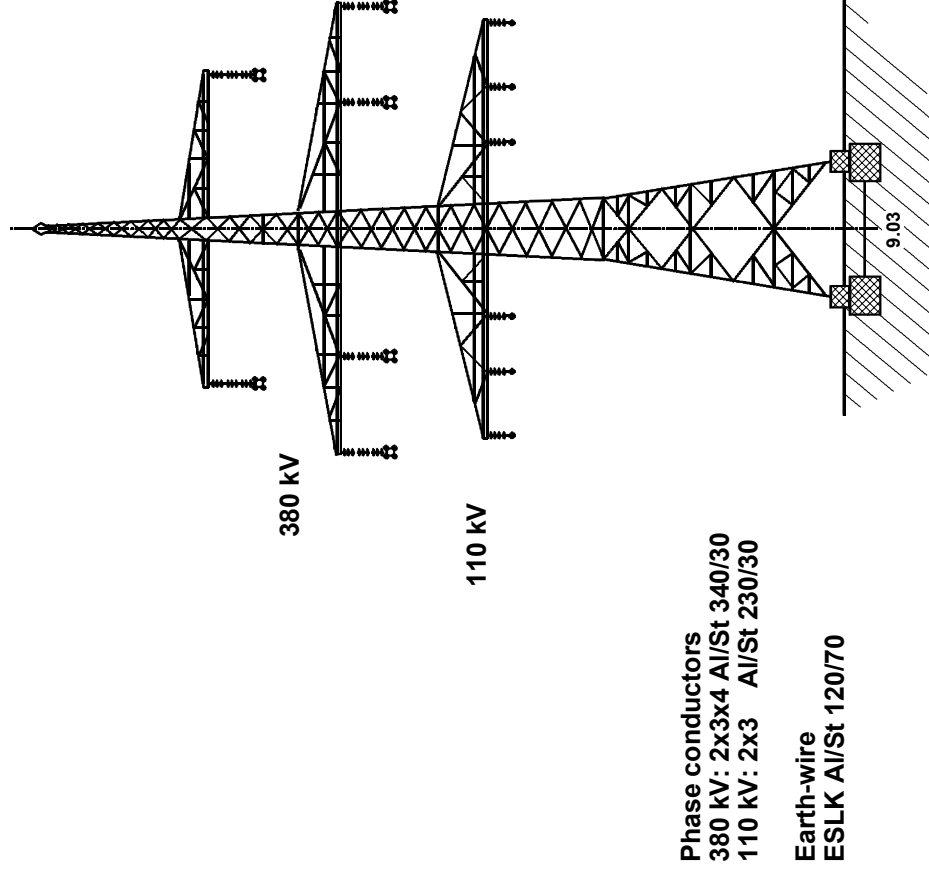
Current Inversion and 7SD52 Differential Protection (example)



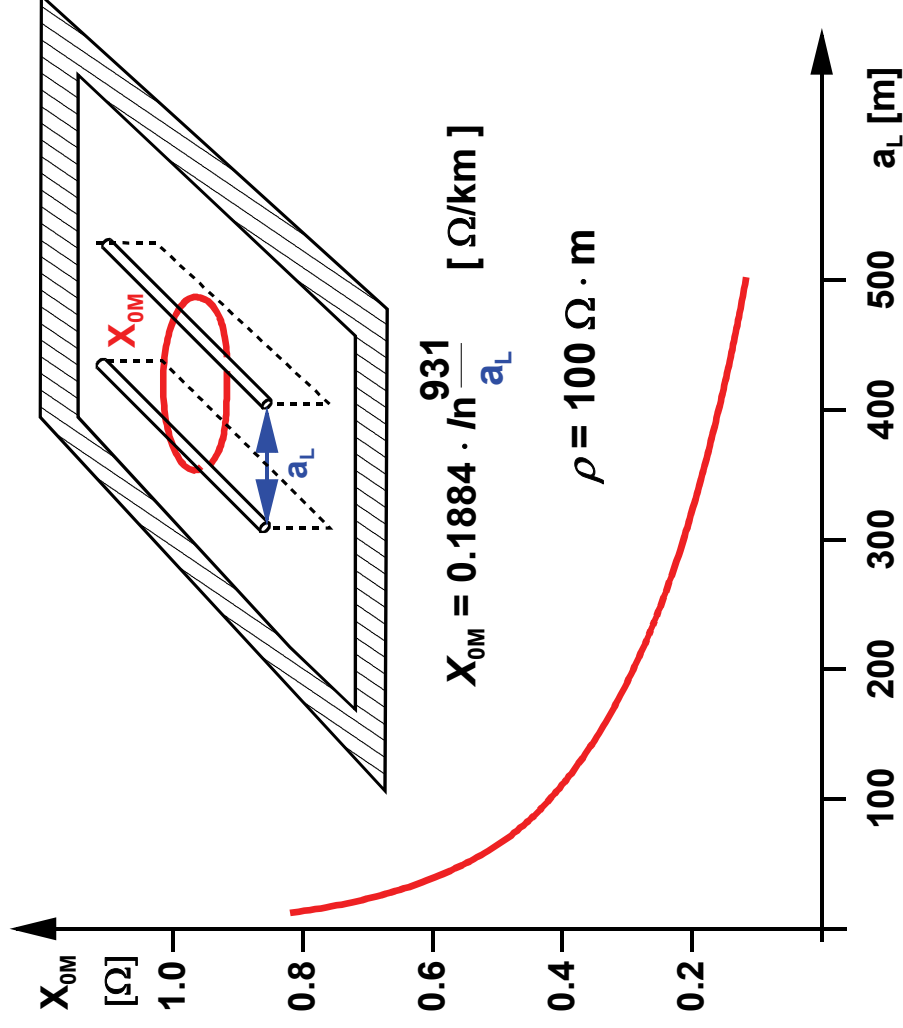
Distance Protection of Parallel Lines

Multiple circuit OH-line tower (Germany)

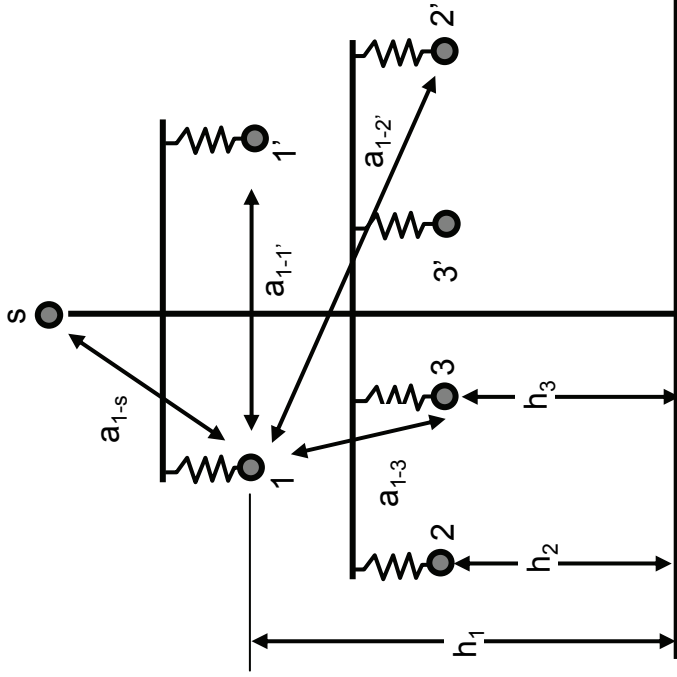
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Mutual reactance of two conductor-earth loops



Calculation of line impedances Parallel line (transposed)



$$A = \sqrt[3]{a_{1-2} \cdot a_{2-3} \cdot a_{3-1}} \quad A_s = \sqrt[3]{a_{1-s} \cdot a_{2-s} \cdot a_{3-s}}$$

$$A' = \sqrt[3]{a_{1-2'} \cdot a_{2-3'} \cdot a_{3-1'}}$$

$$A'' = \sqrt[3]{a_{1-1'} \cdot a_{2-2'} \cdot a_{3-3'}}$$

$$A_L = \sqrt[3]{A'^2 \cdot A''}$$

Parallel line **without** earth wire

$$\underline{Z}'_{M0} = 3 \cdot R'_E + j\omega \cdot 10^{-4} \cdot 6 \cdot \ln \frac{\delta}{AL} \quad \Omega/\text{km}$$

Parallel line **with** earth wire

$$\underline{Z}'_{M0E} = \underline{Z}'_{M0} - \frac{3 \cdot \underline{Z}'_{1s}{}^2}{\underline{Z}'_{-s}} \quad \Omega/\text{km}$$

with: $\underline{Z}'_{1s} = R'_E + j\omega \cdot 10^{-4} \cdot 2 \cdot \ln \frac{\delta}{A_s} \quad \Omega/\text{km}$

$$\underline{Z}'_{-s} = R'_s + R'_E + j\omega \cdot 10^{-4} \cdot \left(2 \cdot \ln \frac{\delta}{r'_s} + 0.5 \cdot \mu_1 \right) \quad \Omega/\text{km}$$

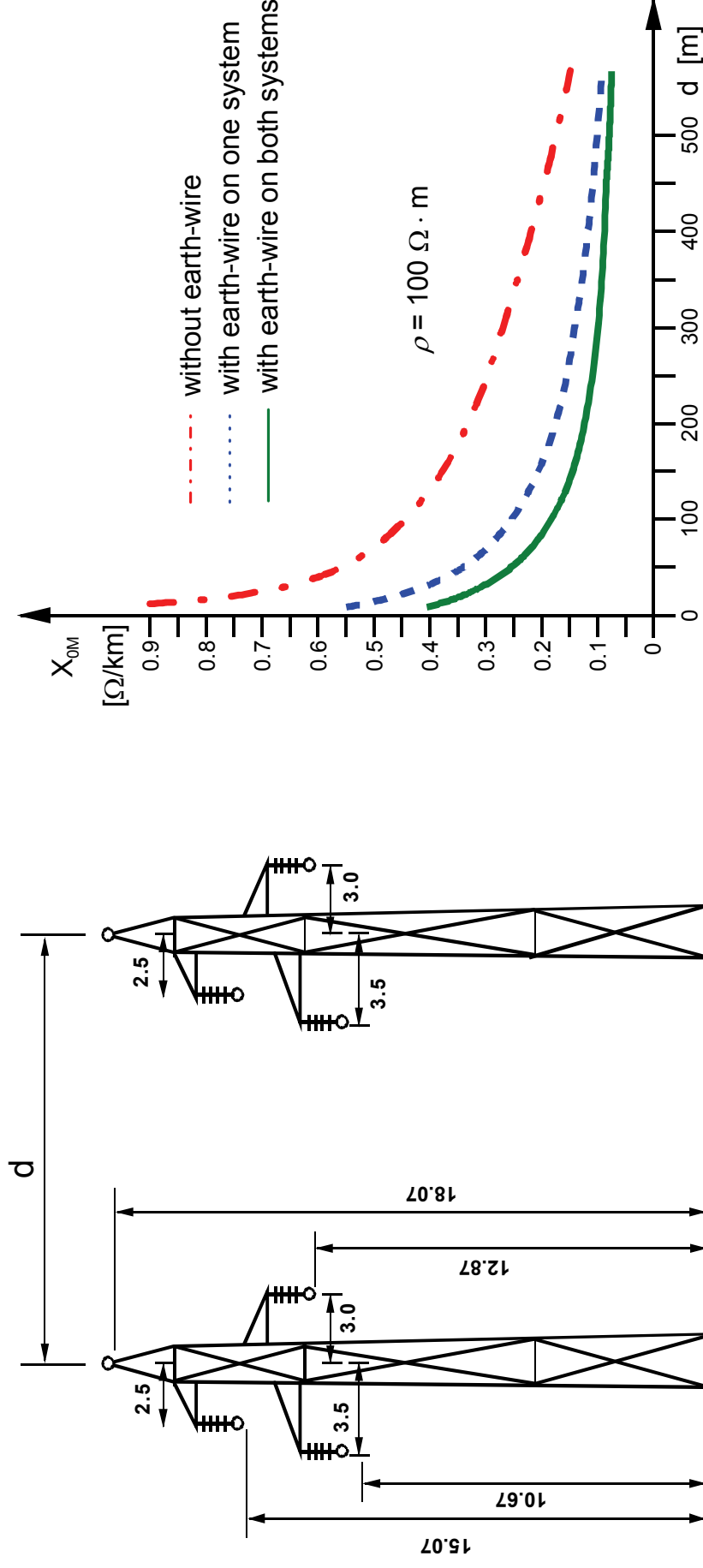
$$\delta = 1650 \cdot \sqrt{\frac{\rho}{\omega}} \quad m \quad \text{und} \quad R'_E = \frac{\pi}{2} \cdot \omega \cdot 10^{-4} \quad \Omega/\text{km}$$

ρ : Earth resistivity in Ωm
100 for wet soil, 500 for dry soil

μ_1 : relative Permeability (1 for Cu and AL)

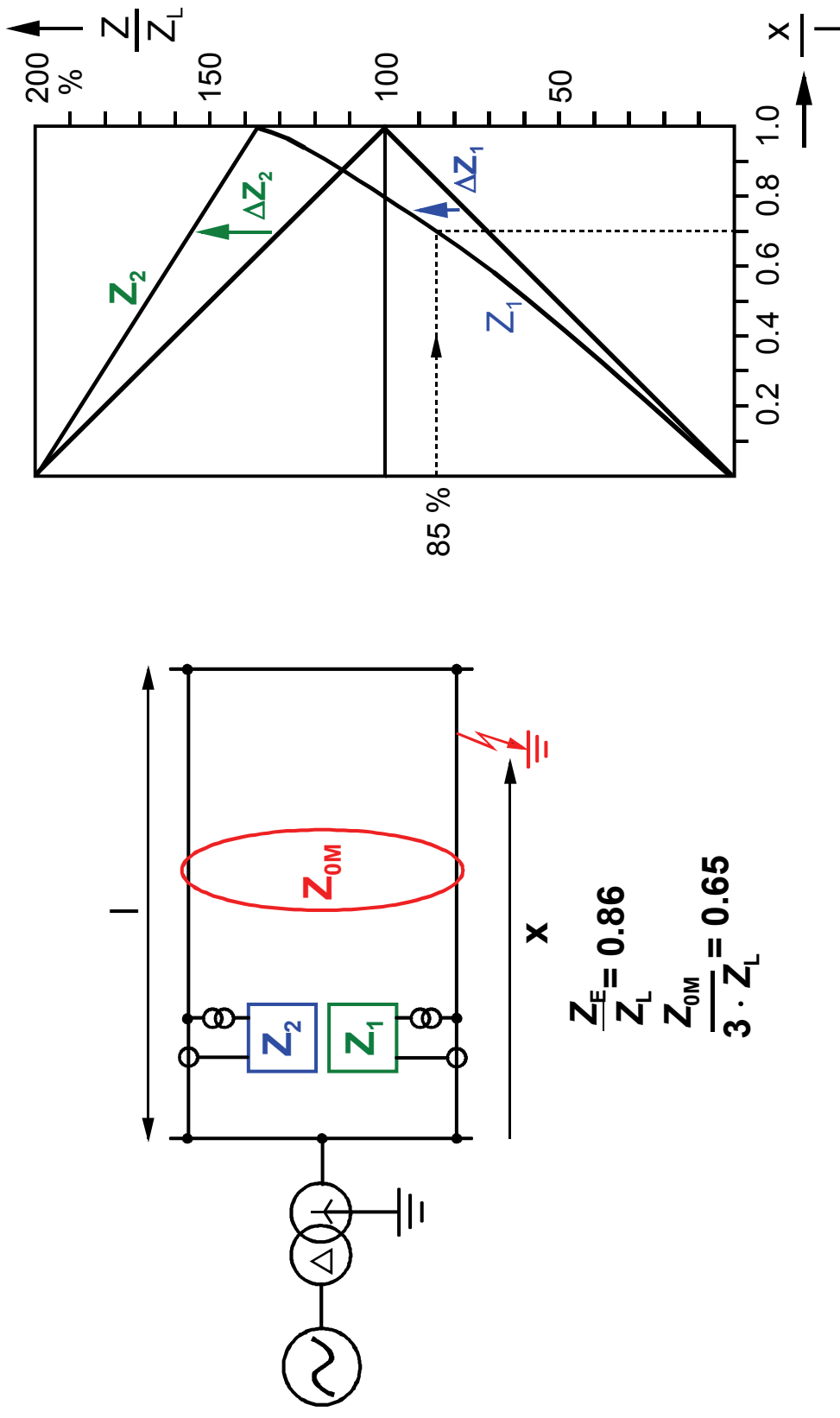
Calculated mutual reactance of two 110 kV lines

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Distance measuring error on a double-circuit line with single-ended infeed

SIEMENS



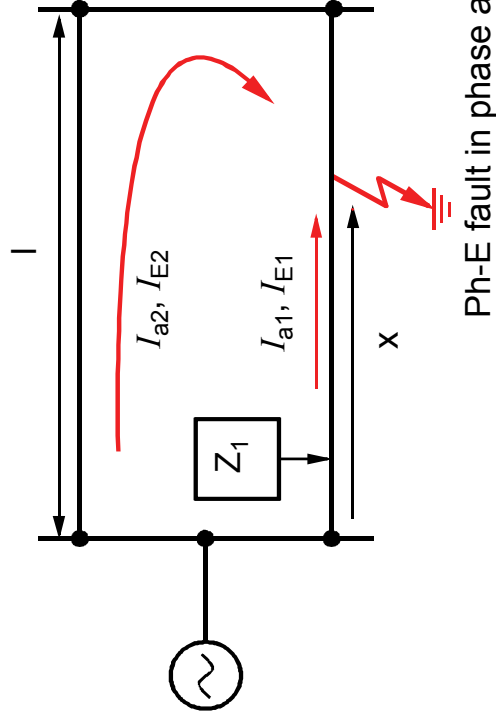
Influence of the zero sequence coupling of the parallel line (Relay on the faulted line **without** compensation)

$$Z_1 = \frac{U_a}{I_{a1} + K_{01} \cdot I_{E1}}$$

$$Z_1 = \frac{x \left[Z_L \cdot I_{a1} + Z_E \cdot I_{E1} + \frac{Z_{0M}}{3} \cdot I_{E2} \right]}{I_{a1} + \frac{Z_E}{Z_L} \cdot I_{E1}}$$

$$Z_E = \frac{Z_0 - Z_1}{3}$$

with $I_{E2} = \frac{x}{2l-x} \cdot I_{E1}$ and $I_{a1} = I_{E1}$ 



$$Z_1 = x \cdot Z_L + x \cdot Z_L \underbrace{\frac{Z_{0M}}{3 \cdot Z_L} \cdot \frac{2l-x}{1 + \frac{Z_E}{Z_L}}}_{\text{measuring error}}$$

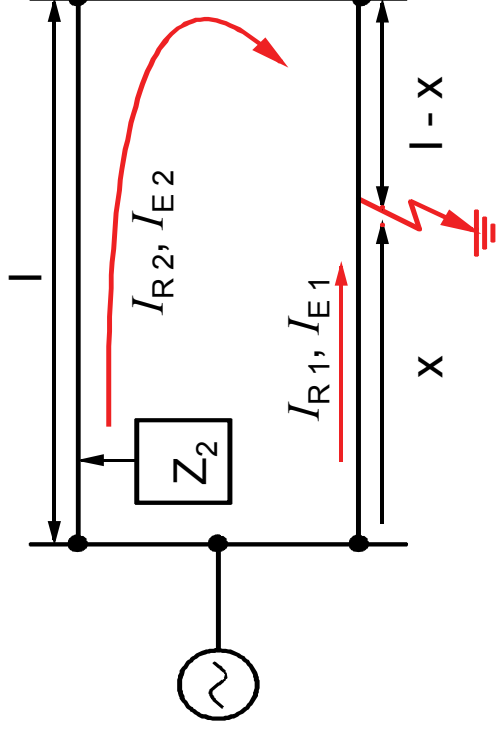
Influence of the zero sequence coupling of the parallel line (Relay on the healthy line **without** compensation)

$$Z_2 = \frac{U_R}{I_{R2} + \frac{Z_E}{Z_L} \cdot I_{E2}}$$

$$I_{R2} = I_{E2}$$

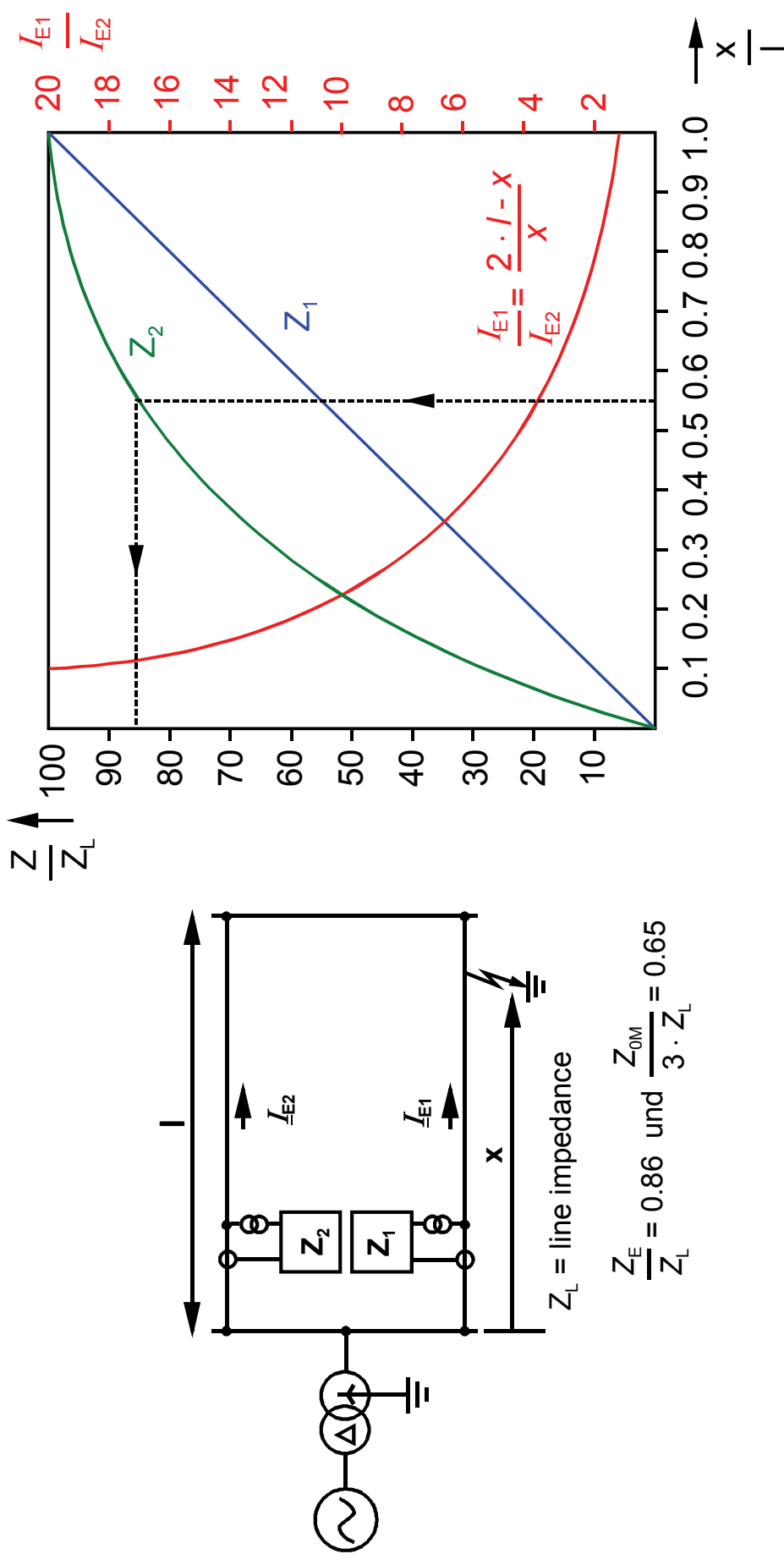
$$I_{E1} = \frac{2 \cdot l - x}{x} \cdot I_{E2}$$

$$Z_2 = Z_L \frac{(2l - x) \left(1 + \frac{Z_E}{Z_L} \right) + x \cdot \frac{Z_{0M}}{3 \cdot Z_L}}{1 + \frac{Z_E}{Z_L}}$$

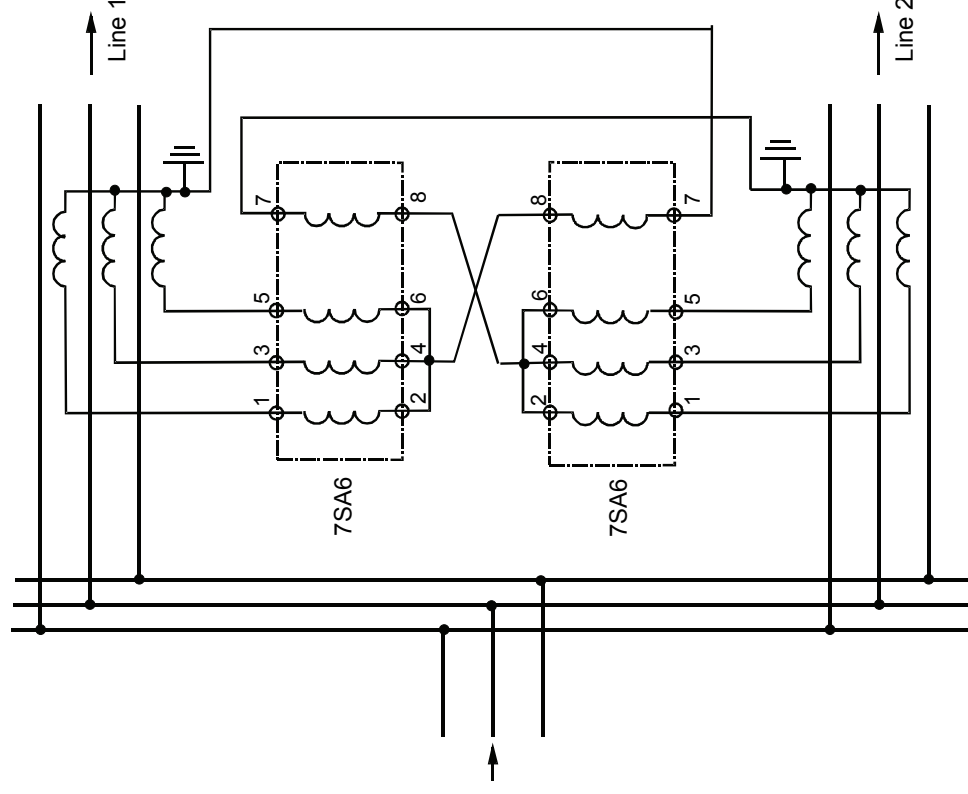


$$Z_2 = Z_L \frac{(2l - x) \left(1 + \frac{Z_E}{Z_L} \right) + x \cdot \frac{Z_{0M}}{3 \cdot Z_L}}{1 + \frac{Z_E}{Z_L}} + \underbrace{\frac{\frac{Z_E}{Z_L} \cdot \frac{Z_{0M}}{3 \cdot Z_L}}{1 + \frac{Z_E}{Z_L}}}_{\text{measuring error}}$$

Measured impedances **with** parallel line compensation



Parallel line compensation, Connection of distance relays 7SA6

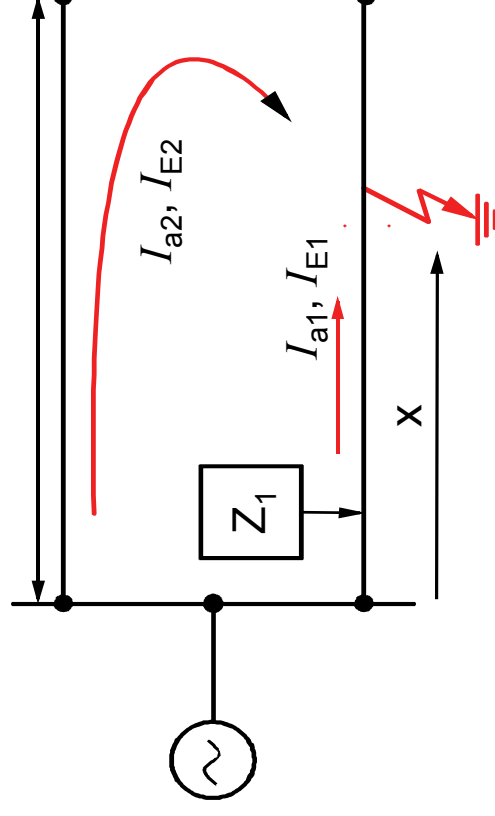


Influence of the zero sequence coupling of the parallel line (Relay on the faulted line **with** compensation)

$$Z_1 = \frac{U_R}{I_{R1} + k_{01} \cdot I_{E1} + \underbrace{k_{02} \cdot I_{E2}}_{\text{compensation}}}$$

$$k_{02} = \frac{Z_{0M}}{3 \cdot Z_L}$$

$$Z_1 = \frac{x(Z_L \cdot I_{R1} + Z_E \cdot I_{E1} + \frac{Z_{0M}}{3} \cdot I_{E2})}{I_{R1} + \frac{Z_E}{Z_L} \cdot I_{E1} + \frac{Z_{0M}}{3 \cdot Z_L} \cdot I_{E2}}$$



$$Z_1 = x \cdot Z_L \text{ (correct fault impedance)}$$

Influence of the zero sequence coupling of the parallel line (Relay on the healthy line **with** compensation)

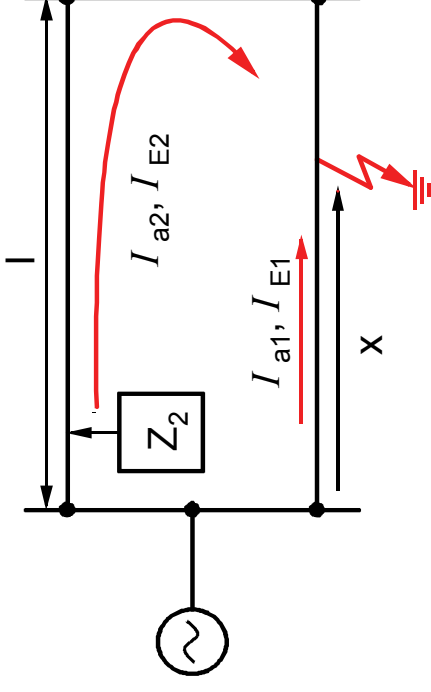
$$Z_2 = \frac{U_{R2}}{I_{R2} + \frac{Z_E}{Z_L} \cdot I_{E2} + \underbrace{\frac{Z_{OM}}{3 \cdot Z_L} \cdot I_{E1}}_{\text{compensation}}}$$

$$\text{with } I_{R2} = I_{E2} \text{ and } I_{E1} = \frac{2 \cdot l - x}{x} \cdot I_{E2}$$

$$U_{a2} = (2 \cdot l - x)(Z_L \cdot I_{a2} + Z_E \cdot I_{E2}) + x \cdot I_{E1} \cdot \frac{Z_{OM}}{3} - 2(l - x) \frac{Z_{OM}}{3} \cdot I_{E2}$$

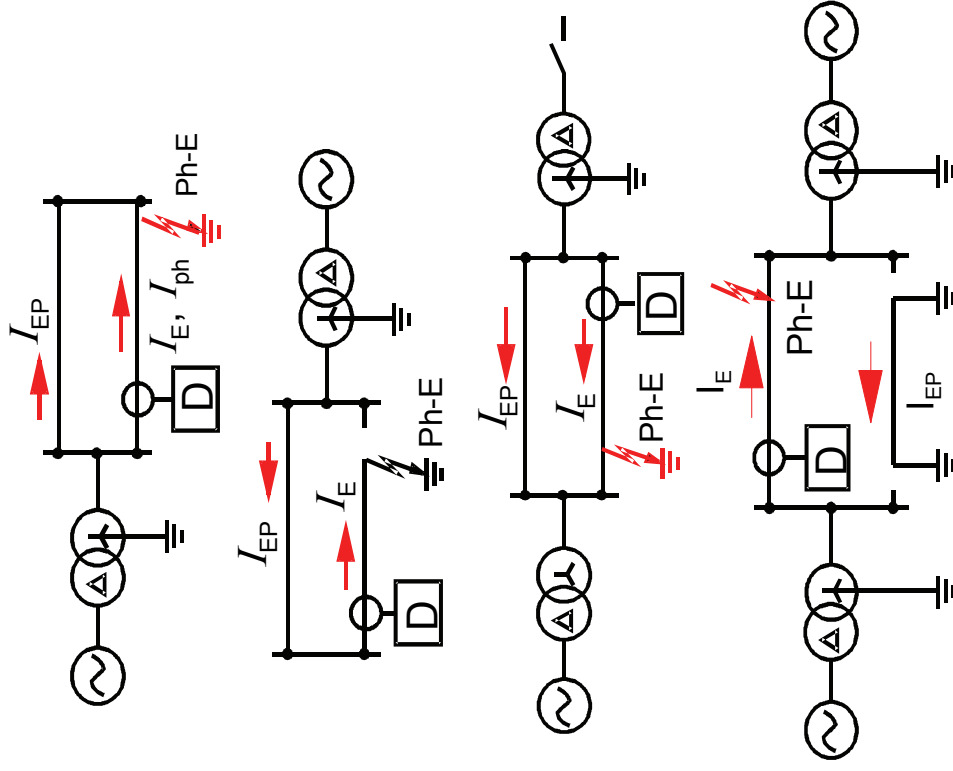
$$Z_2 = Z_L \cdot \frac{(2l - x) \left(1 + \frac{Z_E}{Z_L}\right) + x \cdot \frac{Z_{OM}}{3 \cdot Z_L}}{1 + \frac{Z_E}{Z_L} + \frac{2l - x}{x} \cdot \frac{Z_{OM}}{3 \cdot Z_L}}$$

$$Z_2 = Z_L \cdot (2 \cdot l - x) + \underbrace{\left(\frac{x}{2 \cdot l - x} - \frac{Z_{OM}}{x} \right) \cdot \frac{3 \cdot Z_L}{2l - x} \cdot Z_L \cdot (2 \cdot l - x)}_{\text{Measuring error}}$$



Distance protection on parallel lines

impedance measuring error dependent on switching condition



$$\Delta Z = \frac{k_{0M}}{1+k_0} \cdot Z_L = +39\% Z_L$$

$$\Delta Z = -\frac{k_{0M}}{1+k_0} \cdot Z_L = -39\% Z_L$$

$$\Delta Z = \frac{3 \cdot k_{0M}}{1+3 \cdot k_0} \cdot Z_L = \frac{Z_{0M}}{Z_{0L}} = +65\% Z_L$$

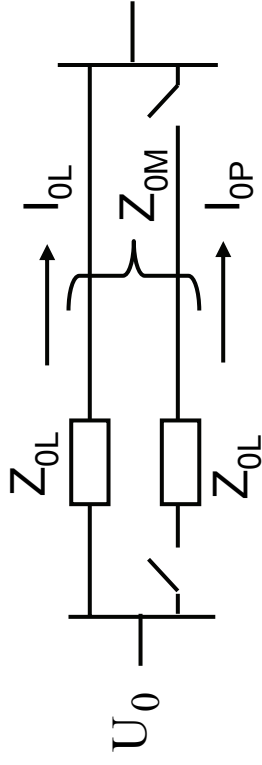
$$\Delta Z = -\frac{k_{0M} \cdot \frac{Z_{0M}}{Z_{0L}}}{1+k_0} \cdot Z_L = -\frac{Z_{0M}}{Z_{0L}} = -25\% Z_L$$

$$(k_0=0.71, k_{0M}=0.67 \text{ and } Z_{0M}/Z_{0L} = 0.65)$$

Parallel line

Earth current compensation factor k_0 dependent on switching state

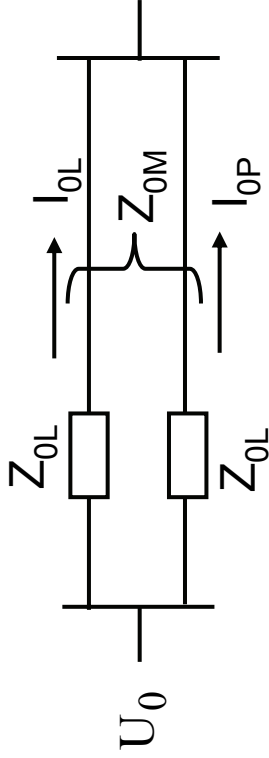
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Example: $K_0 = 0.71$, $K_{0M} = 0.67$, $Z_{0M}/Z_{0L} = 0.65$

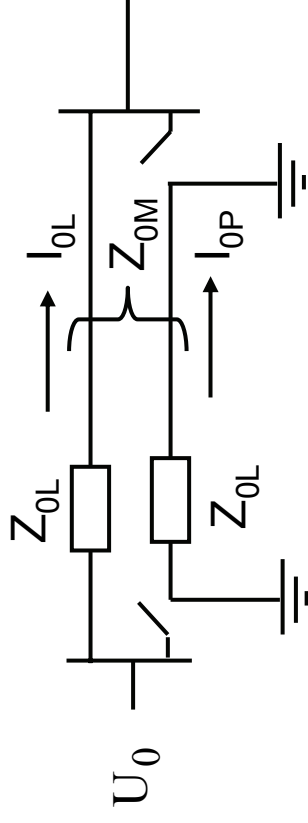
$$I_{0P} = 0 \quad Z_0^* = \frac{U_{0L}}{I_{0L}} = Z_{0L}$$

$$k_0 = \frac{Z_E}{Z_L} = \frac{(Z_{0L} - Z_{1L})/3}{Z_{1L}} = 0.71$$



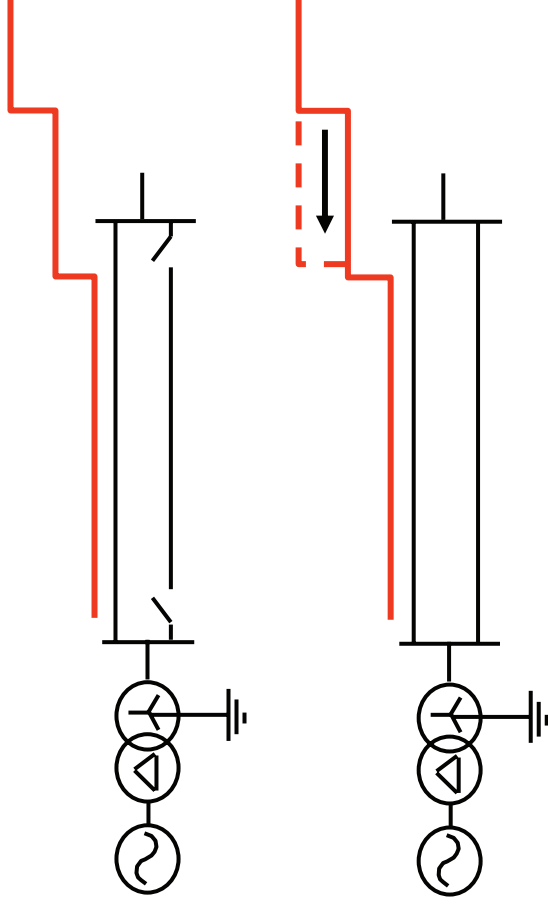
$$I_{0P} = I_{0L} \quad Z_0^* = \frac{U_{0L}}{I_{0L}} = Z_{0L} + Z_{0M}$$

$$k_0^* = \frac{(Z_0 - Z_{1L})/3}{Z_{1L}} + \frac{Z_{0M}/3}{Z_{1L}} = k_0 + k_{0M} = 1.38$$



$$I_{0P} = -\frac{Z_{0M}}{Z_{0P}} \cdot I_{0L} \quad Z_0^{**} = \frac{U_{0L}}{I_{0L}} = Z_{0L} - \frac{Z_{0M}^2}{Z_{0L}}$$

$$k_0^{**} = \frac{Z_{0L} - Z_{1L}}{3 \cdot Z_{1L}} - \frac{Z_{0M}}{Z_{0L}} \cdot \frac{Z_{0M}}{3 \cdot Z_{1L}} = k_0 - \frac{Z_{0M}}{Z_{0L}} \cdot k_{0M} = 0.27$$



Zone setting based on Ph-Ph-Faults:

$$Z_2 = 1.2 \cdot Z_L$$

$k_0 = Z_E / Z_L$ of single line

Zone reach for Ph-E faults:

$$Z_2 = 1.2 \cdot Z_L \cdot \frac{1 + k_0}{1 + k_0 + k_{0M}}$$

$$= \frac{1 + 0.71}{1 + 0.71 + 0.67} \cdot 1.2 \cdot Z_L = 0.86 \cdot Z_L$$

120% Overreach of 2nd zone for earth faults would require a zone setting of

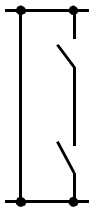
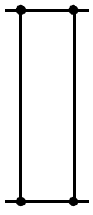
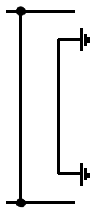
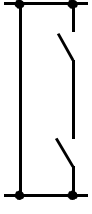
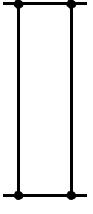
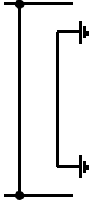
$$Z_2 = 1.2 \cdot Z_L \cdot \frac{1 + k_0 + k_{0M}}{1 + k_0} = 1.2 \cdot Z_L \cdot \frac{1 + 0.71 + 0.67}{1 + 0.71} = 1.67 \cdot Z_L$$

Use  separate k_0 factor for overreaching zones

 or parallel line compensation

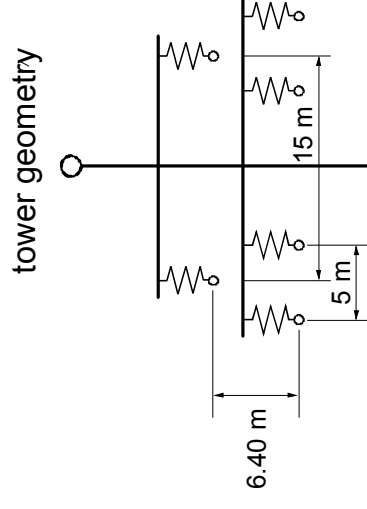
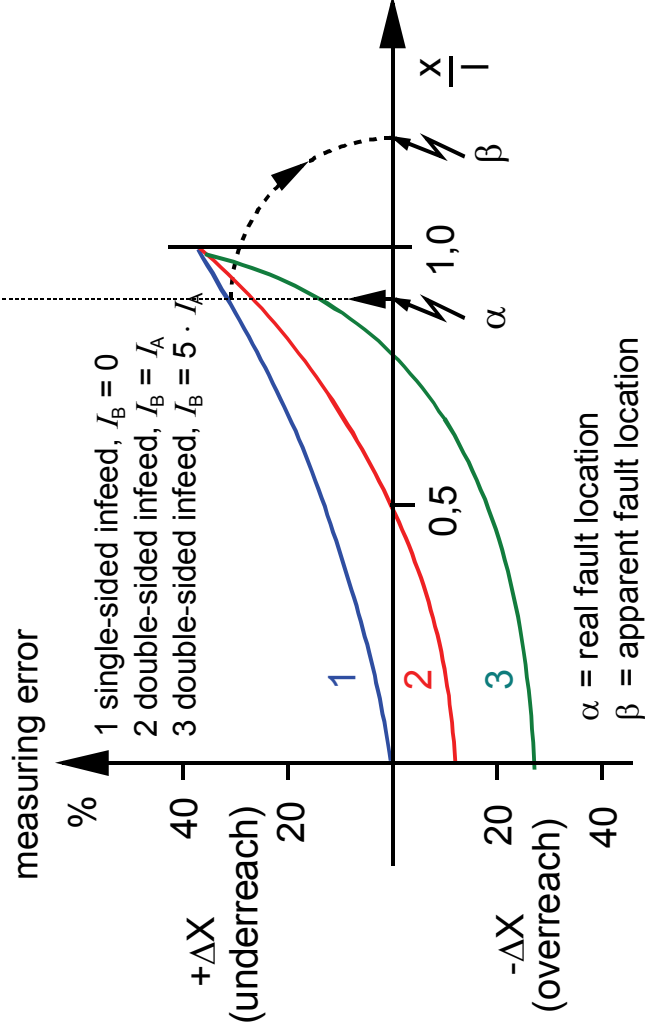
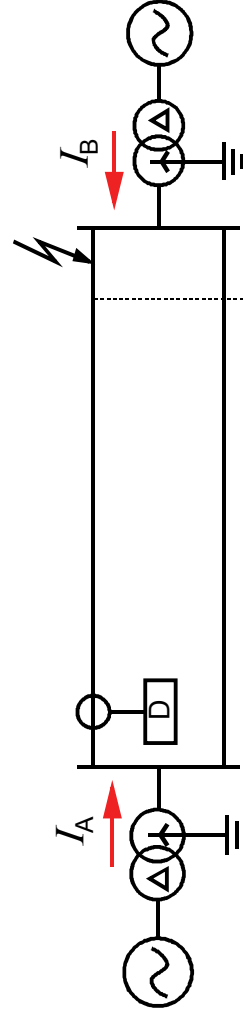
Distance measurement on parallel lines

Zone reach dependent on switching state and relay k_0 -setting

		Zone reach in % line length dependent on switching state		
				
Setting to 85% line length for switching state:	 $K_0 = 0.71(0.5)$	85% (75%)	71% (64%)	108% (98%)
	 $K_0 = 1.59$	108%	85%	132%
	 $K_0 = 0.27$	65%	56%	85%

Example: 400kV-line: $K_0 = 0.71$, $K_{0M} = 0.67$, $Z_{0M}/Z_{0L} = 0.65$

Ph-to-E fault on a double circuit line with double-sided in-feed, measuring error due to parallel line coupling

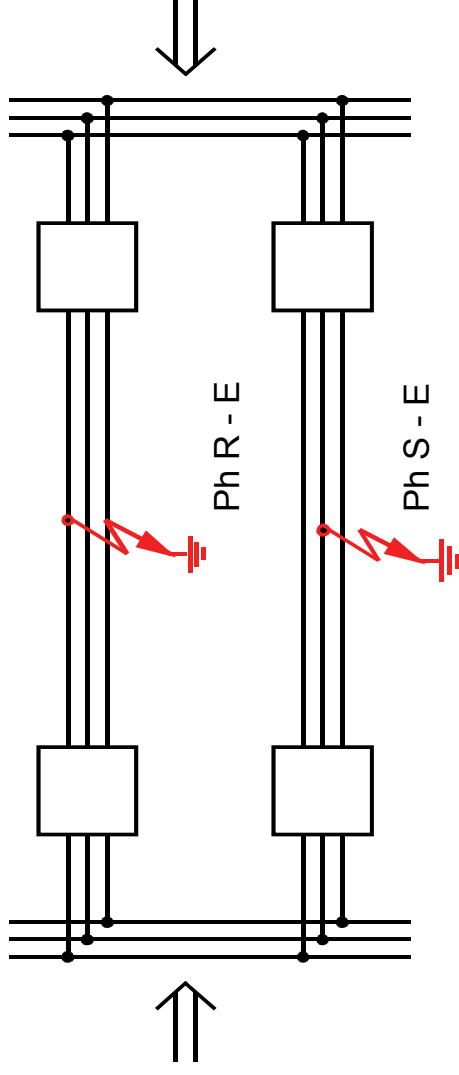


phase conductors: St Al 340/110 mm²
earth-wire: St 70 mm²

$$\frac{Z_E}{Z_L} = 0,84$$

$$\frac{Z_{OM}}{3 \cdot Z_L} = 0,68$$

Protection in case of cross country faults

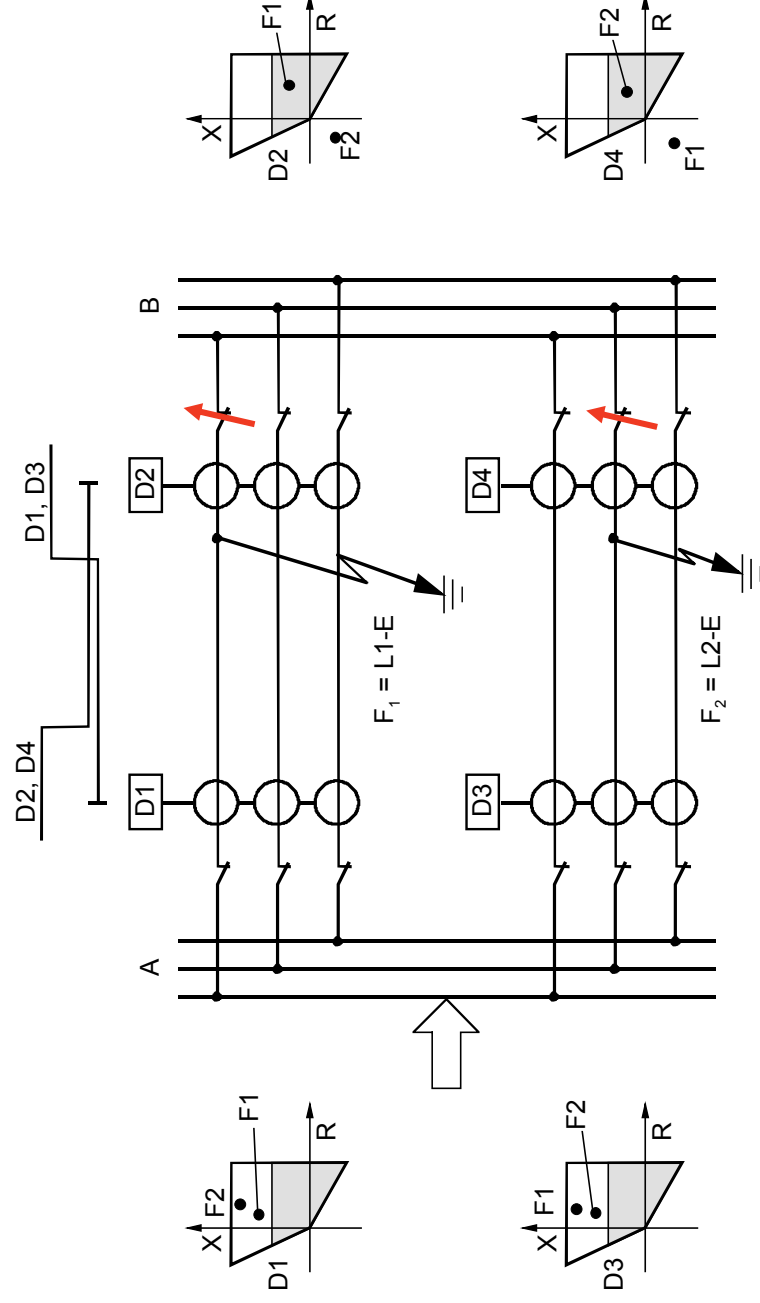


Selective fault clearance in combination with single-pole auto-reclosure requires phase segregated protection:

- | | | |
|---|---|--|
| - Differential | } | per phase |
| - Phase comparison | | |
| - distance relaying using communication | } | Directional comparison per phase or permissive intertripping per phase phase |

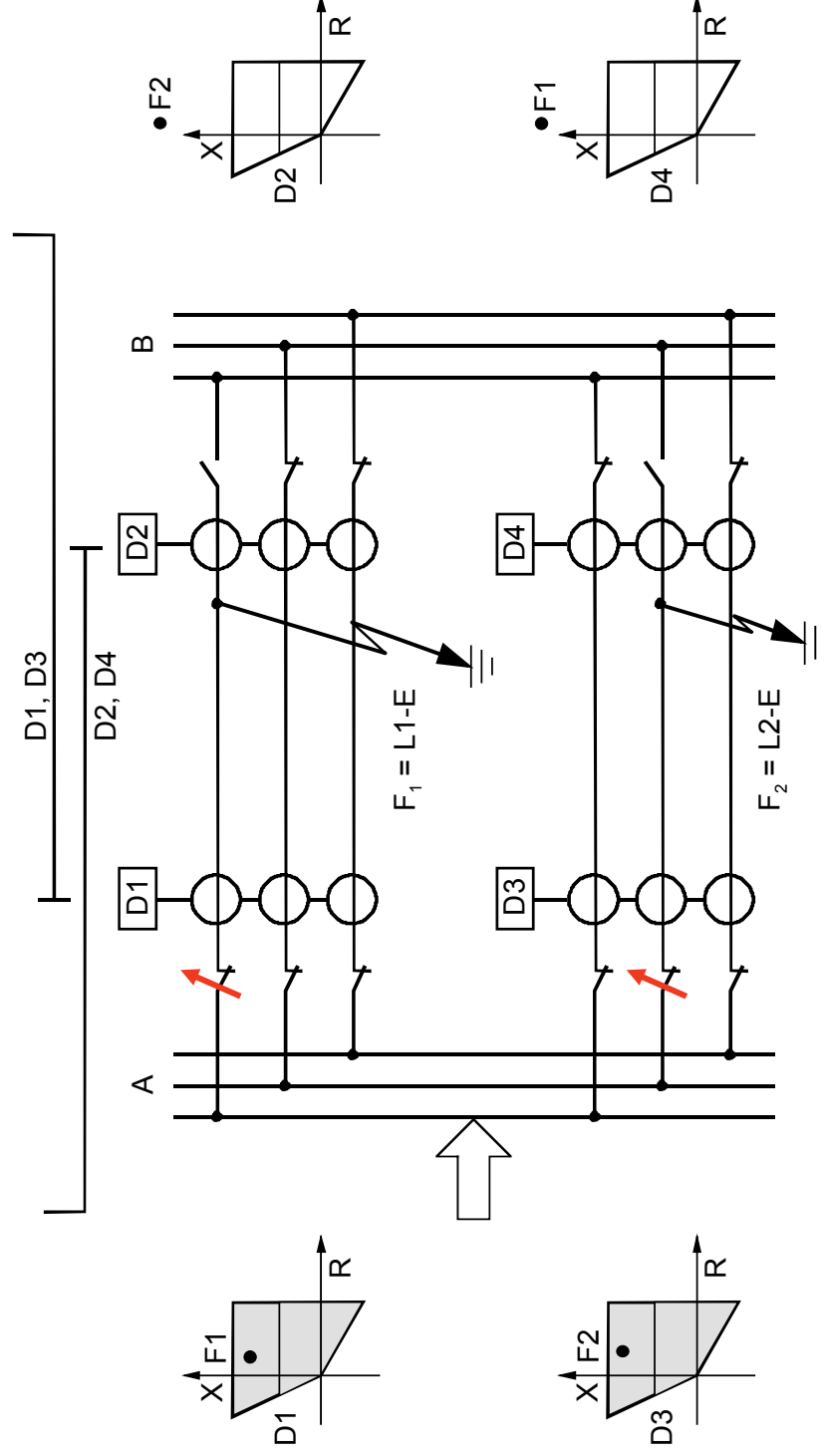
Double-circuit line, distance protection using zone extension with single-phase faults only and single-pole ARC (1)

At fault inception: Multiple-phase fault detection, underreaching zones active
D2 und D4 detect single phase faults and trip single-phase each at their side.



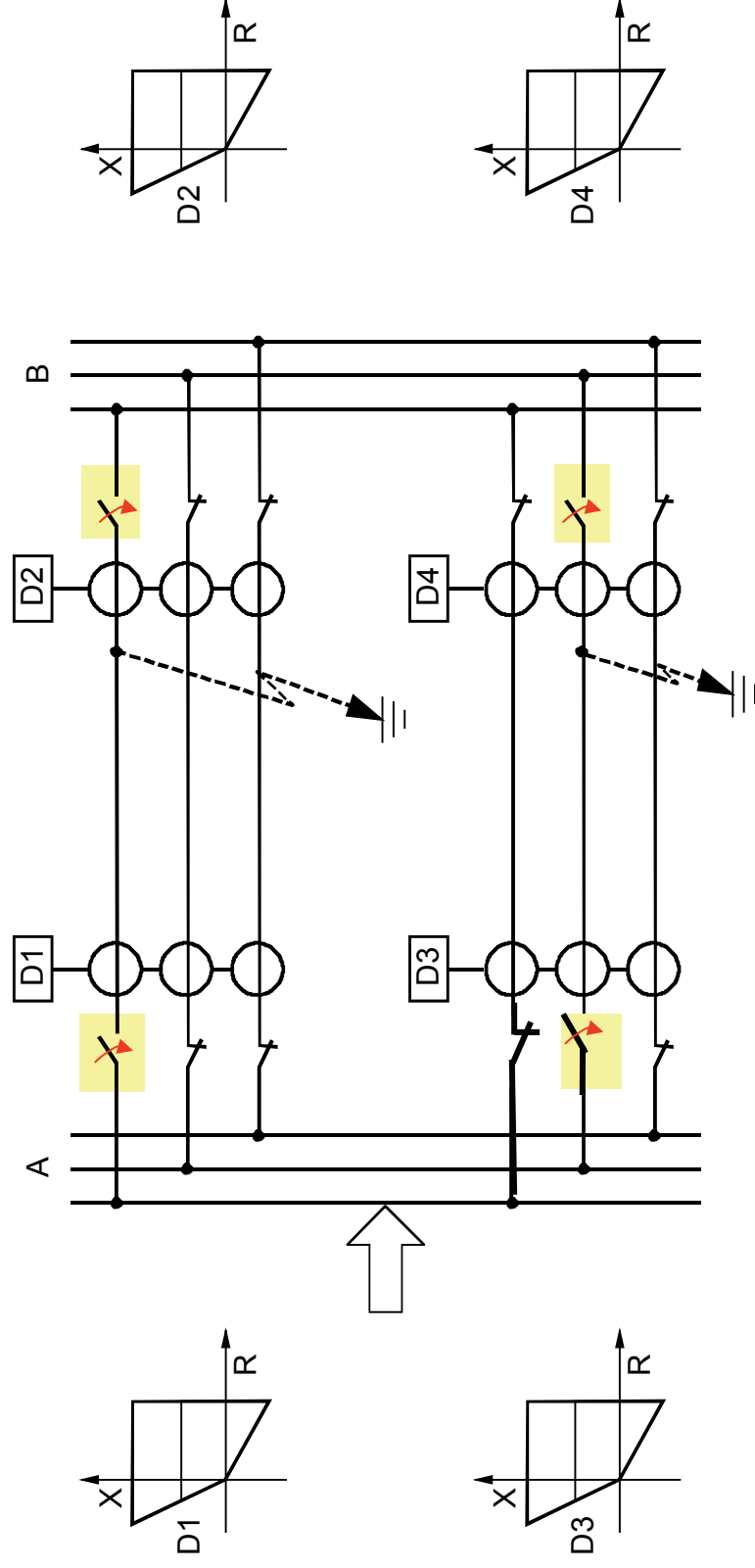
Double-circuit line, distance protection using zone extension with single-phase faults only and single-pole ARC (2)

After single-pole tripping in B: Relays D1 und D3 in A change to single phase fault detection, extend zones to overreach and also trip single phase (cascaded tripping).

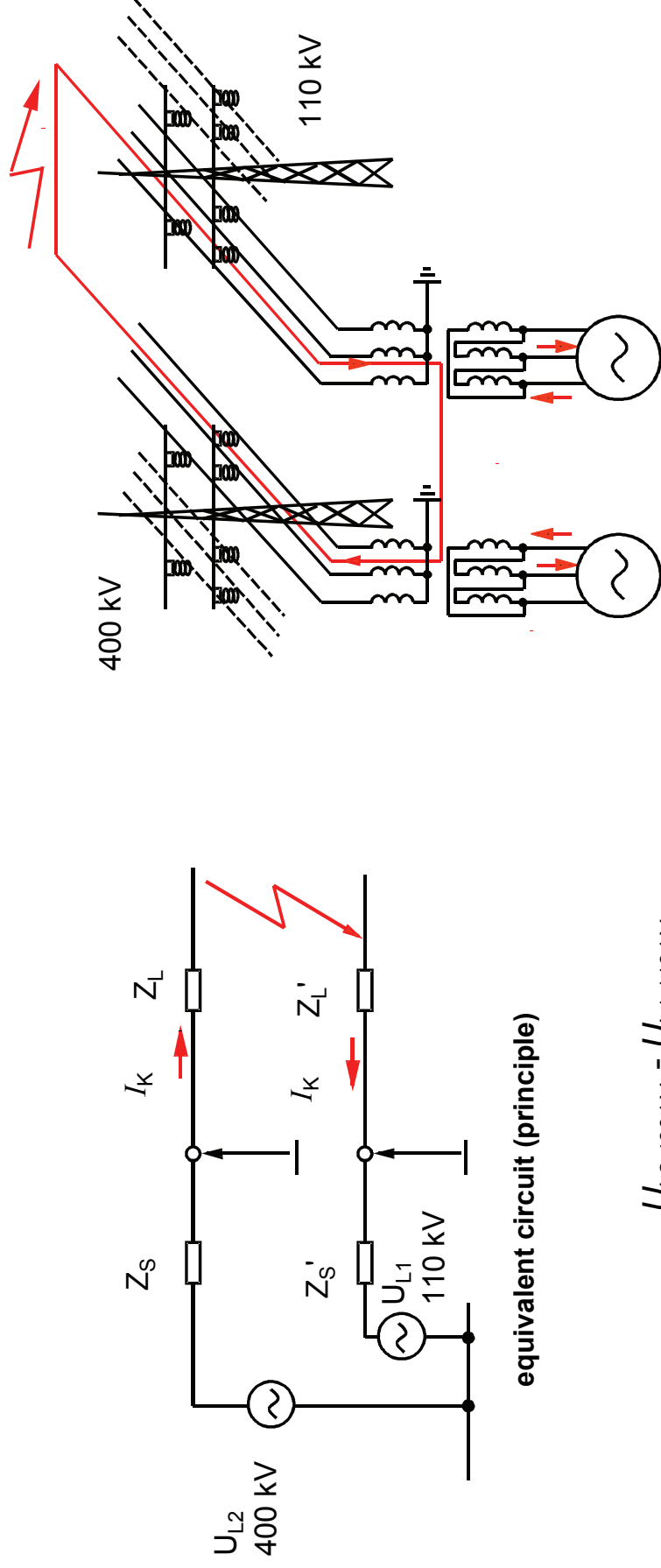


Double-circuit line, distance protection using zone extension with single-phase faults only and single-pole ARC (3)

Fault now selectively cleared, one complete three-phase system remains in service
Auto-reclosure at all 4 line ends and full system recovery after single-pole dead time.



Inter-circuit faults, z.B. 400/110kV



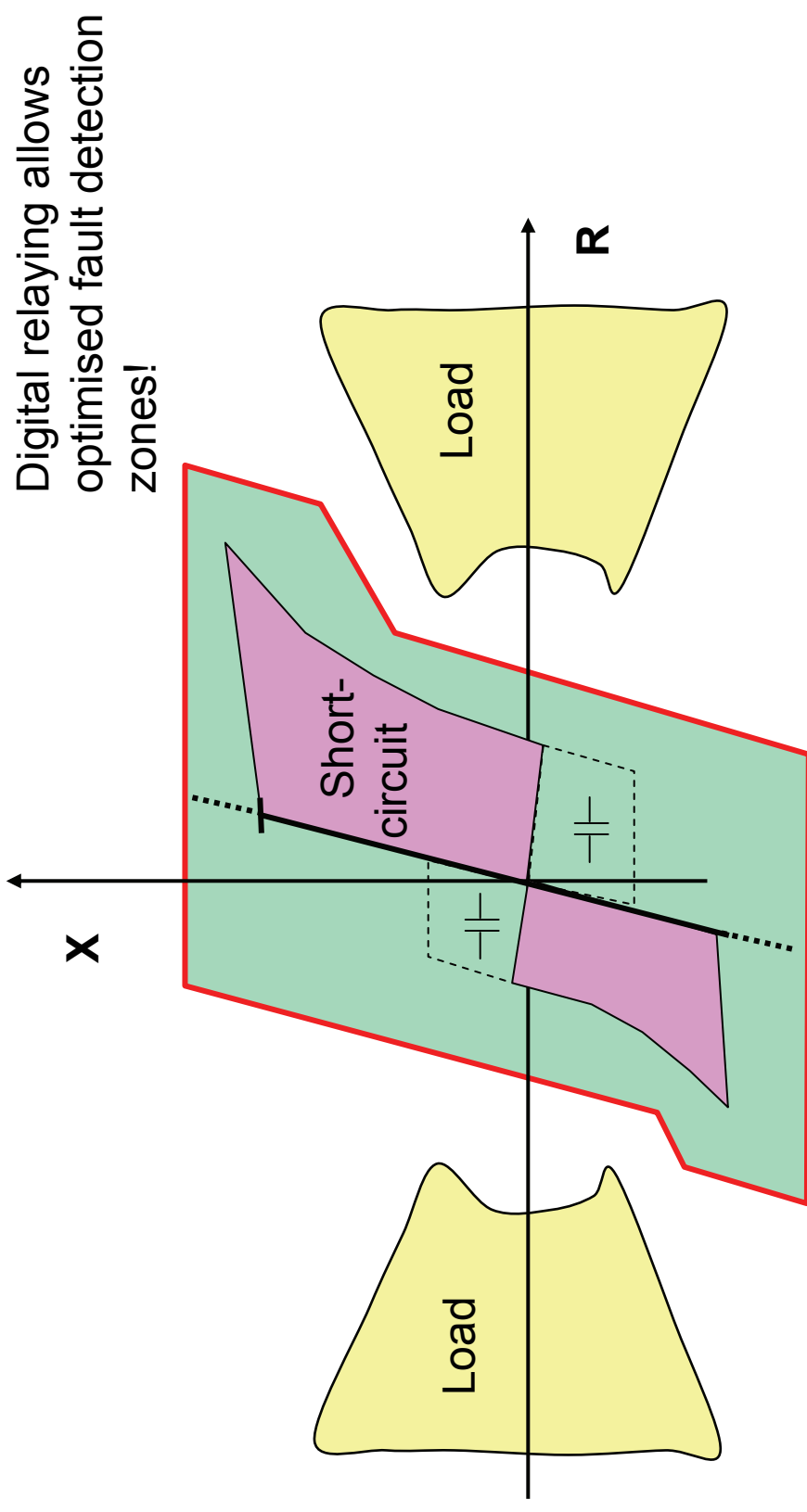
Power swing

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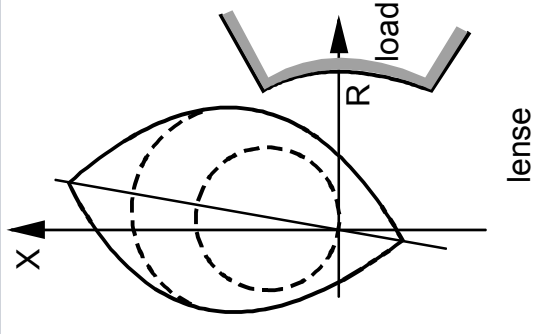
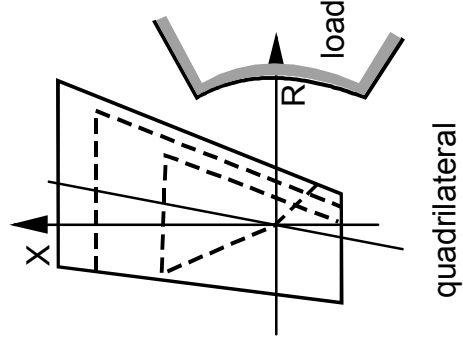
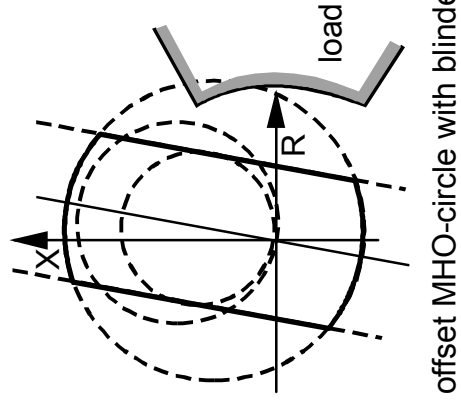
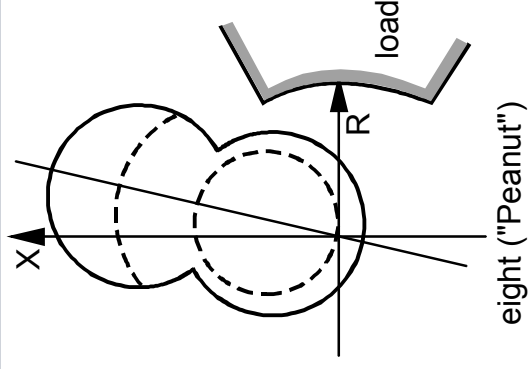
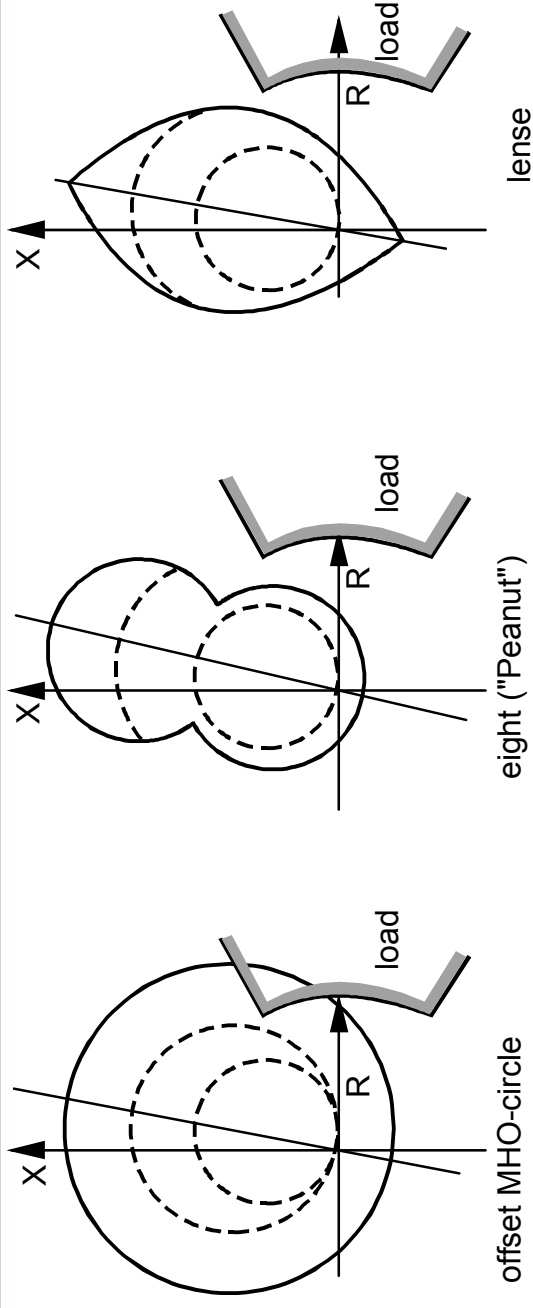


© Siemens AG 2006

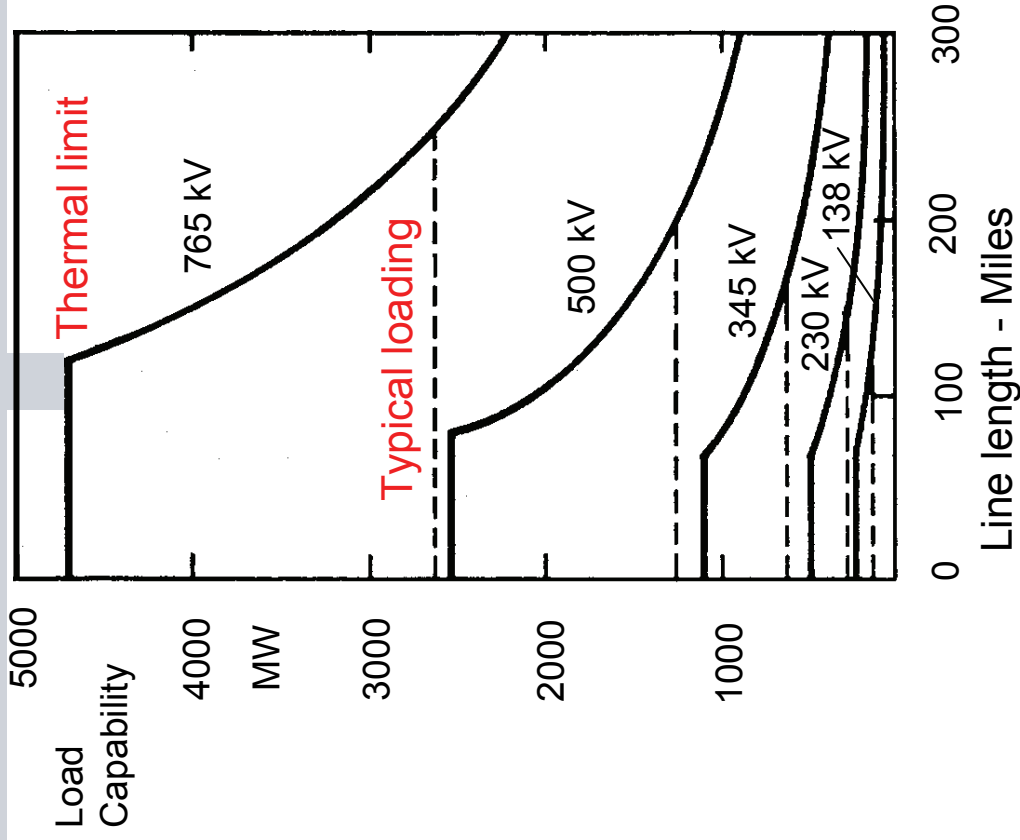
Fault versus load discrimination



Traditional shape of fault detector zones



Transmission line load capability

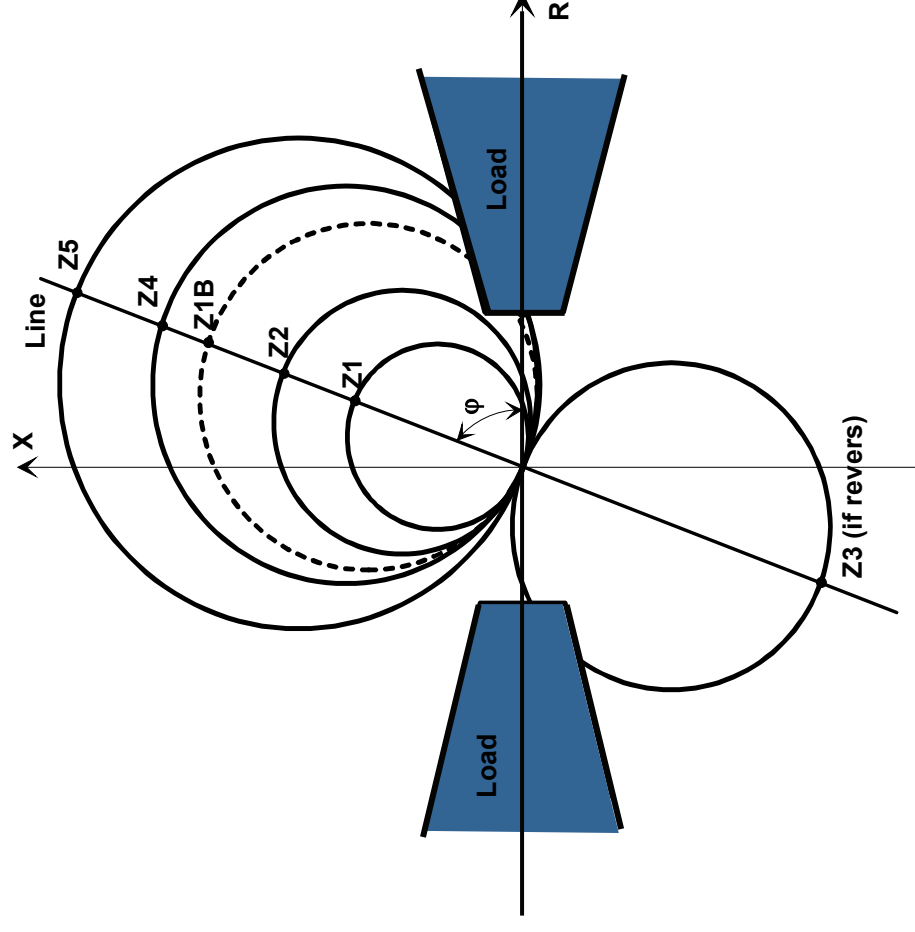
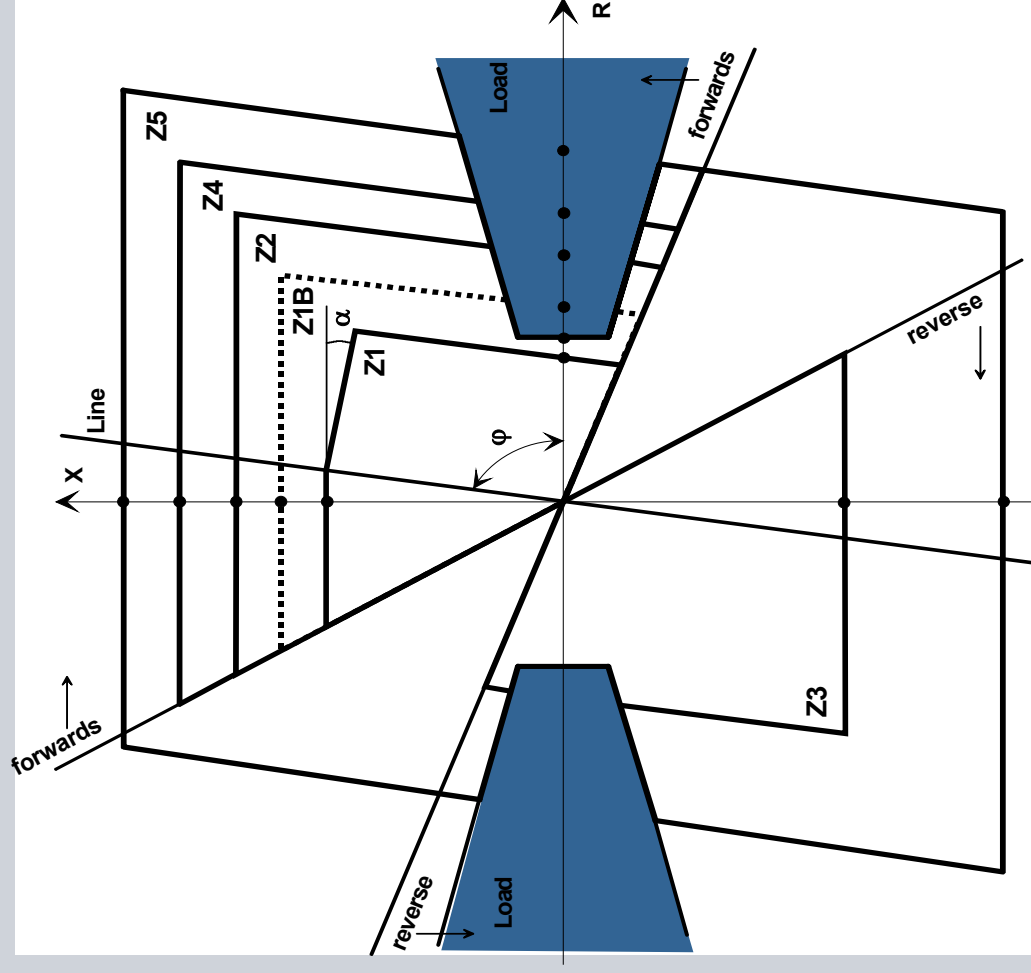


Typical Line Capabilities (about natural load):

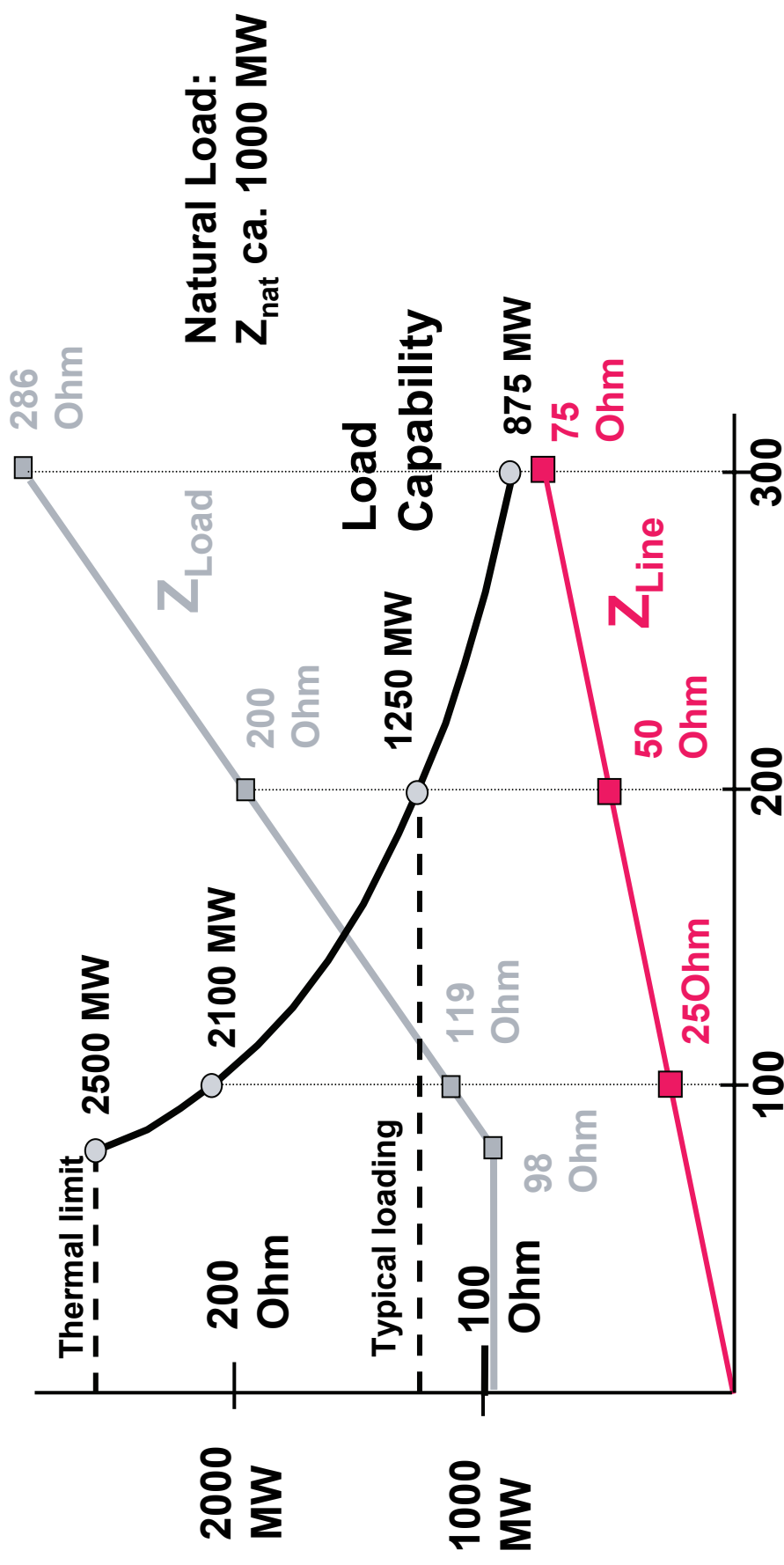
Voltage	Capability	Load	Impedance
138 kV	100 MW		190 Ohm
230 kV	250 MW		212 Ohm
345 kV	600 MW		198 Ohm
500 kV	1200 MW		208 Ohm
765 kV	2500 MW		234 Ohm

Digital operating characteristics with load blocking area (selectable with relays 7SA522 and 7SA6)

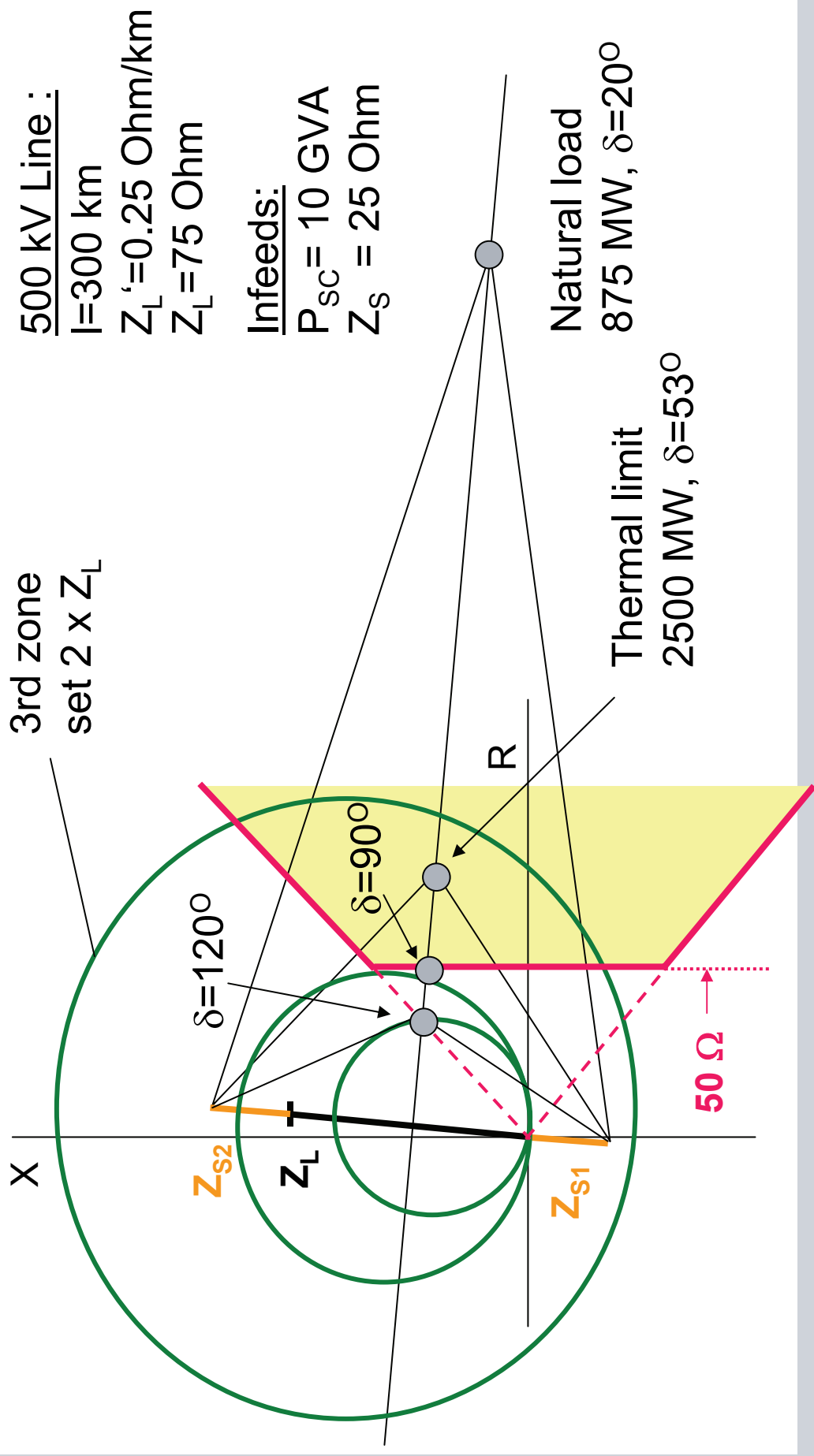
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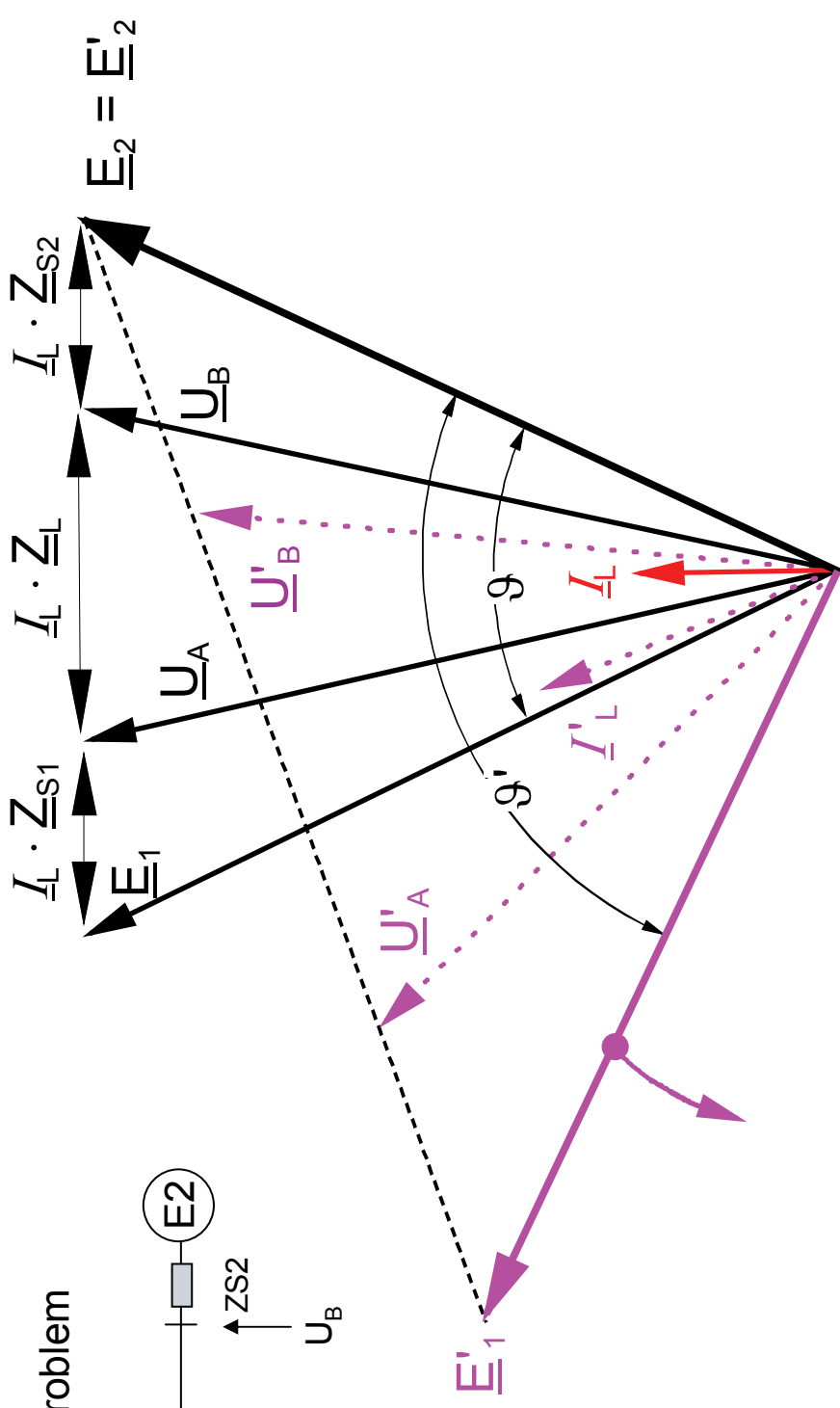
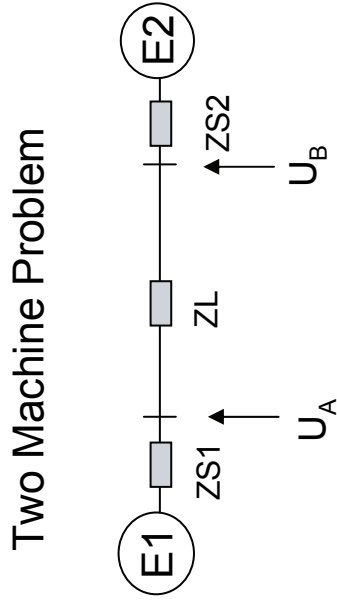
Transmission lines, Load and fault data



Setting of load blocking area

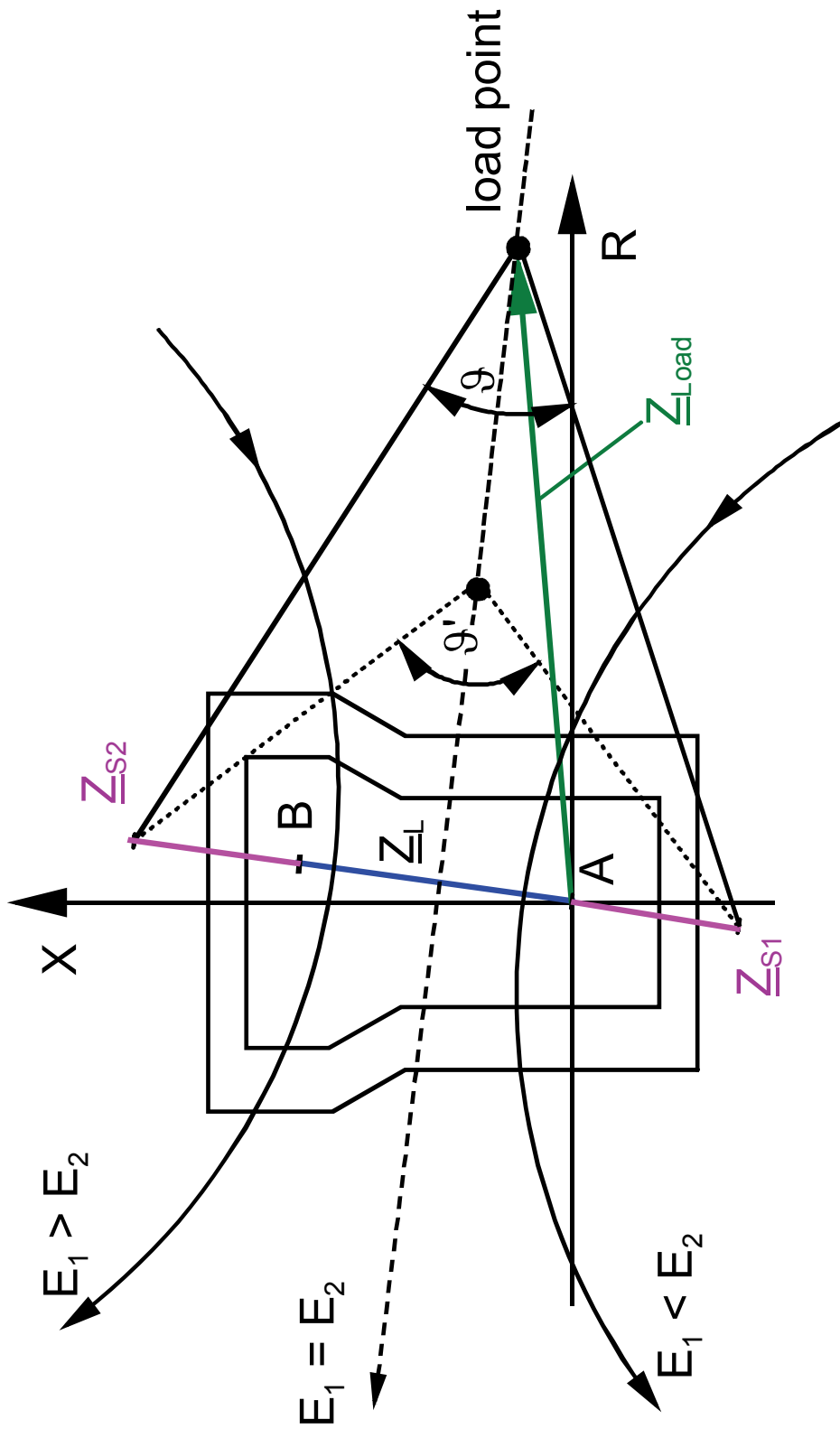


Power swing: Voltage diagram

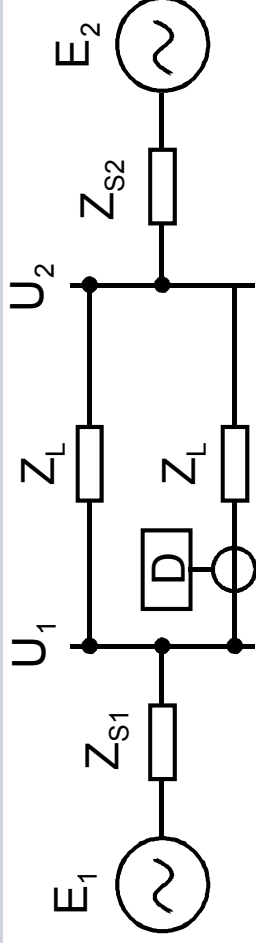


If the angle becomes too large, the system stability can be lost

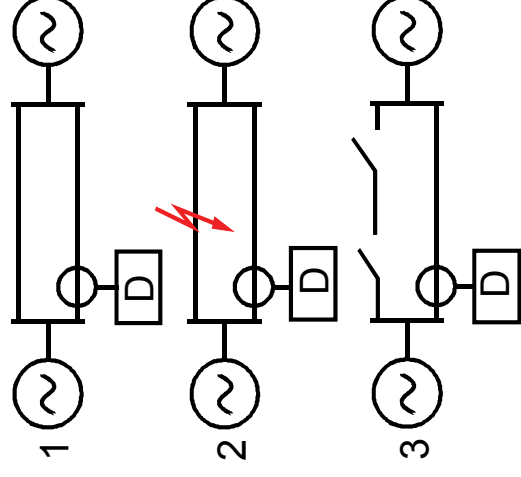
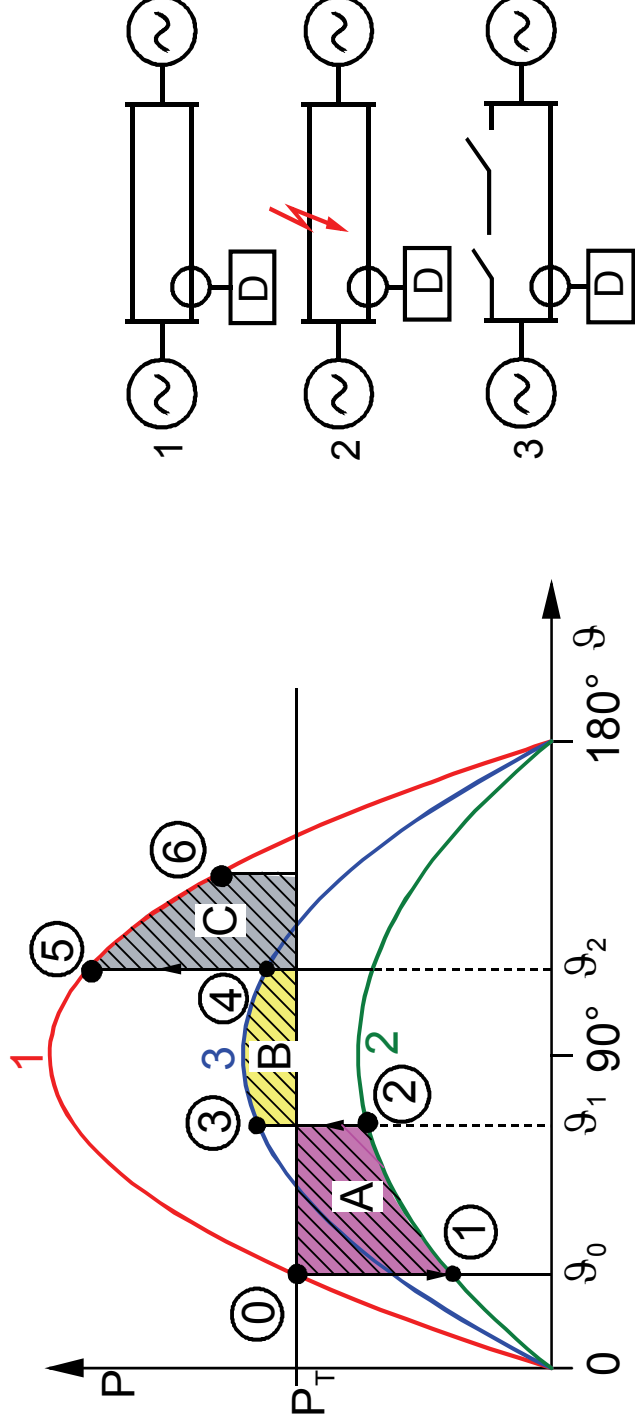
Power swing locus and relay characteristic in the impedance diagram



Dynamic system stability, equal area criterion

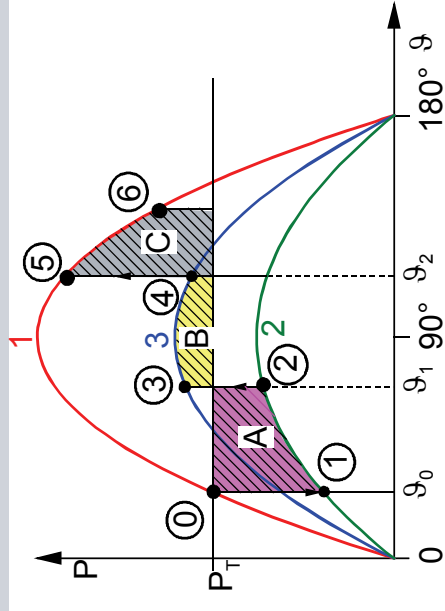
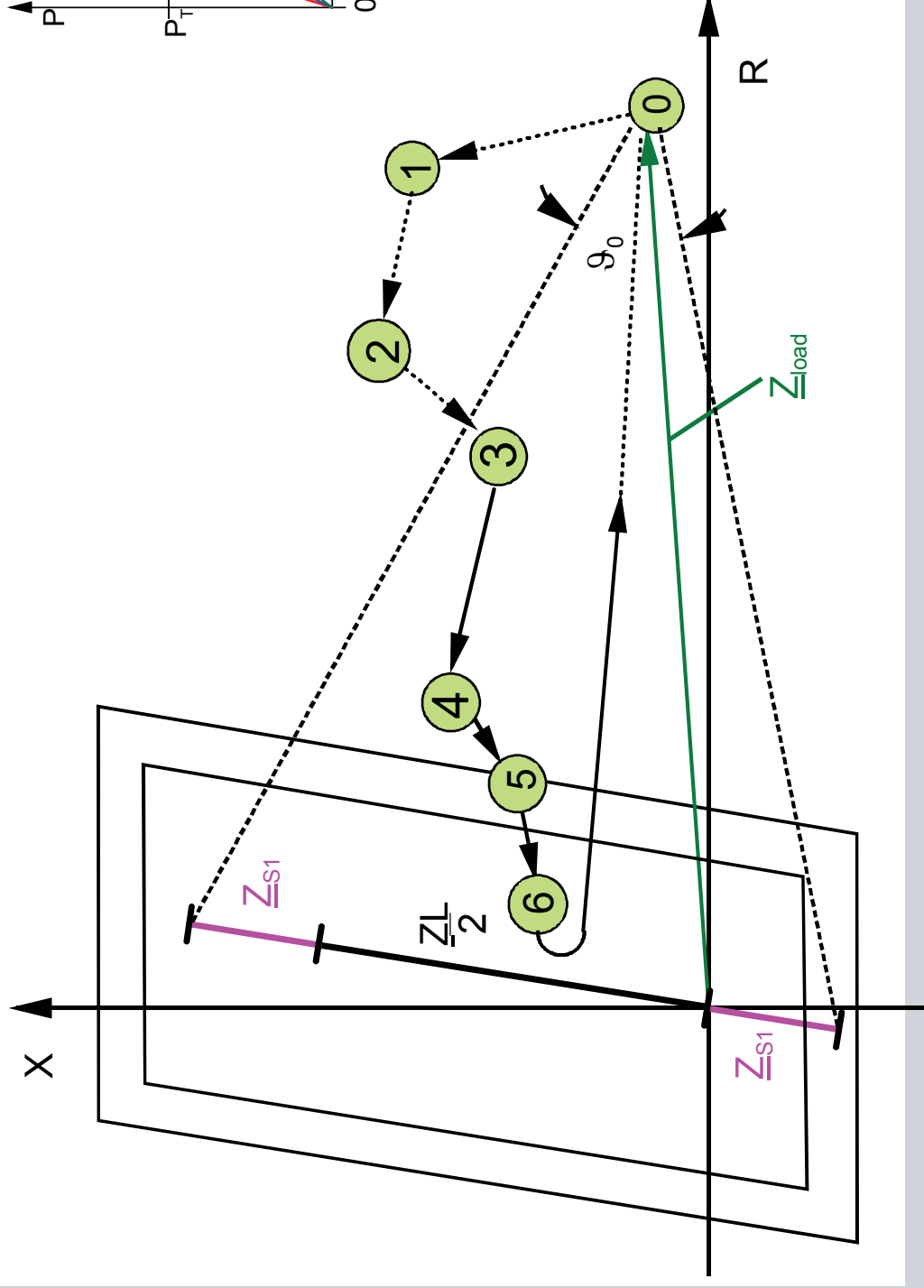


$$P_{TP} = \frac{E_1 \cdot E_2}{X_T} \cdot \sin \vartheta$$



Power swing locus in the impedance plane

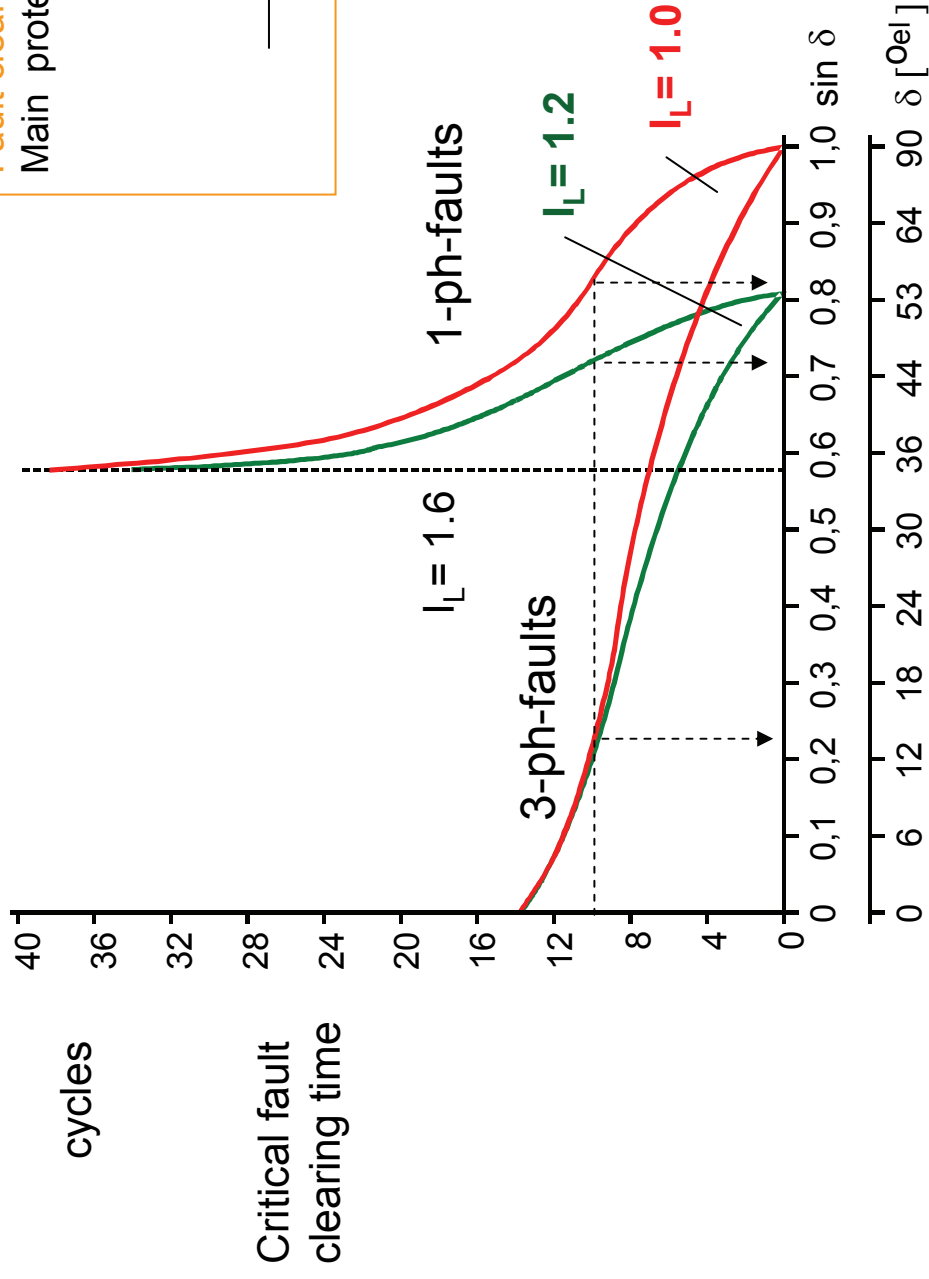
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Critical fault clearing time

Fault clearing times:

Main protection (85% of line):	1 cycle
CB:	2 cycles
BF:	4 cycles
CB:	2 cycles
Total:	9 cycles



Independent tripping of CB poles required!

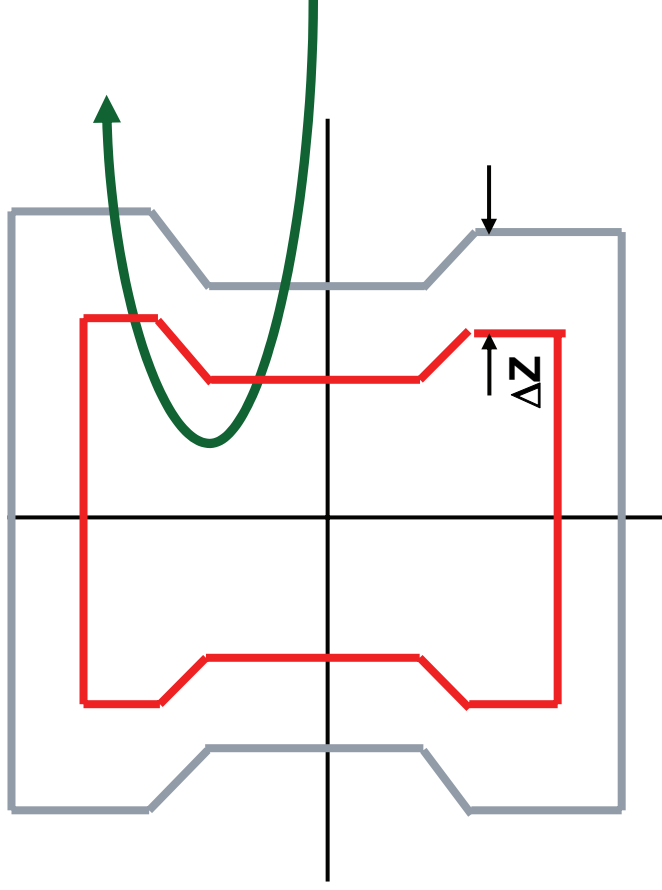
δ = transmission angle before fault inception

Requirements on power swing protection

- ◆ Must prevent overfunction of distance protection during power swing up to high slip frequencies where necessary, say at least 5 Hz
- ◆ Shall maintain function also during single-pole open condition (auto-reclosure dead time)
- ◆ Must trip on all kind of internal faults (also 3-phase) occurring during power swing (release of blocking)
- ◆ Should be setting free, without complex setting calculations
- ◆ Shall need minimum ΔZ distance, to allow high fault resistance coverage and at high load

Power swing detection: Classic method (Not used in 7SA52 and 7SA6)

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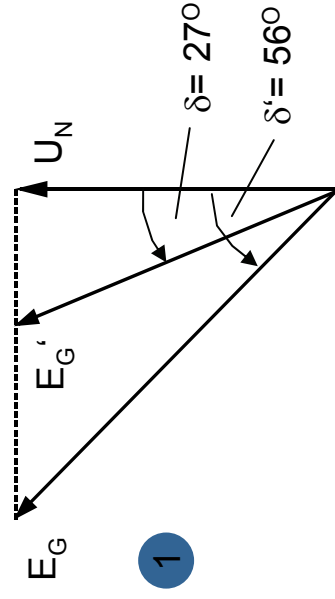
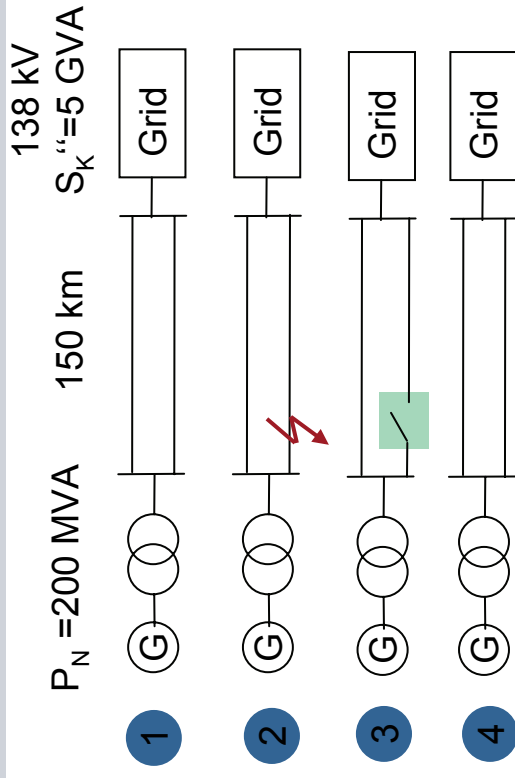
Classic power swing detection is restricted to slow swings

The setting of ΔZ may not be too large to avoid load encroachment (typ. 5Ω)

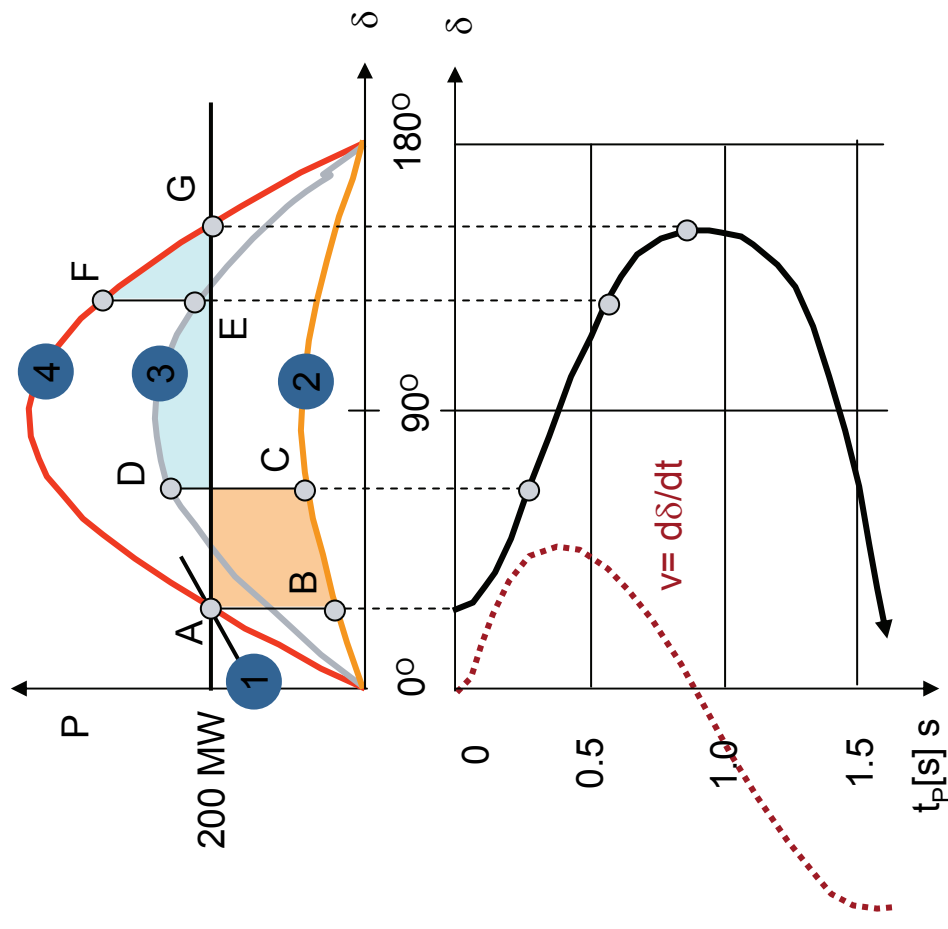
During fast swings the time available (Δt) for detection of impedance vector in the power swing zone is too short.

Δt = time for transition of Z from outer to inner zone

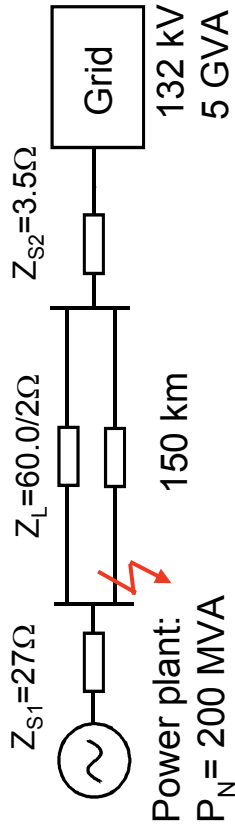
Power swing after 3-ph fault clearing with ARC



Steady-state condition before fault inception



Setting of traditional power swing blocking



Maximum swing frequency assumed: 2 Hz

Maximum Load angle: $\delta = 60^{\circ}_{\text{Oel}}$ (emergency case)

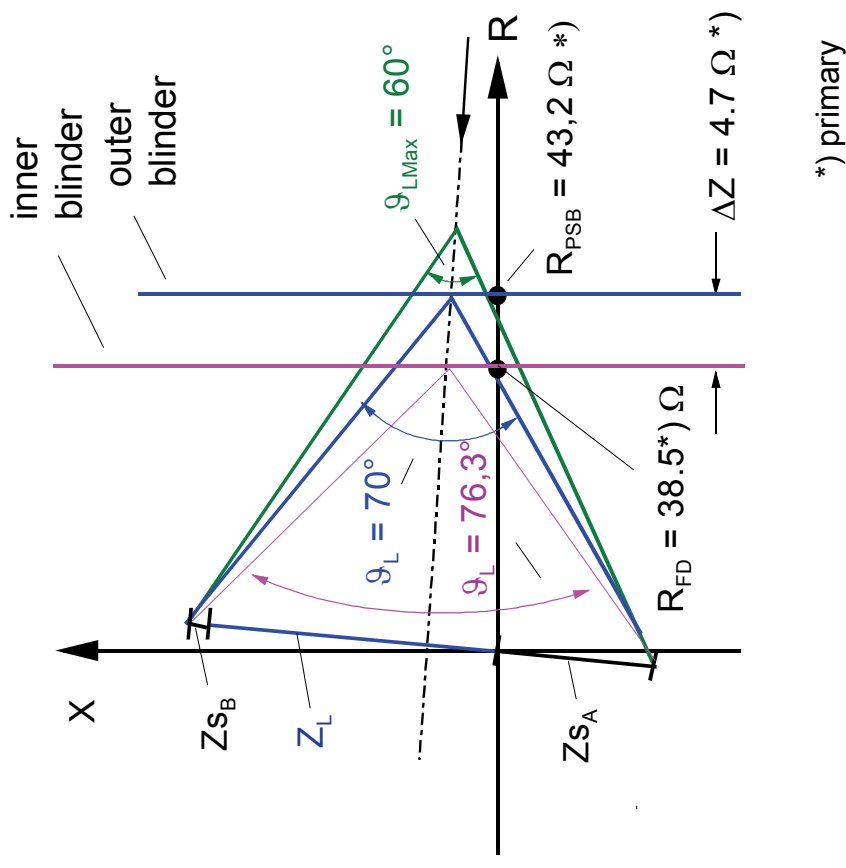
Outer blinder set to $\delta = 70^{\circ}_{\text{Oel}}$ (10° security margin)

$$R_{\text{PSB}} \approx \frac{Z_{\Sigma}}{2} \cdot \cot\left(\frac{\delta}{2}\right) = \frac{60.5}{2} \cdot \cot\left(\frac{70}{2}\right) = 43.2 \Omega_{\text{prim.}}$$

$$\begin{aligned} \frac{dR_{\text{PSB}}}{dt} &\approx \frac{\pi}{2} \cdot Z_{\Sigma} \cdot f_p \cdot \text{tg}\left(\frac{g}{2}\right) \\ &= \frac{\pi}{2} \cdot 60.5 \Omega \cdot 2.0 \frac{1}{s} \cdot \tan\left(\frac{70}{2}\right) = 133 \left[\frac{\Omega_{\text{prim.}}}{s} \right] \end{aligned}$$

Relay requirement for PSB detection: $\Delta T \geq 35 \text{ ms}$

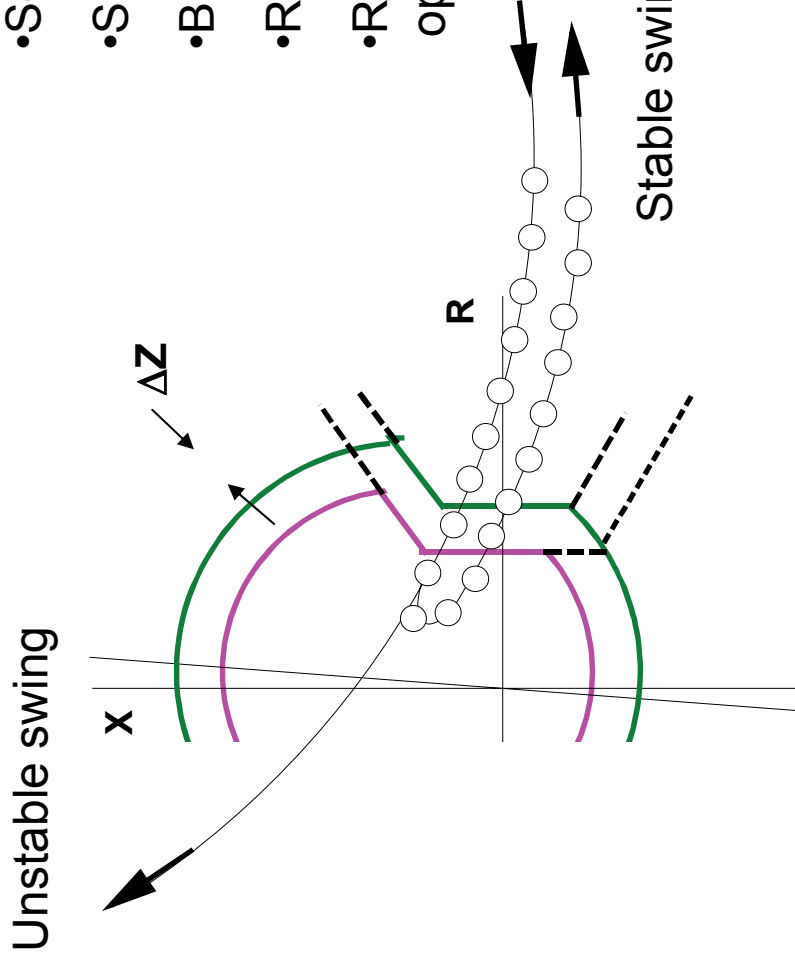
$$\Delta Z \geq 0.035 \cdot \frac{dR}{dt} = 0.035 \cdot 133 = 4.7 \Omega_{\text{prim.}}$$



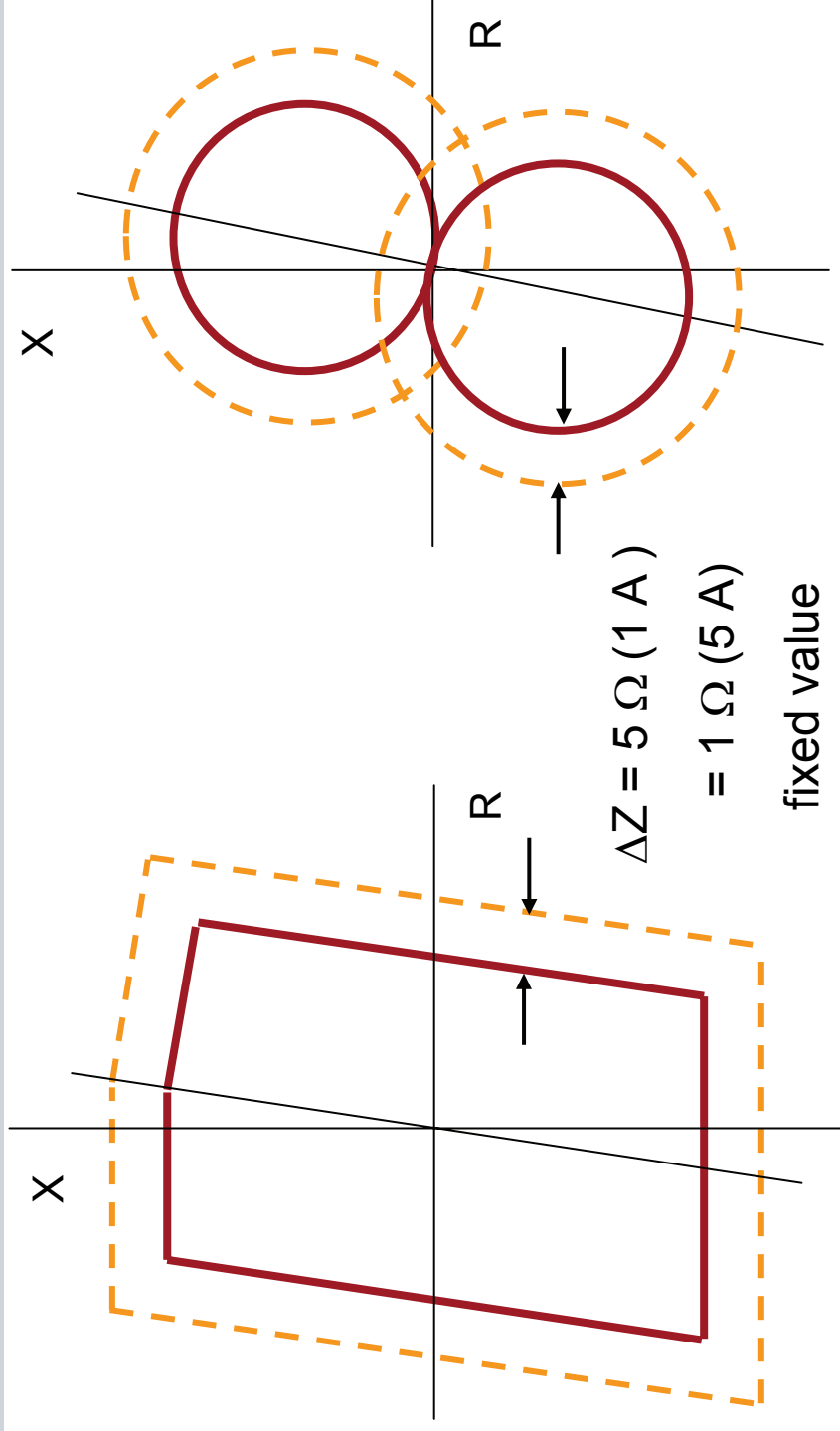
Advanced Power swing blocking techniques (7SA522, 7SA6..)

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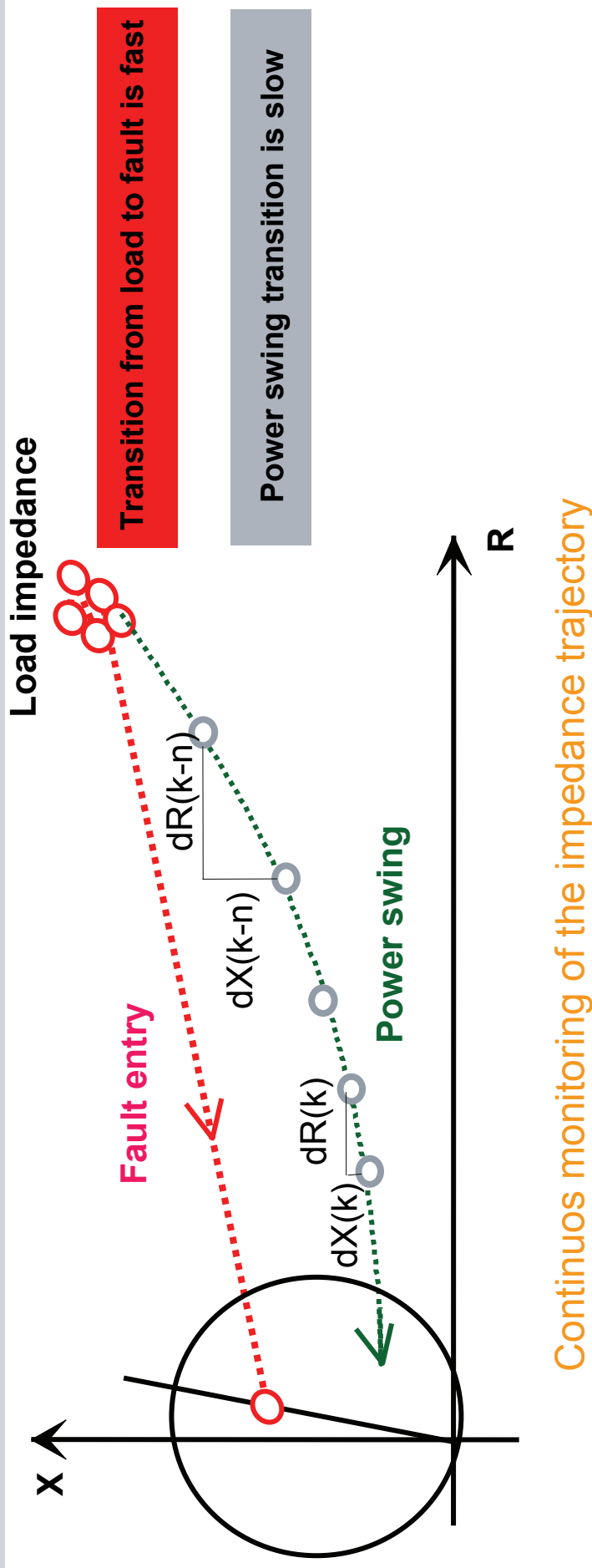
- Novel space vector based principle
- Self-setting
- Small ΔZ (5 Ohm at $I_n = 1$ A) , fixed setting
- Blocking up to high slip frequencies (7 Hz)
- Recognition of all fault types during swing
- Remains effective during single pole ARC open time (3-phase set-up)



Self-adaptation of outer power swing characteristic

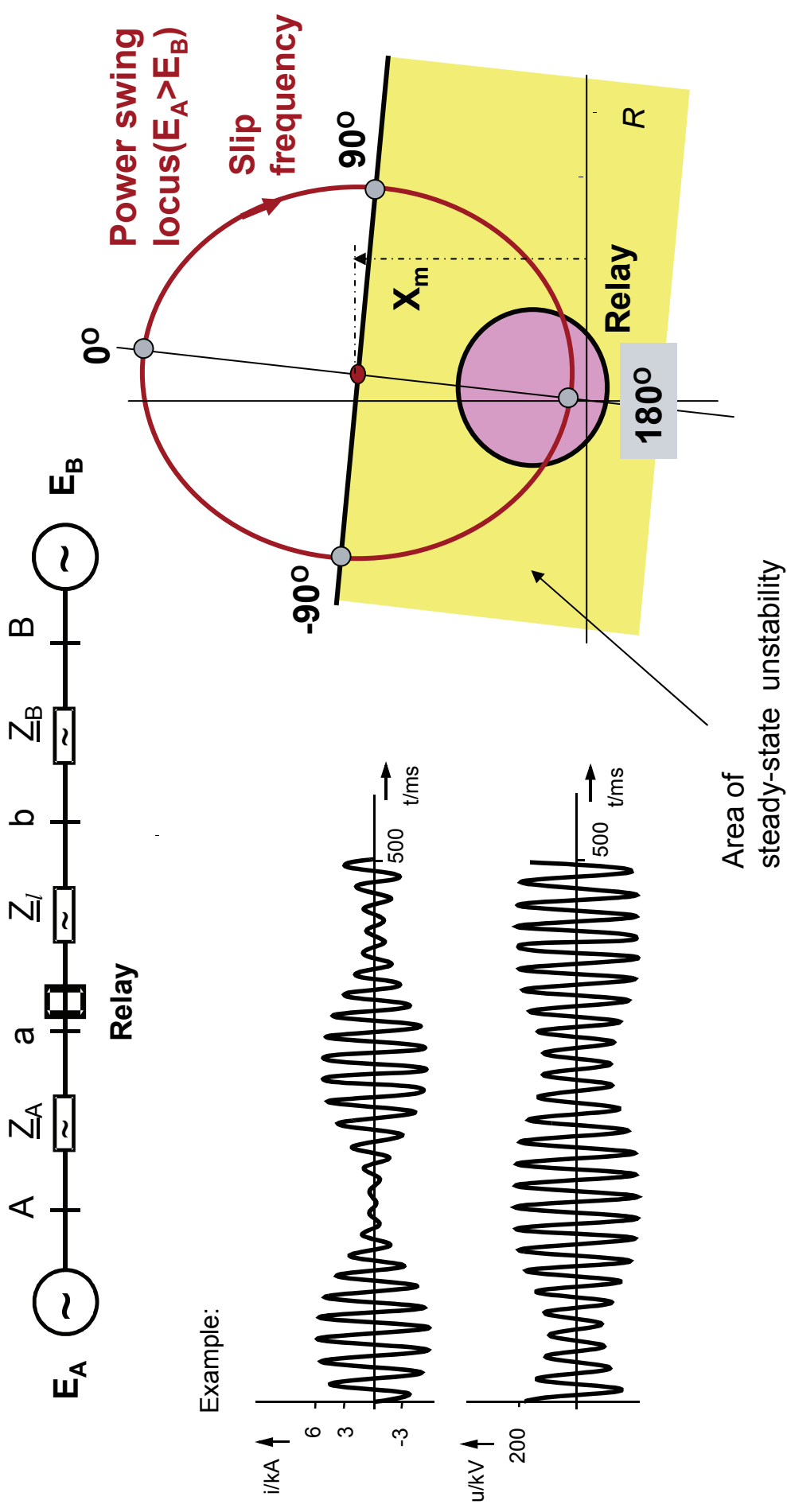


Power Swing detection: New method

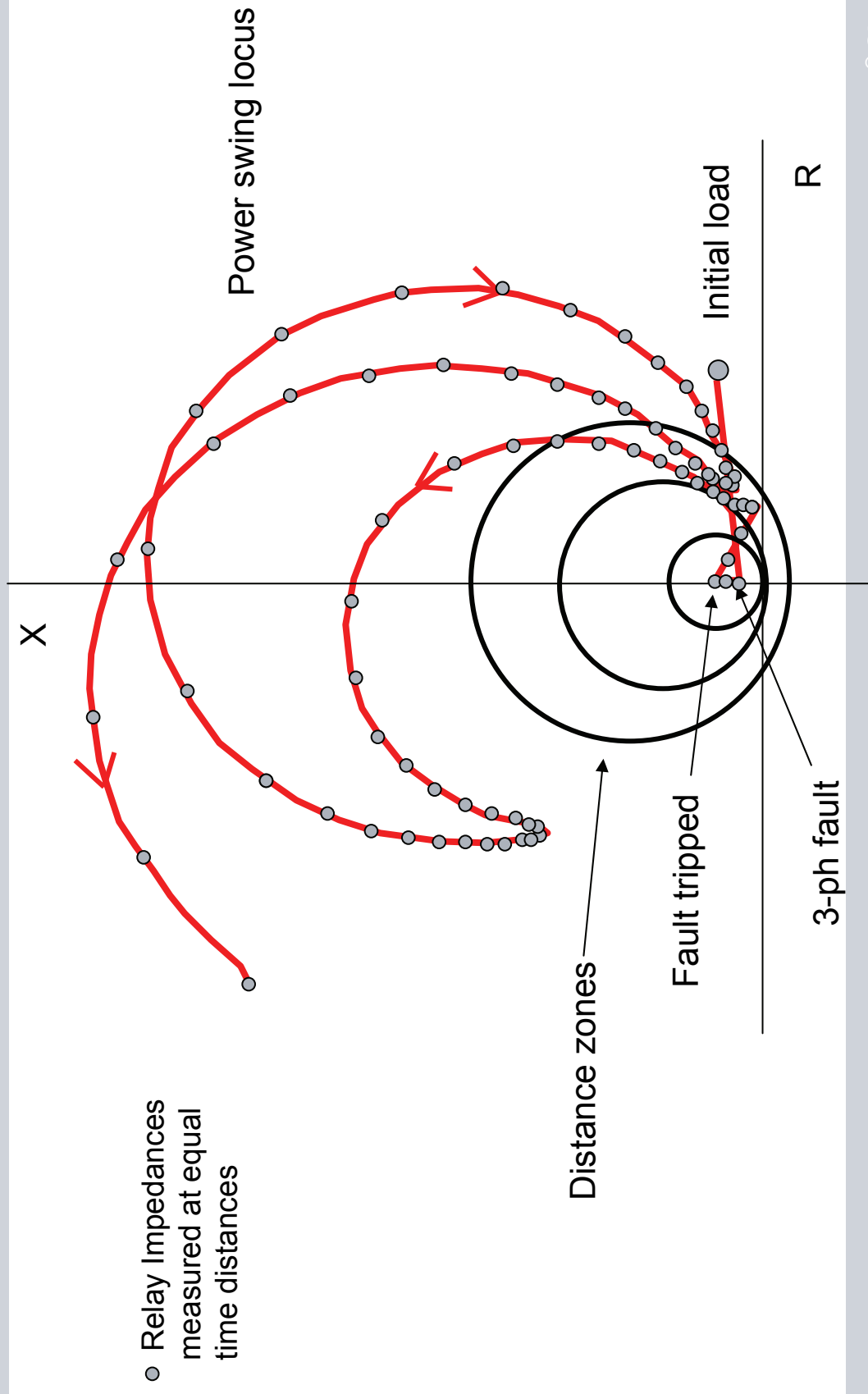


- Monitoring of trajectory continuity: $R(n) - R(n-1) < 300\%$, $Z(n) - Z(n-1) < 15\%$
- Monitoring of trajectory velocity ($> 10 \Omega/s$)
- Evaluation of trajectory ellipse: unstable area: $-90^\circ < \delta < +90^\circ$

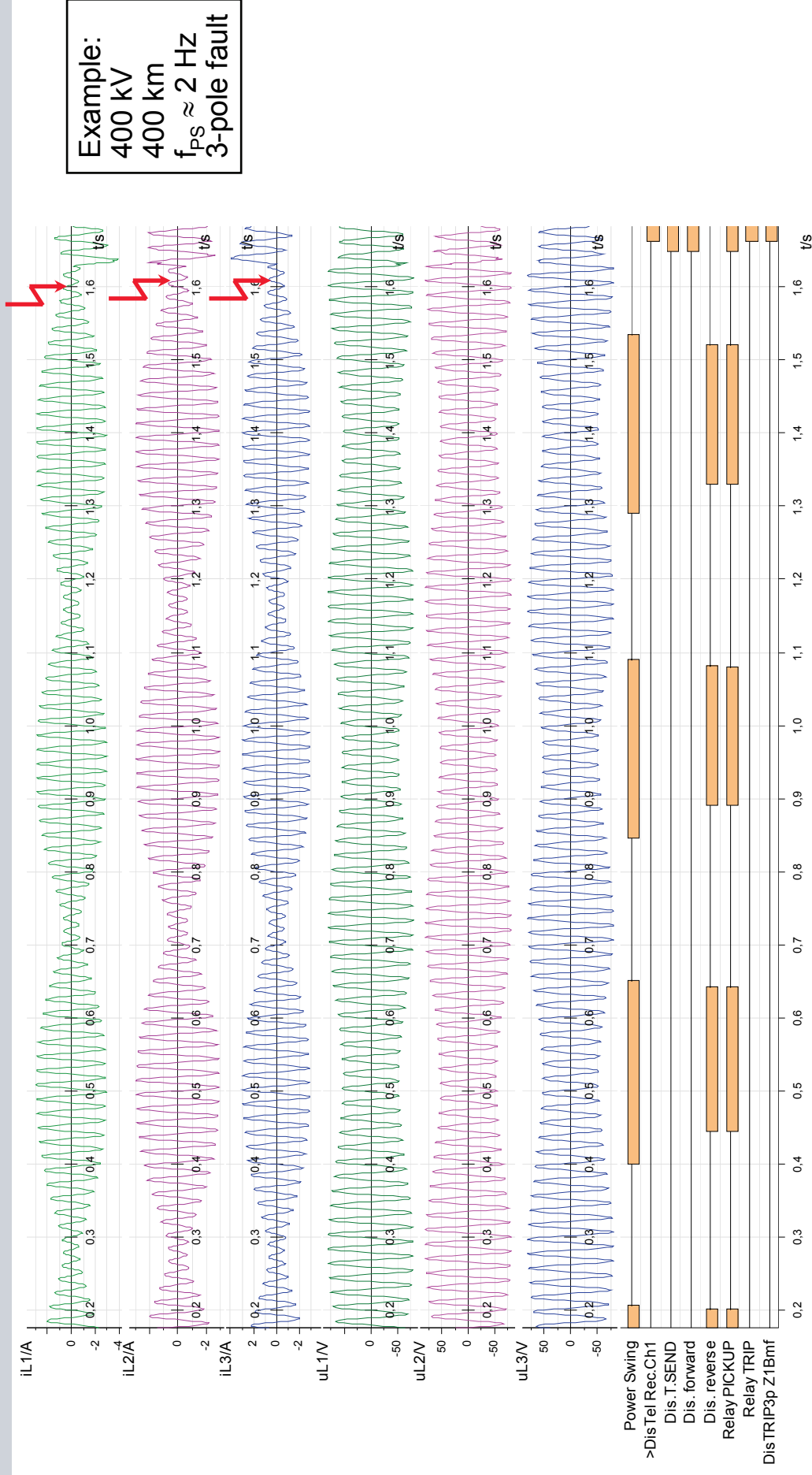
Evaluation of the power swing process



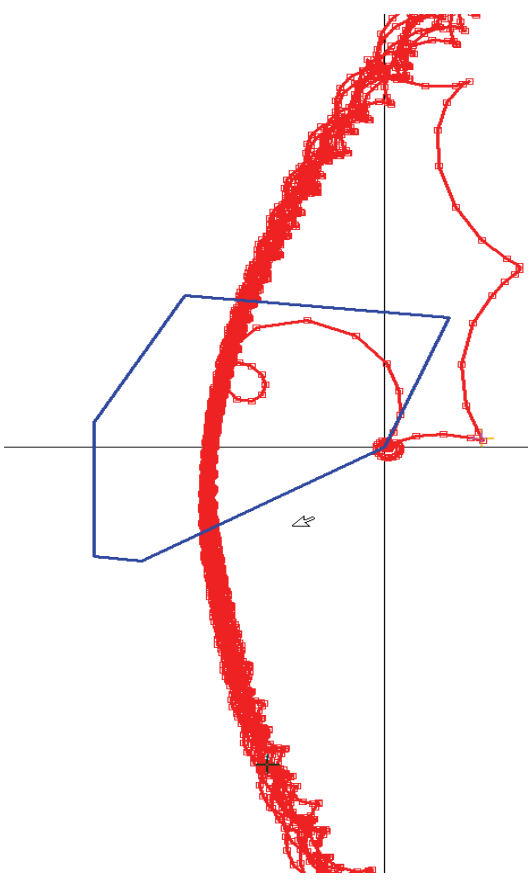
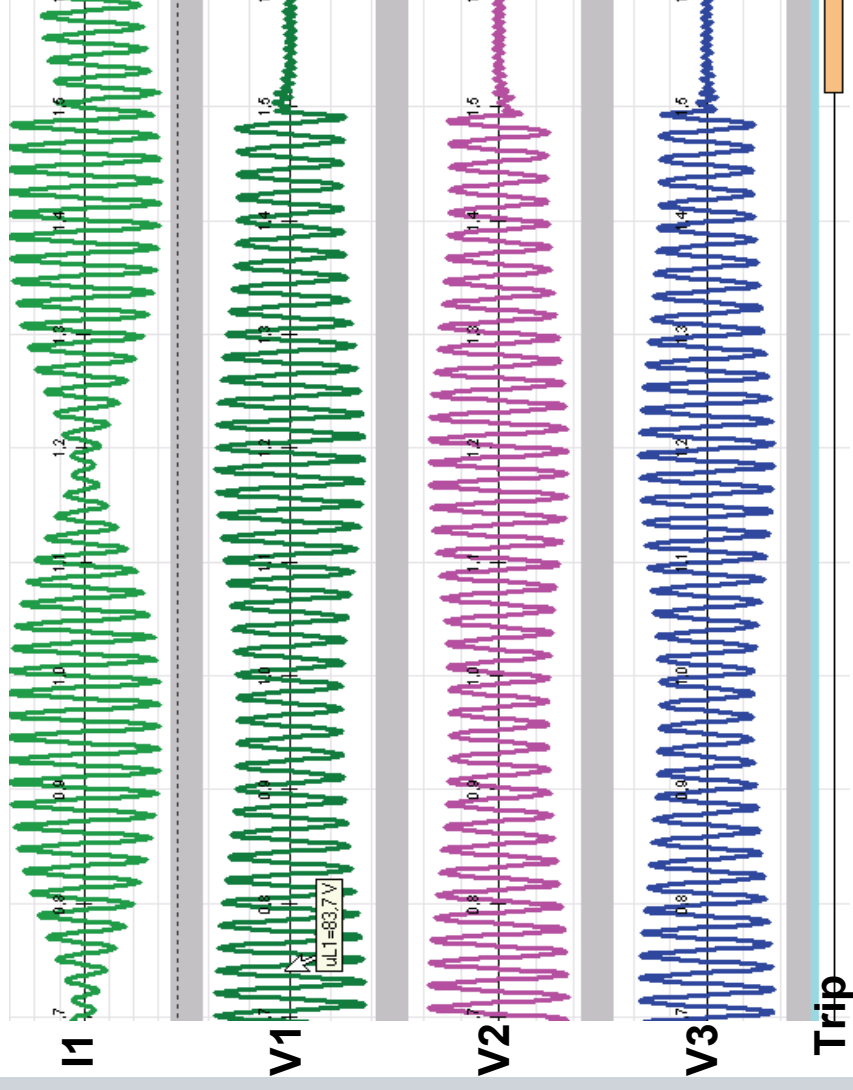
Power swing (simulation)



Novel power swing detection provides secure operation with swing frequencies of up to 7 Hz



Three-phase fault during Power Swing



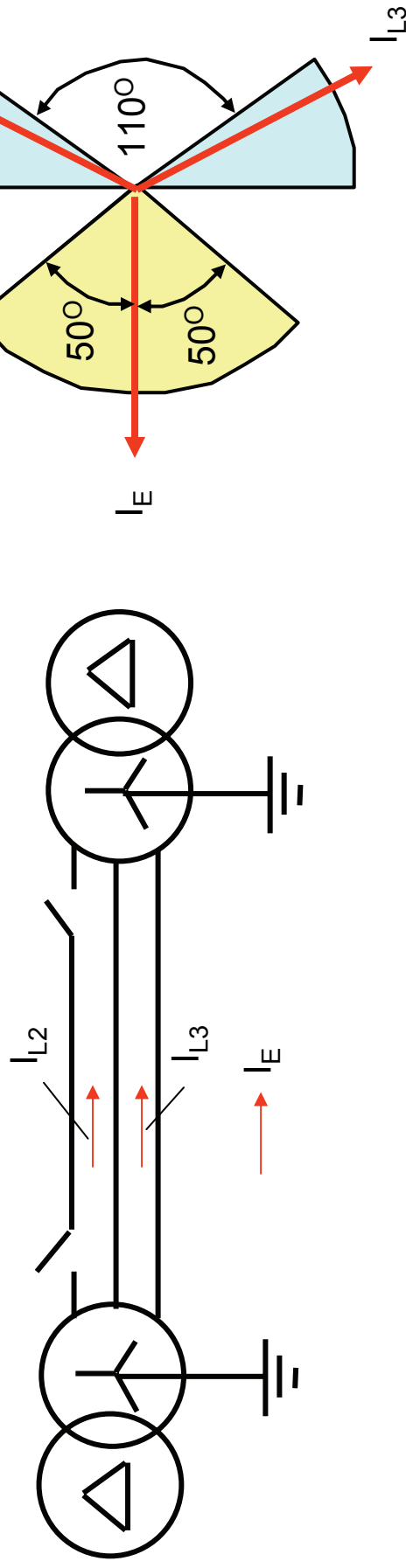
Three phase fault during power swing
is detected and cleared

Fault inception while swing is inside
trip characteristic

Special functions to maintain power swing blocking during one pole open condition

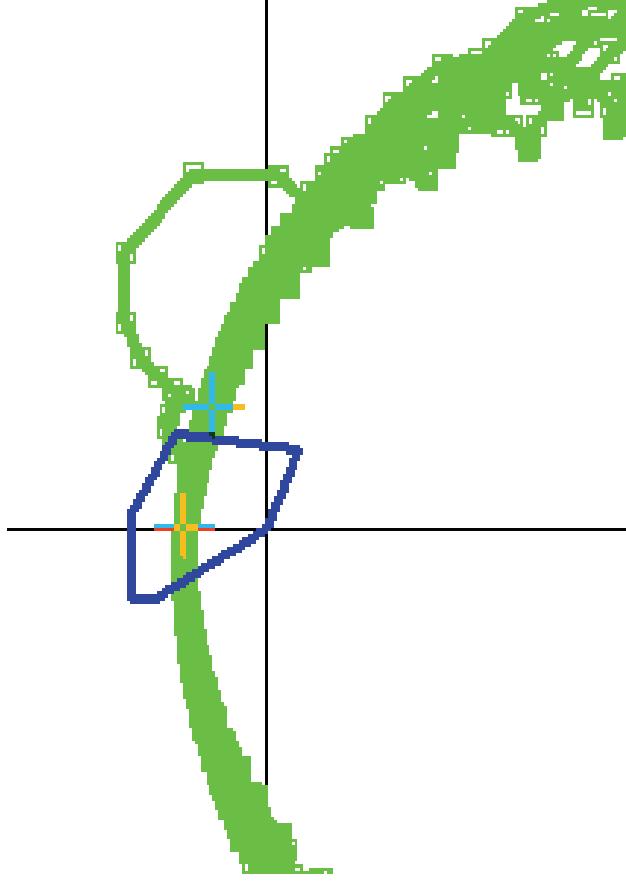
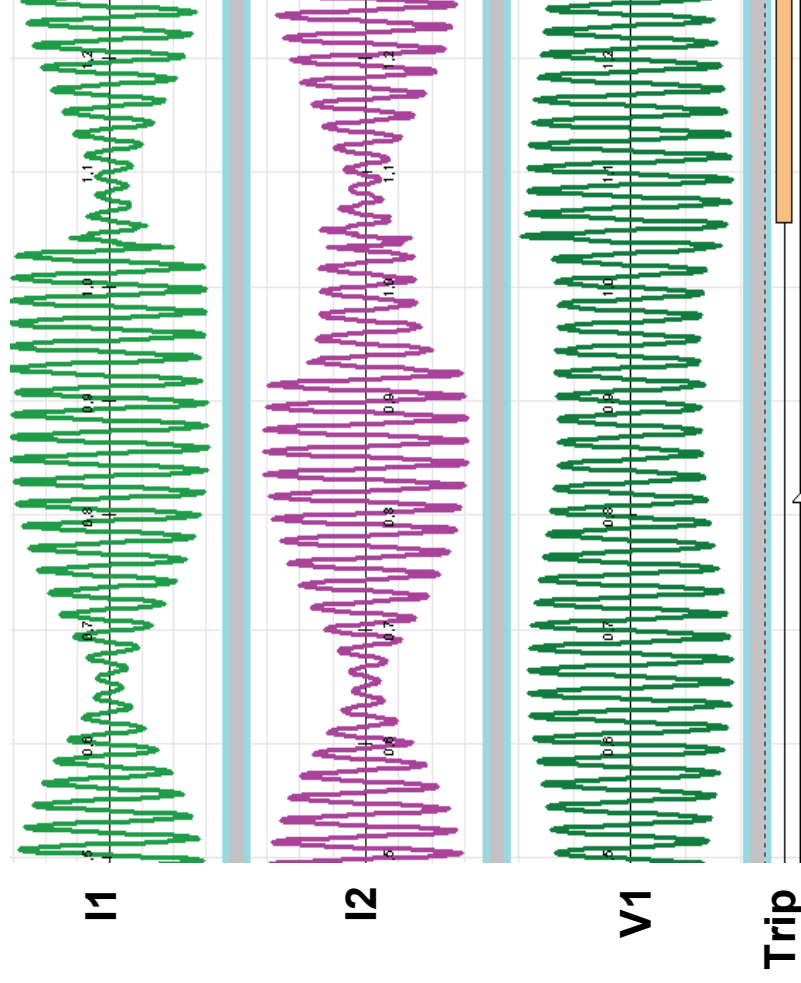
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- ◆ Phase segregated measurement
- ◆ Changed criteria for symmetry monitoring and earth-fault detection



Single-phase fault detection during power swing 1-pole open condition (auto-reclosure dead time)

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The Power swing passes through the trip characteristic several times.

Single phase fault is detected and cleared.

Selectable actions of power swing protection

Power swing blocking

- ◆ Block all zones ➤ normal
- ◆ Block 1st zone only ➤ fast swings only
- ◆ Block all but 1st zone ➤ 1st zone short, electrical centre far outside

Power swing tripping

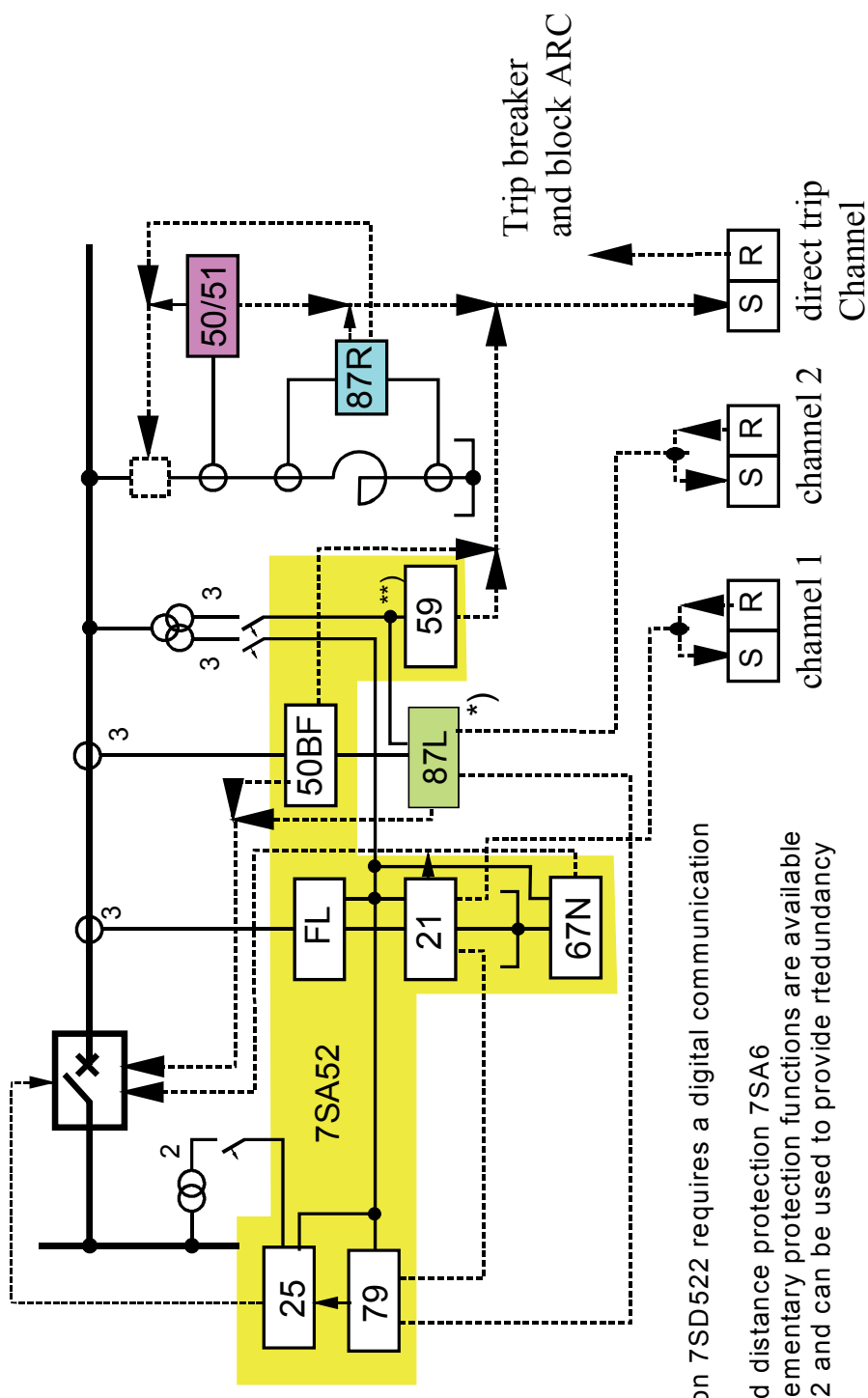
- controlled separation of swinging areas (tie-lines)



- ◆ Shaped quadrilateral and mho type characteristics with load cut-out allow high line loading.
- ◆ Reliable power swing protection prevents overfunction under transient conditions:
 - ◆ Blocking up to high slip frequencies (7 Hz)
 - ◆ Automatic setting adaptation (no need for special analyses and calculations)
 - ◆ All kinds of fault during power swing are detected and distance protection is released to operate and trip if required
 - ◆ Power swing tripping can be selected where appropriate

Distance Protection in the Transmission System

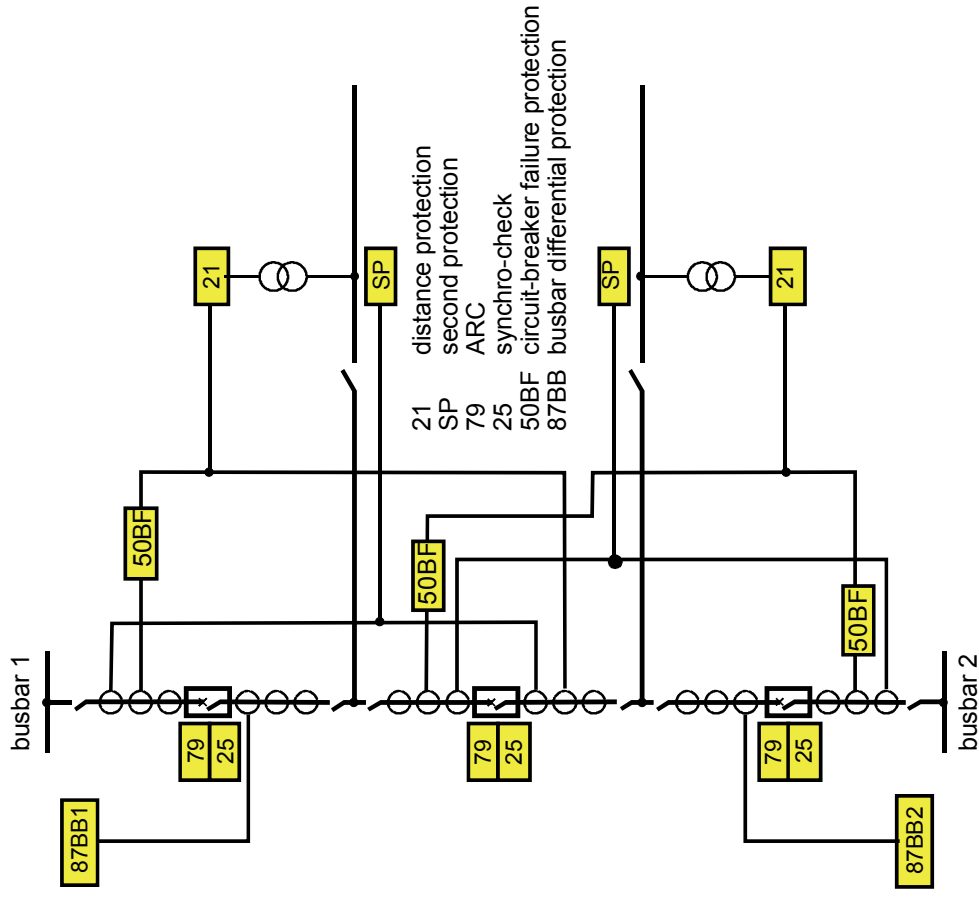
Protection Concept for EHV-lines

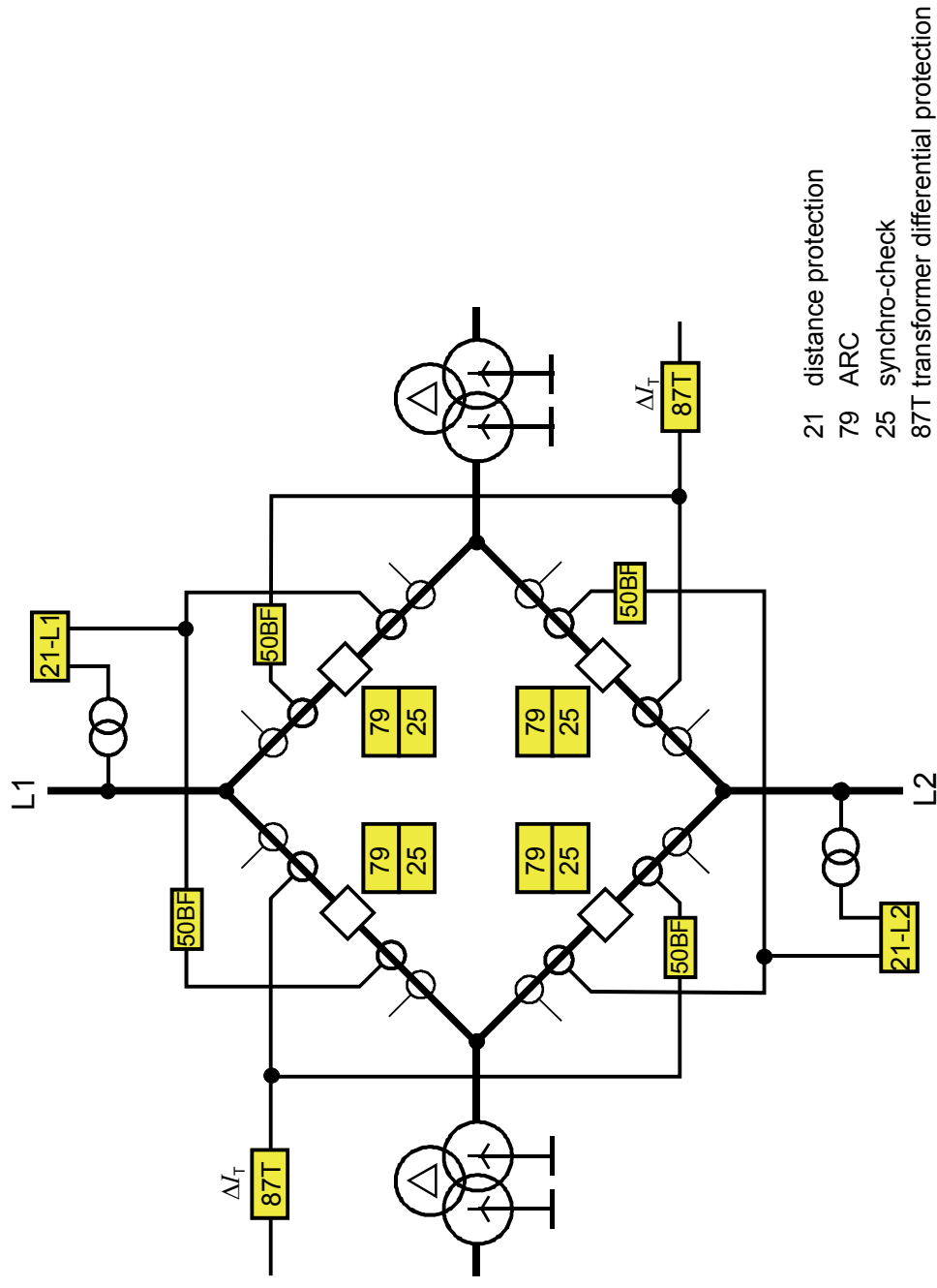


- *) - differential protection 7SD522 requires a digital communication channel (64 kBit/s)
- alternatively second distance protection 7SA6
- In each case supplementary protection functions are available similar to the 7SA52 and can be used to provide redundancy

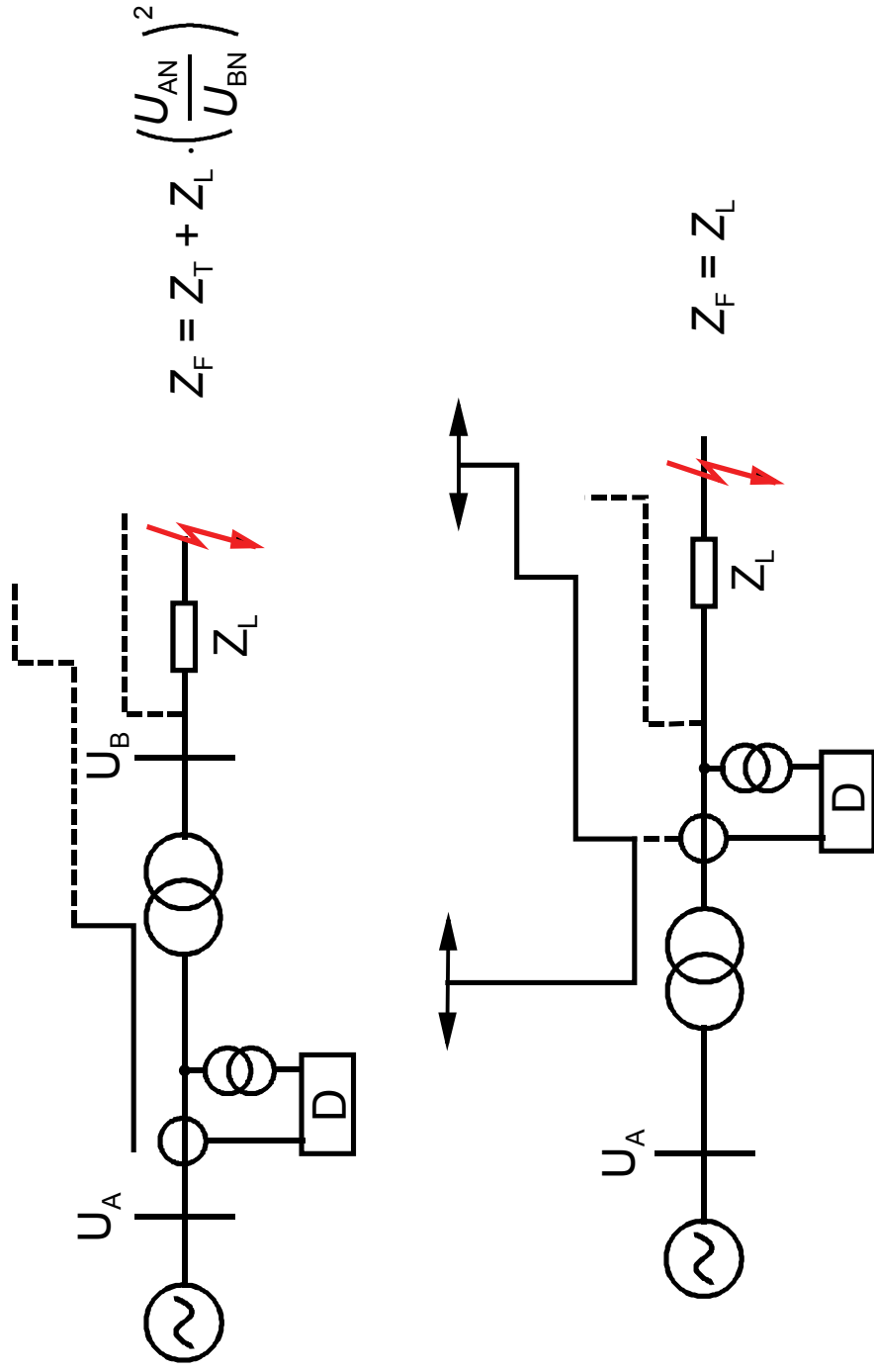
**)only on very long lines > approx. 150 km

Protection concept for a 1-and-1/2 circuit-breaker bay





Distance protection at generating units



Fundamentals of Distance Protection

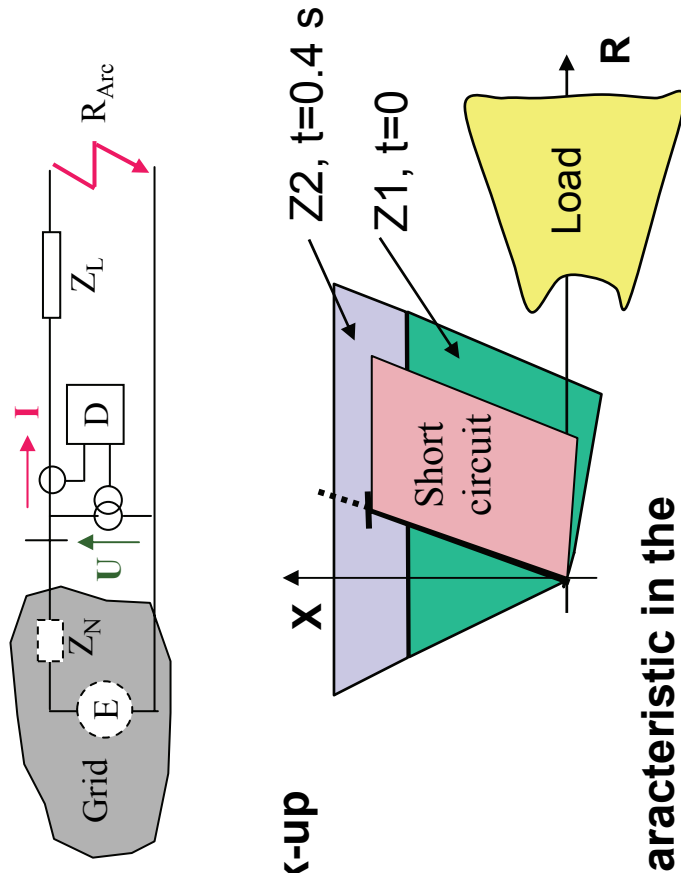
Protection criterion “Impedance”

■ The fault impedance is calculated from voltage and current at the fault location: $Z = U / I$

■ The fault impedance is proportional to the fault distance

■ Add-on criterion “time” is used for selectivity and graded back-up

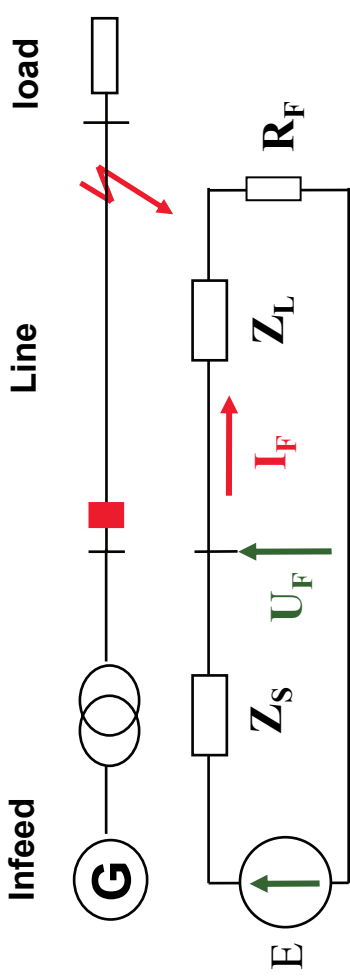
Distance protection
(Impedance protection)



■ Characteristic in the impedance diagram:

Fault loop quantities

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$$E = \frac{1,1 \times U_N}{\sqrt{3}} \quad Z_S = \frac{U_N^2}{SSC'''} \quad Z_F = Z_L' [\text{Ohm / km}] \times l(\text{km})$$

$$I_{F-3ph} = \frac{E_{Ph-N}}{Z_S + Z_L + R_F}$$

$$\underline{U}_{F-3ph} = \frac{Z_L + R_F}{Z_S + Z_L + R_F} \cdot \underline{E}_{Ph-N}$$

Influencing quantities:

- Short circuit power of the infeed (Source impedance Z_S)
- Line impedance to fault location (fault impedance Z_L)
- Fault resistance (R_F)
- Star point earthing impedance (current limitation, e.g. to 2 kA)

Example (R_F neglected):

$$E = \frac{1,1 \times 110 \text{ kV}}{\sqrt{3}} = 70 \text{ kV}$$

$$Z_S = \frac{110 \text{ kV}^2}{5000 \text{ MVA}} = 2,4 \text{ Ohm}$$

$$Z_L = 0,4 [\text{Ohm / km}] \times 20 (\text{km}) = 8 \text{ Ohm}$$

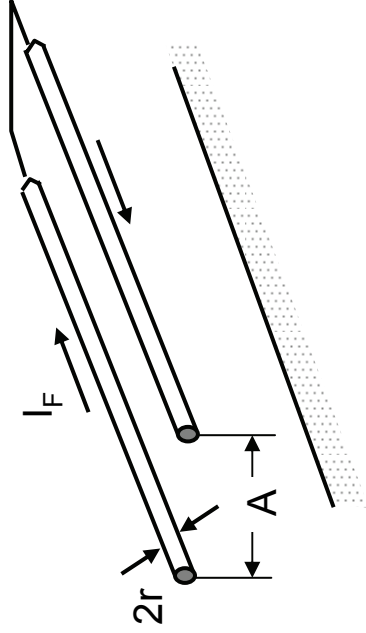
$$I_{F-3-ph} = \frac{70 \text{ kV}}{(2,4 + 8,0) \text{ Ohm}} = 6,7 \text{ kA}$$

$$U_{F-3ph} = \frac{8 \text{ Ohm}}{(2,4 + 8) \text{ Ohm}} \cdot 70 \text{ kV} = 53,8 \text{ kV}$$

$$\text{SIR (System impedance ratio): } \frac{Z_S}{Z_L}$$

Fault loops, Impedances

Phase-Phase loop



$$\underline{Z}'_{Ph-Ph} = 2 \cdot R'_L + j 2 \cdot \omega \cdot 10^{-4} \cdot \left(2 \cdot \ln \frac{A}{r} + 0.5 \cdot \mu_1 \right) \Omega/km$$

Example:

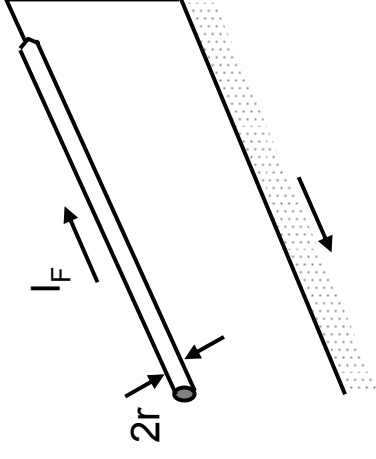
$A = 3.5 \text{ m}$, $r = 0.95 \text{ cm} = 9.5 \cdot 10^{-3} \text{ m}$, $\rho = 100 \text{ Ohm} \cdot \text{m}$

$R'_L = 0.157 \text{ Ohm/km}$

$Z'_{Ph-Ph} = 0.314 + j0.774 \text{ Ohm/km}$

$Z'_{Ph-E} = 0.207 + j0.737 \text{ Ohm/km}$

Phase-Earth loop



$$\underline{Z}'_{Ph-E} = R'_L + R'_E + j \omega \cdot 10^{-4} \cdot \left(2 \cdot \ln \frac{\delta}{r} + 0.5 \cdot \mu_1 \right) \Omega/km$$

$$\delta = 1650 \cdot \sqrt{\frac{\rho}{\omega}} \text{ m}$$

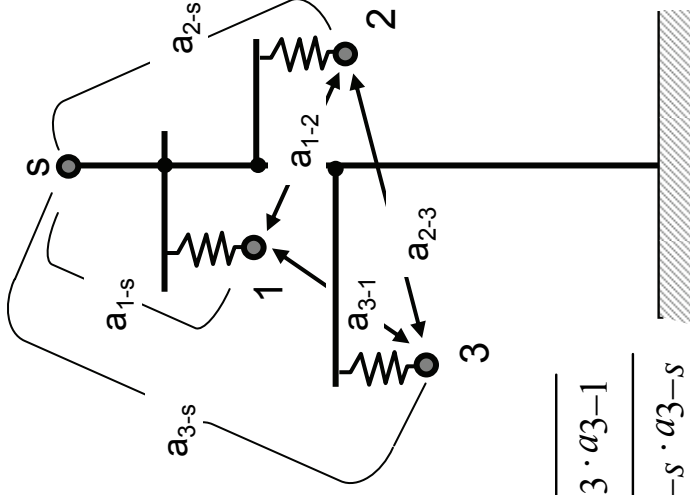
$$R'_E = \frac{\pi}{2} \cdot \omega \cdot 10^{-4} \Omega/km$$

ρ : earth resistivity in Ωm

100 for wet soil, 500 for dry soil

μ_1 : relative permeability (1 für Cu and AL)

Calculation of the line impedances transposed line



$$A = \sqrt[3]{a_{1-2} \cdot a_{2-3} \cdot a_{3-1}}$$

$$A_s = \sqrt[3]{a_{1-s} \cdot a_{2-s} \cdot a_{3-s}}$$

ρ : Earth resistivity in Ωm
100 for wed soil, 500 for dry soil

μ_1 : relative Permeability (1 for Cu and AL)

Positive-sequence impedance

$$\underline{Z}'_1 = R'_L + j\omega \cdot 10^{-4} \cdot \left(2 \cdot \ln \frac{A}{r} + 0.5 \cdot \mu_1 \right) \Omega/\text{km}$$

Zero-sequence impedance

Without earth wire:

$$\underline{Z}'_0 = R'_L + 3 \cdot R'_E + j\omega \cdot 10^{-4} \cdot \left(6 \cdot \ln \frac{\delta}{\sqrt[3]{r \cdot A^2}} + 0.5 \cdot \mu_1 \right) \Omega/\text{km}$$

With earth wire:

$$\underline{Z}'_{0E} = \underline{Z}'_0 - 3 \cdot \frac{\underline{Z}'_{1s}}{\underline{Z}'_s} \Omega/\text{km}$$

with: $\underline{Z}'_{1s} = R'_E + j\omega \cdot 10^{-4} \cdot 2 \cdot \ln \frac{\delta}{A_s} \Omega/\text{km}$

$$\underline{Z}'_s = R'_s + R'_E + j\omega \cdot 10^{-4} \cdot \left(2 \cdot \ln \frac{\delta}{r_s} + 0.5 \cdot \mu_1 \right) \Omega/\text{km}$$

$$\delta = 1650 \cdot \sqrt{\frac{\rho}{\omega}} \text{ m} \quad \text{und} \quad R'_E = \frac{\pi}{2} \cdot \omega \cdot 10^{-4} \Omega/\text{km}$$

Loop impedances (phase-phase fault) Transposed and non-transposed line

Example:

132 kV line 185/32 mm² Al/St

Conductor radius $r = 0.95 \text{ cm} = 9.5 \cdot 10^{-3} \text{ m}$

Tower configuration: see figure)

$R_L' = 0.157 \text{ Ohm/km}$

$\rho = 100 \text{ Ohm} \cdot \text{m}$

Loop impedances:

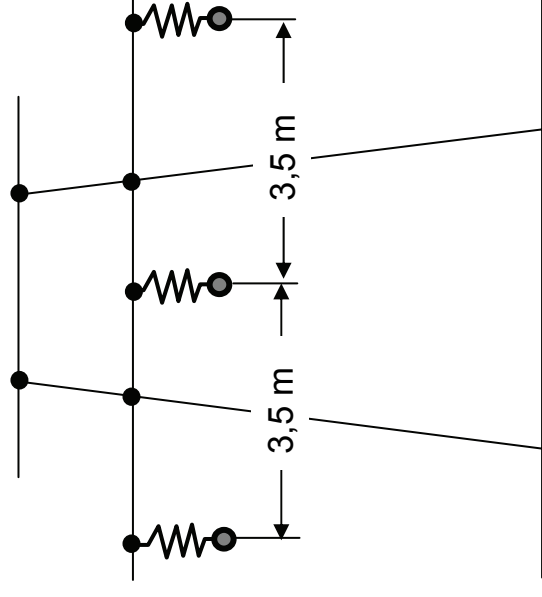
Transposed line:

$$\underline{Z}'_{\text{Ph-Ph}} = 2 \cdot \underline{Z}'_1 = 0.314 + j0.803 \text{ Ohm/km}$$

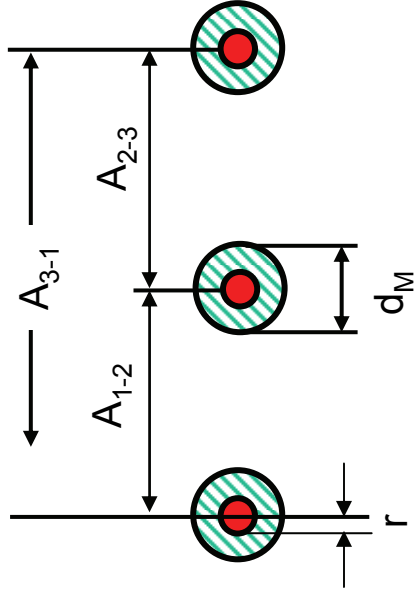
Non-transposed line:

$$\underline{Z}_{L1-L2} = \underline{Z}_{L2-L3} = 0.314 + j0.774 \text{ Ohm/km} (\Delta X = -3.6\% \text{ von } \underline{Z}'_1)$$

$$\underline{Z}_{L3-L1} = 0.314 + j0.861 \text{ Ohm/km} (\Delta X = +7.2\% \text{ von } \underline{Z}'_1)$$



Estimation of positive sequence cable impedances (Accurate data from the manufacturer)



$$\underline{Z}'_1 = R'_L + j\omega \cdot 10^{-4} \cdot \left(2 \cdot \ln \frac{A}{r} + 0.5 \cdot \mu_1 \right) \Omega/km$$

$$A = \sqrt[3]{A_{1-2} \cdot A_{2-3} \cdot A_{3-1}}$$

Example:

20 kV Plastic cable 240 mm²

Conductor: Cu

$r = 9,3$ mm

$d_M = 39,8$ mm

$A = 110$ mm

$$R'_L = \frac{10^3}{q[\text{mm}^2]} \cdot \kappa \left[\frac{\text{m}}{\Omega \cdot \text{mm}^2} \right] = \frac{10^3}{240 \cdot 58} = 0,072 \text{ } [\Omega/km]$$

$$A = \sqrt[3]{110 \cdot 110 \cdot 2 \cdot 110} = 138,6 \quad X'_L = 314 \cdot 10^{-4} \cdot (2 \cdot \ln \frac{138,6}{9,3} + 0,5) = 0,185 \text{ } \Omega/km$$

Cables with conductive shield:

When the conductive shield is earthed at both cable ends, X_L is reduced and R_L increased.
The coupling impedance between conductor and shield must be considered.

Zero-sequence impedance of cables

Can hardly be calculated:

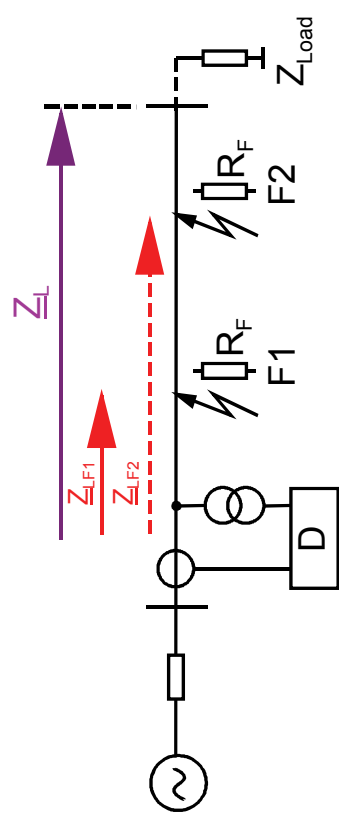
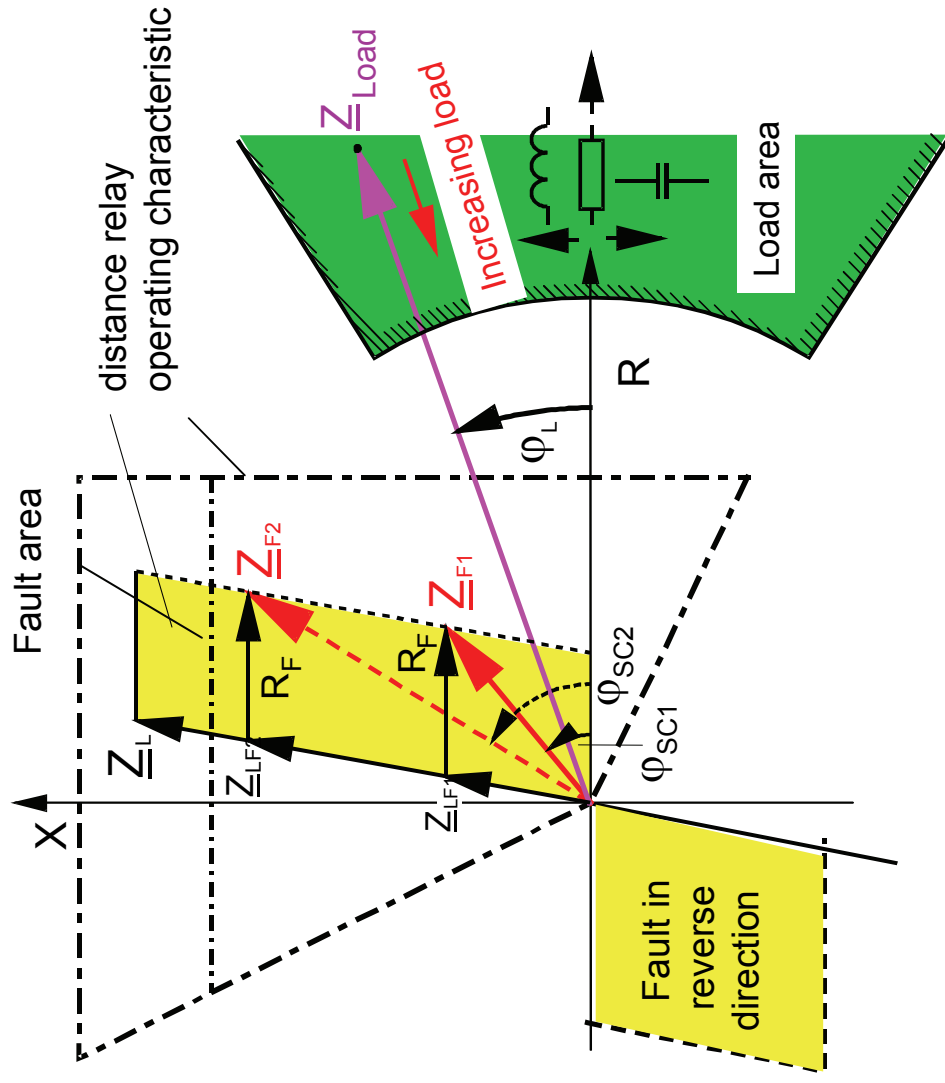
- Z_0 depends on the cable environment:
Parallel shields of other cables, gas pipes and rails
- In case of steel armoured cables, Z_0 is also current dependent:
Magnetising of steel bands and wires

Z_0 must be measured at the installed cable!

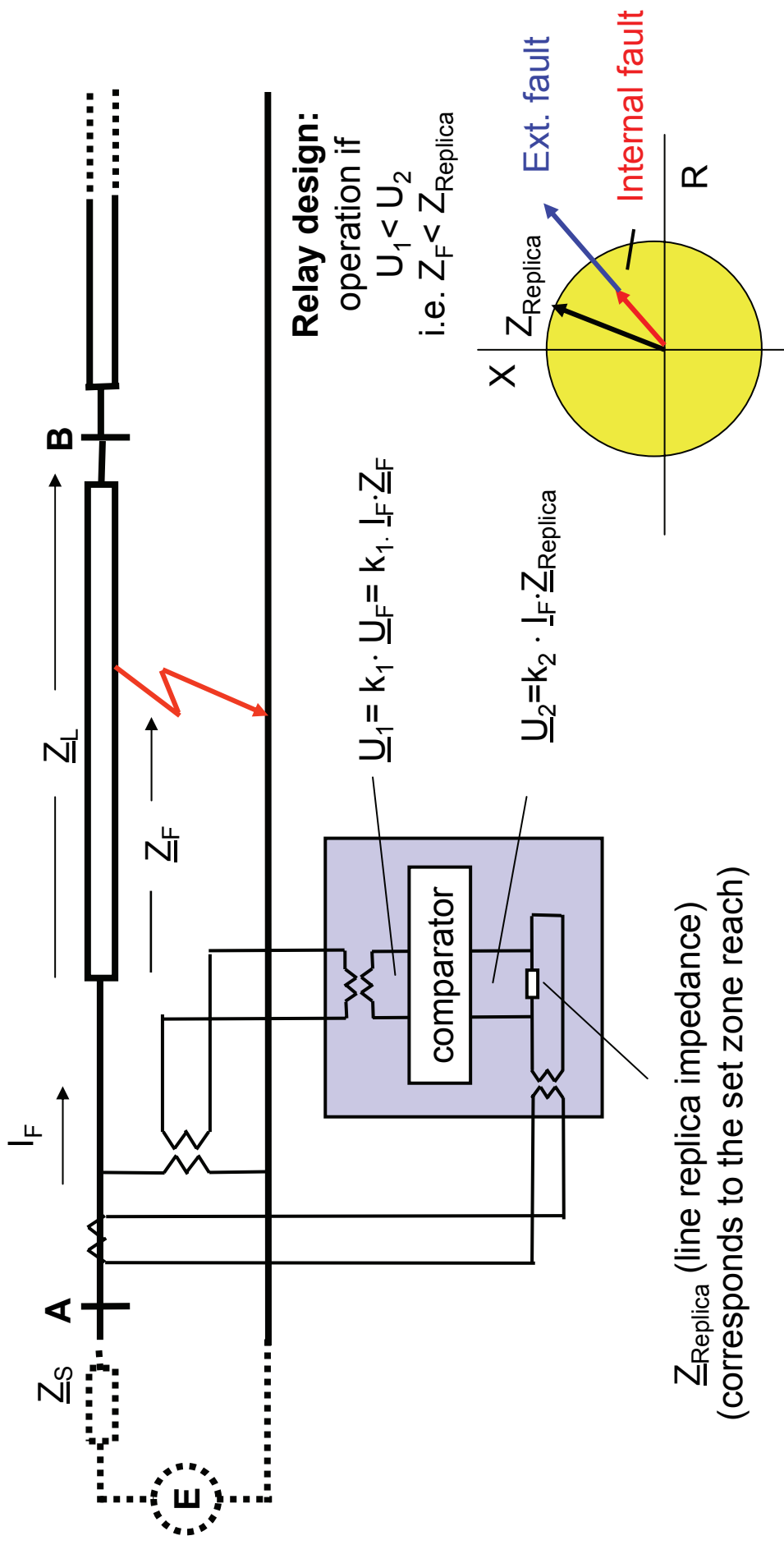
Measured mean values of cables in urban areas *):

400 kV	Single conductor oil cable 3x1x1200 mm ² Cu 0,05 + j0,11 Ohm/km	
110 kV	Three-core separately sheathed cable 3x150 mm ² Cu 0,5 + j0,3 Ohm/km	Plastic-insulated cable 3x1x630 mm ² Cu 0,45 + j0,34

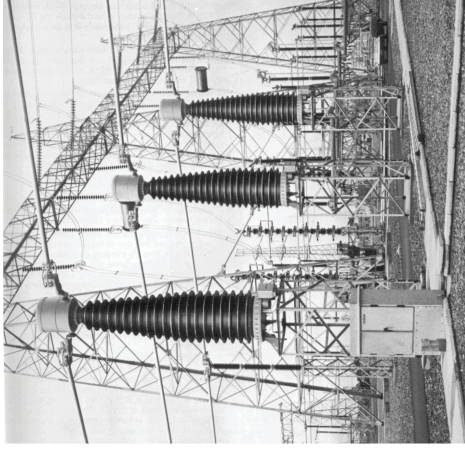
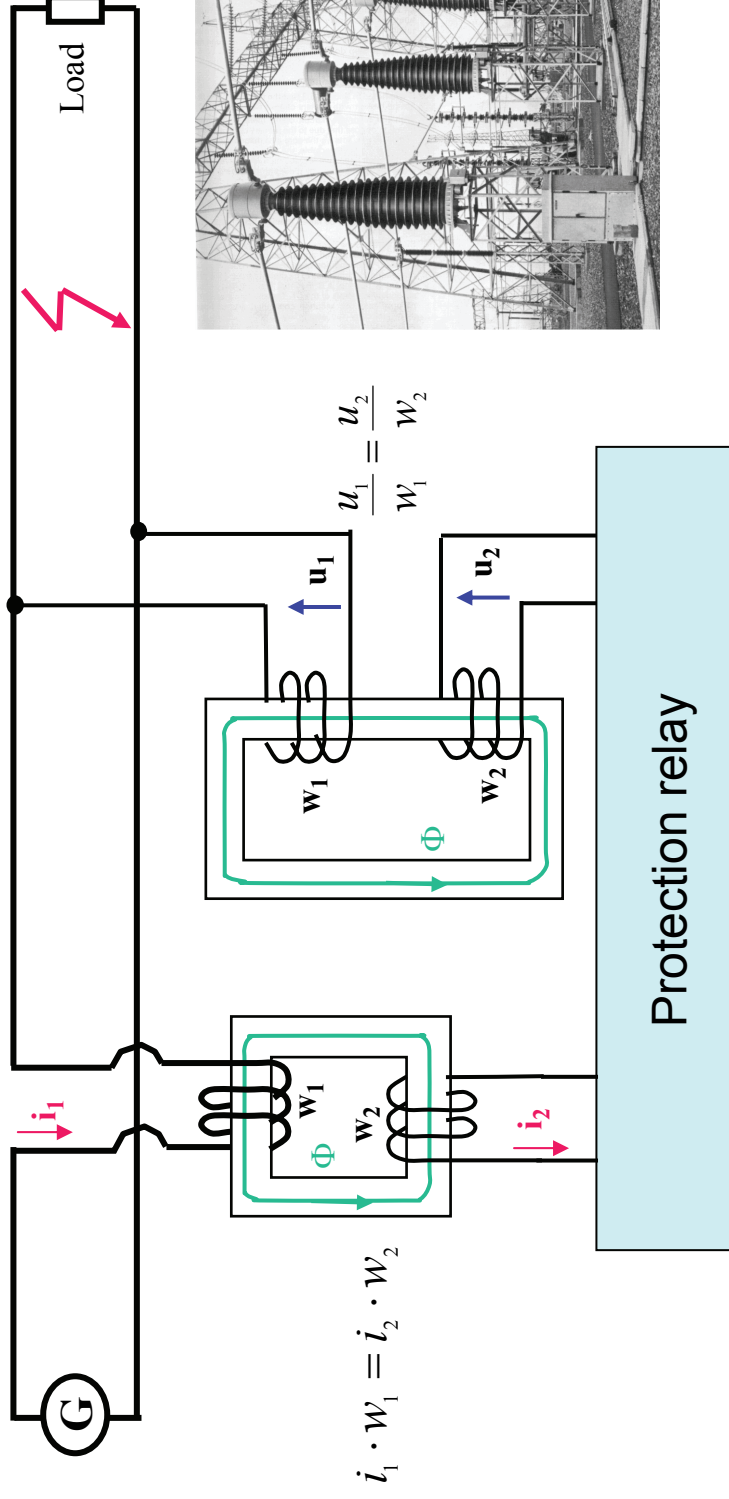
Load and short-circuit impedances



Principle of (analogue) distance relaying



Secondary impedance



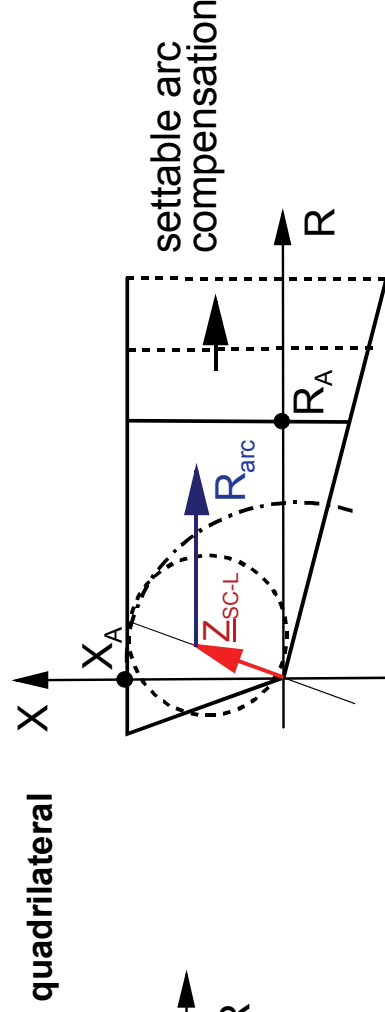
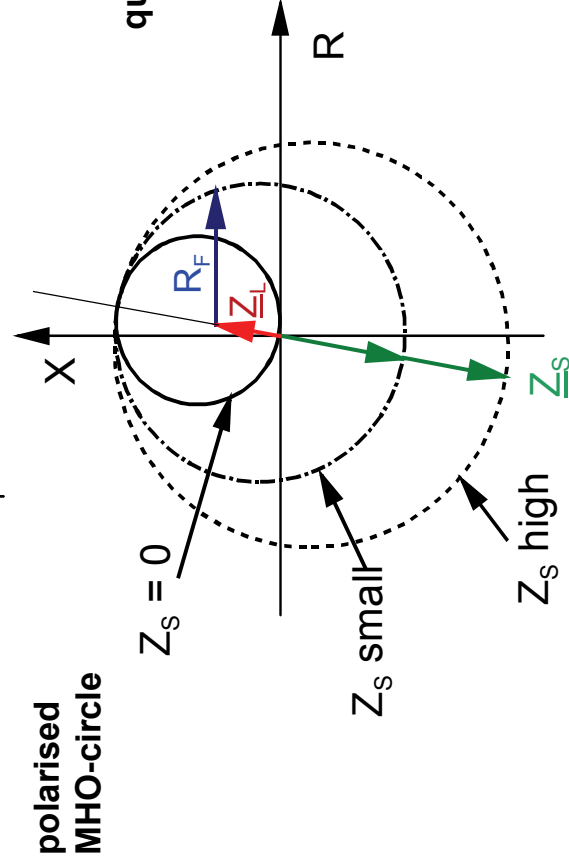
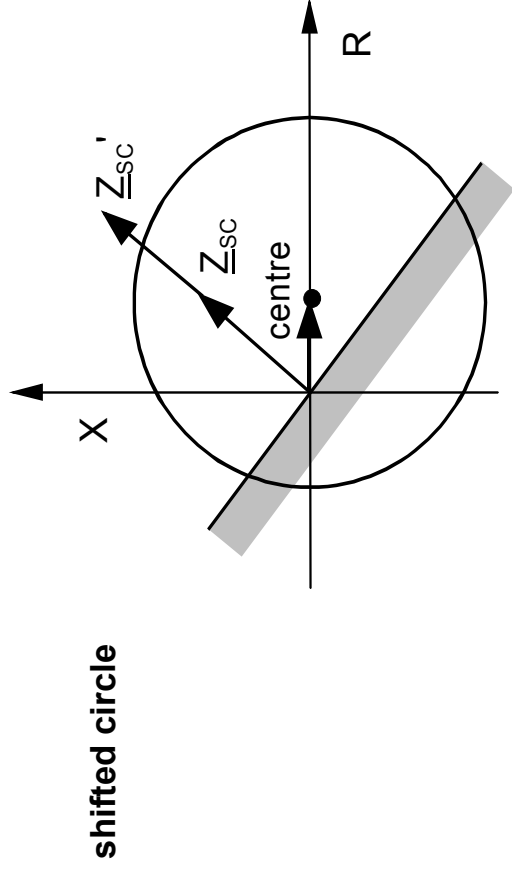
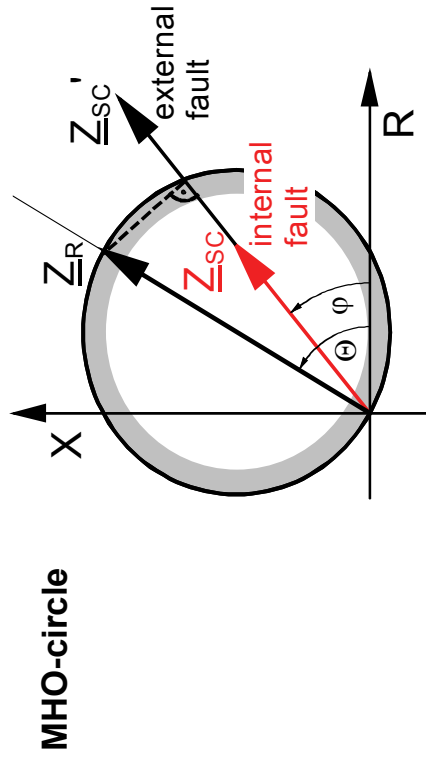
$$I_{\text{sec}} = I_{\text{prim}} / \text{CTR}$$

$$Z_{\text{sec}} = \frac{\text{CTR}}{\text{VTR}} \cdot Z_{\text{prim}}$$

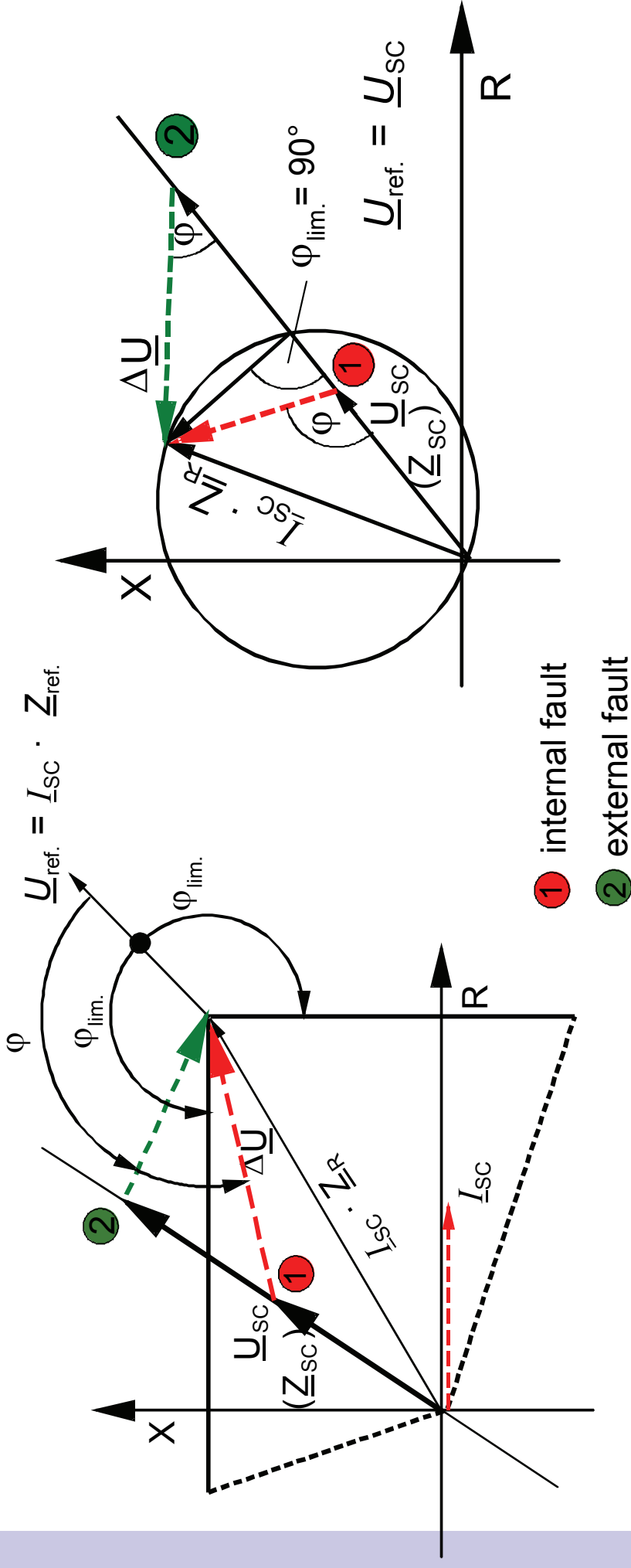
$$U_{\text{sec}} = U_{\text{prim}} / \text{VTR}$$

$$\left. \begin{array}{l} \text{CTR} = 600 / 1 \text{ A} \\ \text{VTR} = 110 / 0.1 \text{ kV} \end{array} \right\} Z_{\text{sec}} = 0.55 \cdot Z_{\text{prim}}$$

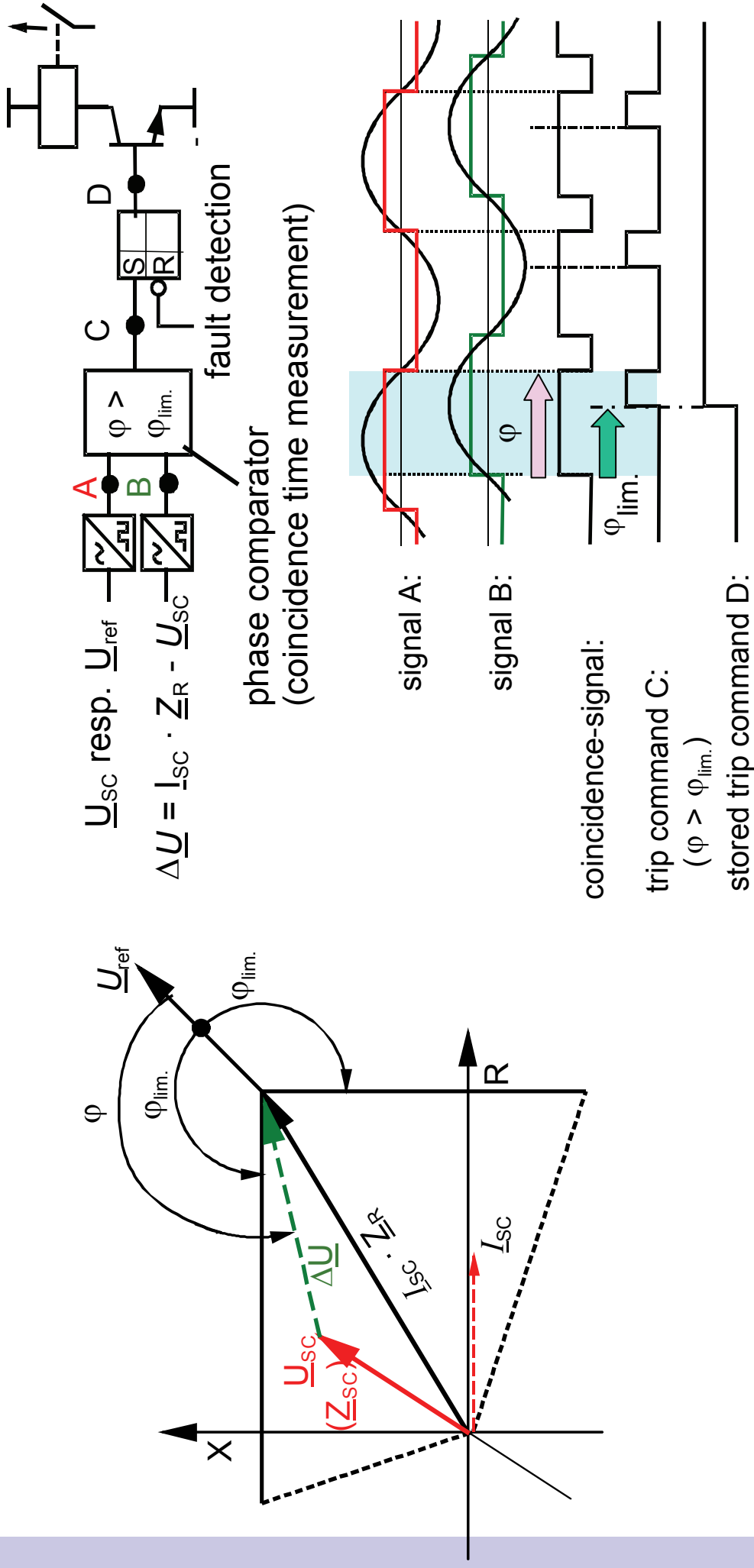
Typical distance zone-characteristics



Analogue static relays: distance measurement (1)

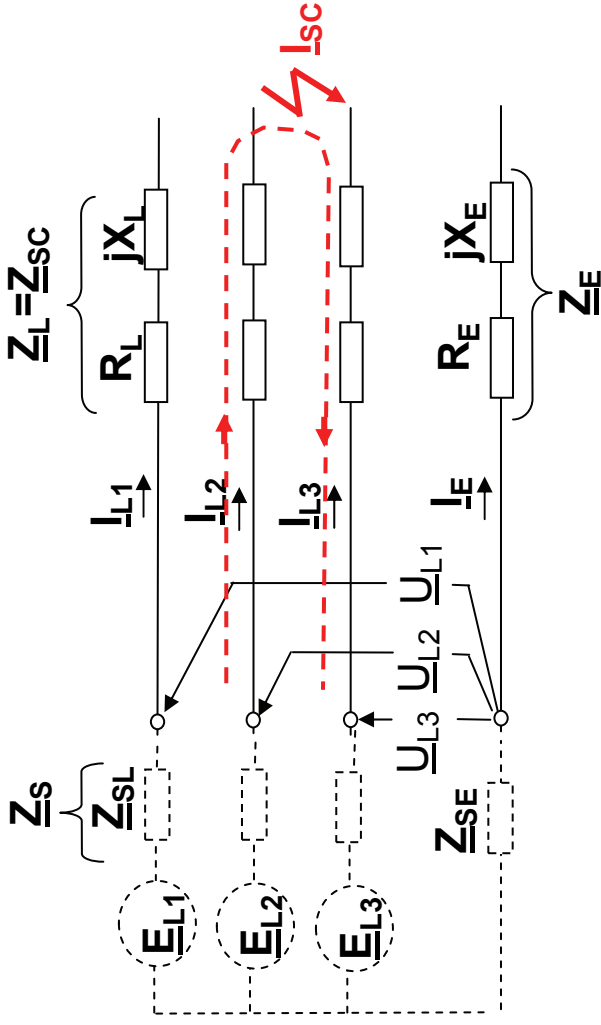


Analogue static relays: distance measurement (2)



Traditional Impedance measurement Phase-Phase loop

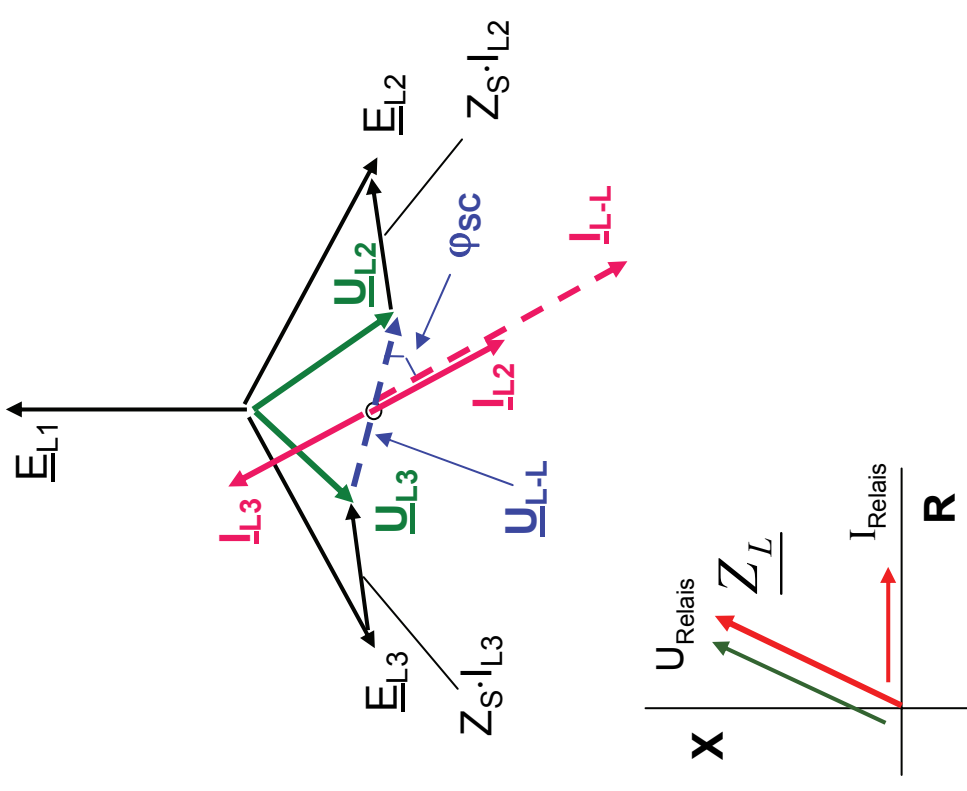
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$$\underline{U}_{L2-L3} = \underline{U}_{L2} - \underline{U}_{L3} = \underline{I}_{L2} \cdot \underline{Z}_L - \underline{I}_{L3} \cdot \underline{Z}_L = 2 \cdot \underline{I}_{sc} \cdot \underline{Z}_L$$

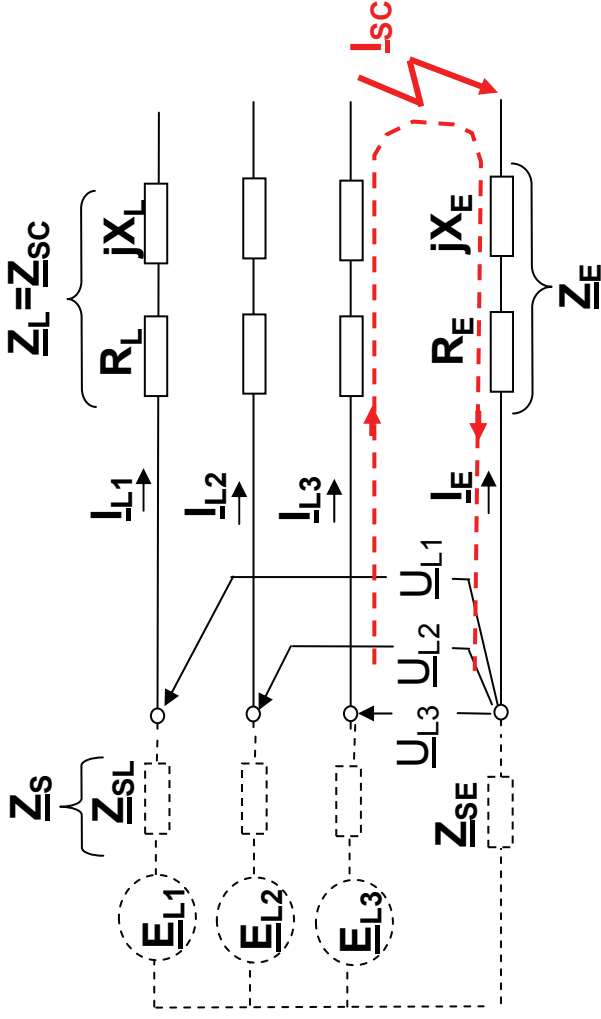
$$\underline{I}_{L2-L3} = \underline{I}_{L2} - \underline{I}_{L3} = 2 \cdot \underline{I}_{sc}$$

$$\underline{Z}_{L2-L3} = \frac{\underline{U}_{L2} - \underline{U}_{L3}}{\underline{I}_{L2} - \underline{I}_{L3}} = \frac{\underline{U}_{L-L}}{\underline{I}_{L-L}} = \frac{2 \cdot \underline{I}_{sc} \cdot \underline{Z}_L}{2 \cdot \underline{I}_{sc}} = \underline{Z}_L$$



Traditional Impedance measurement Phase-Earth loop

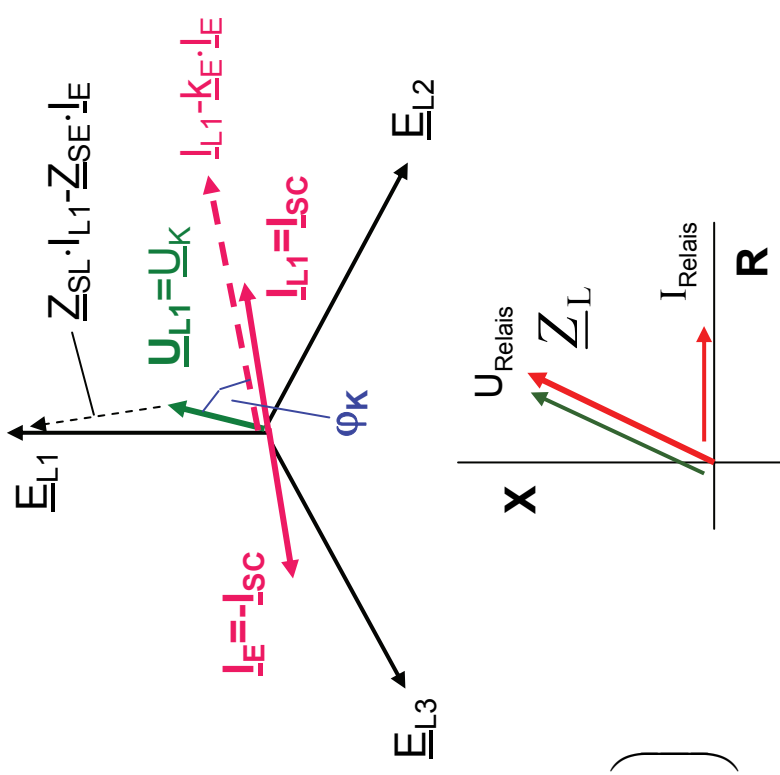
SIEMENS



$$\underline{U}_{\text{Re lais}} = \underline{U}_{L1} = \underline{I}_{L1} \cdot \underline{Z}_L - \underline{I}_E \cdot \underline{Z}_E = \underline{Z}_L \cdot \left(\underline{I}_{L1} - \frac{\underline{Z}_E}{\underline{Z}_L} \cdot \underline{I}_E \right)$$

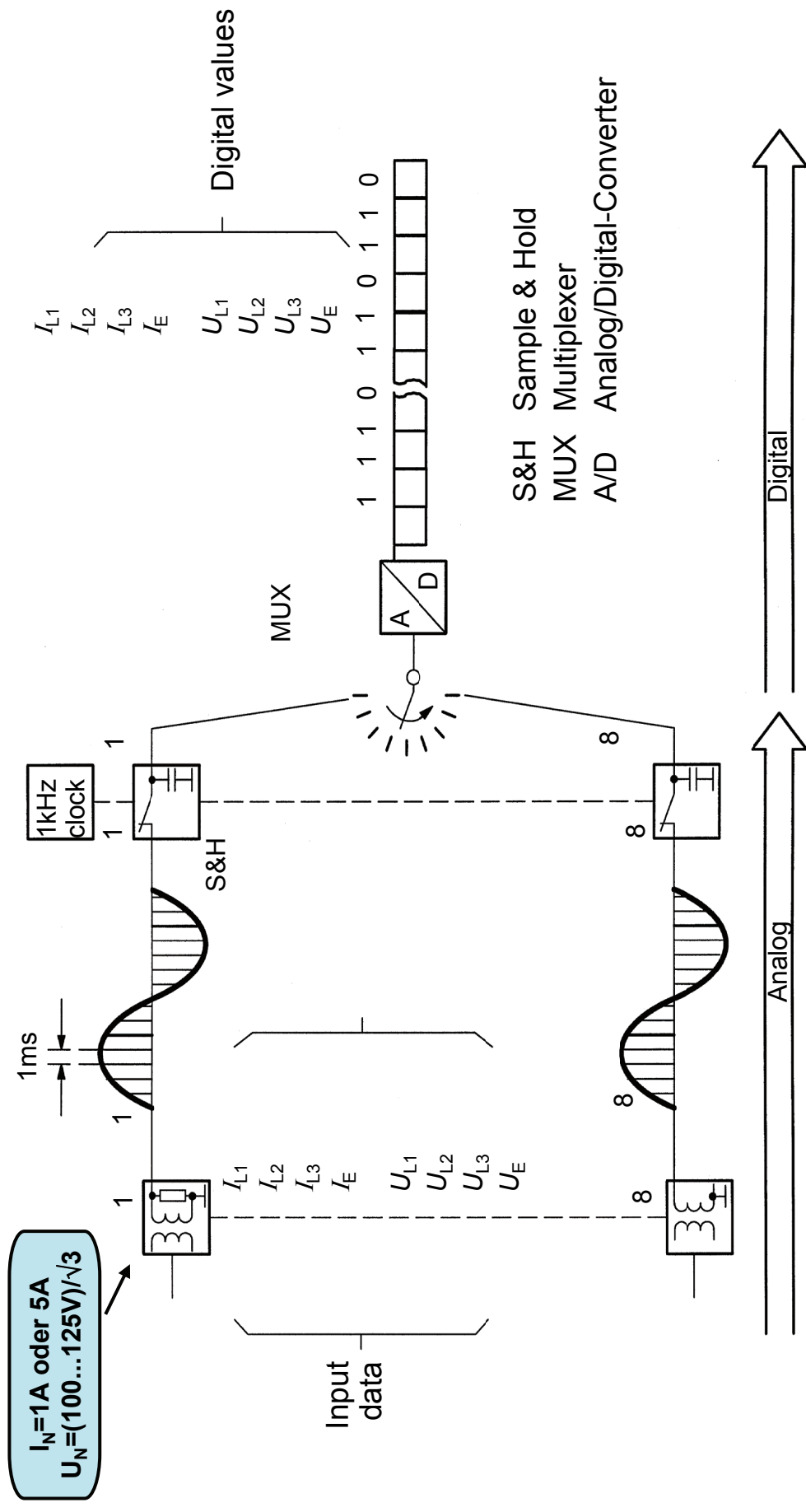
$$\underline{I}_{\text{Re lais}} = \underline{I}_{L1} - k_{E-\text{Re lais}} \cdot \underline{I}_E$$

$$\underline{Z}_{L1} = \frac{\underline{U}_{\text{Re lais}}}{\underline{I}_{\text{Re lais}}} = \frac{\underline{U}_{L1}}{\underline{I}_{L1} - k_{E-\text{Re lais}} \cdot \underline{I}_E} = \underline{Z}_L \quad \text{with}$$

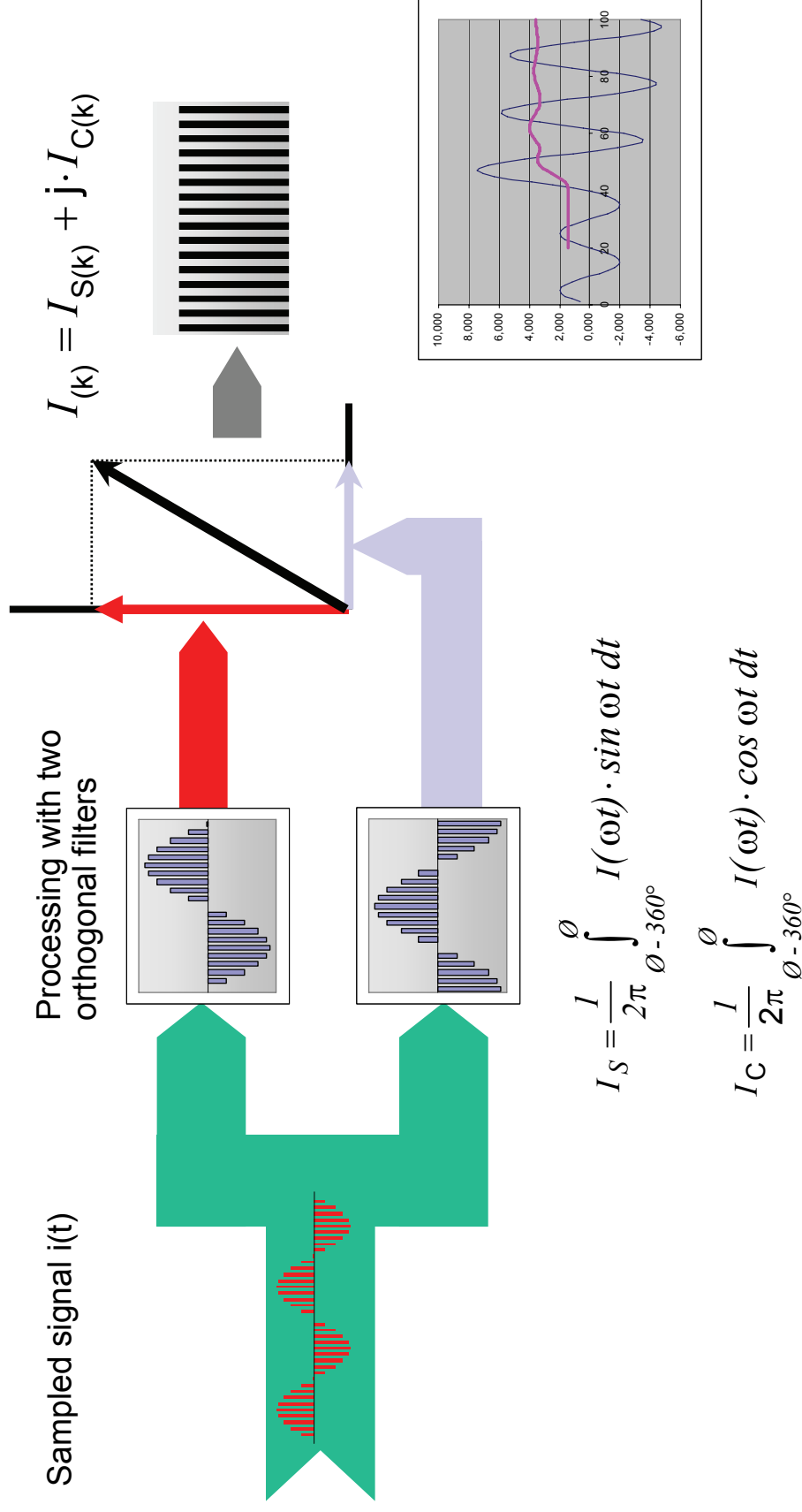


$$k_{E-\text{Re lais}} = \frac{\underline{Z}_E}{\underline{Z}_L} = \left| \frac{\underline{Z}_E}{\underline{Z}_L} \right| \cdot e^{j(\varphi_E - \varphi_L)}$$

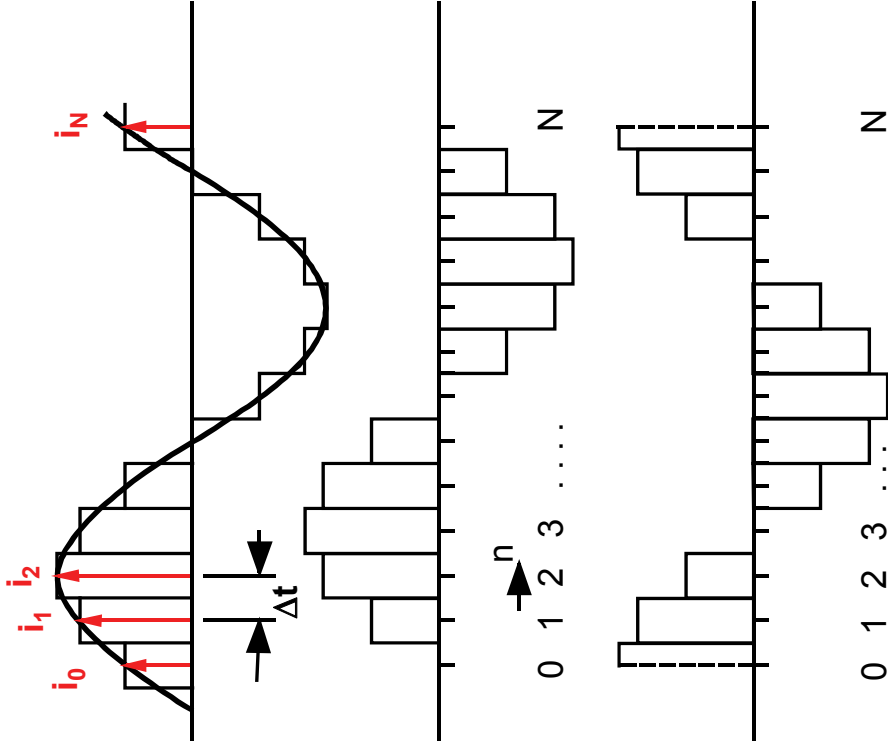
Capture of measuring data (principle)



Fourier analysis of measured values



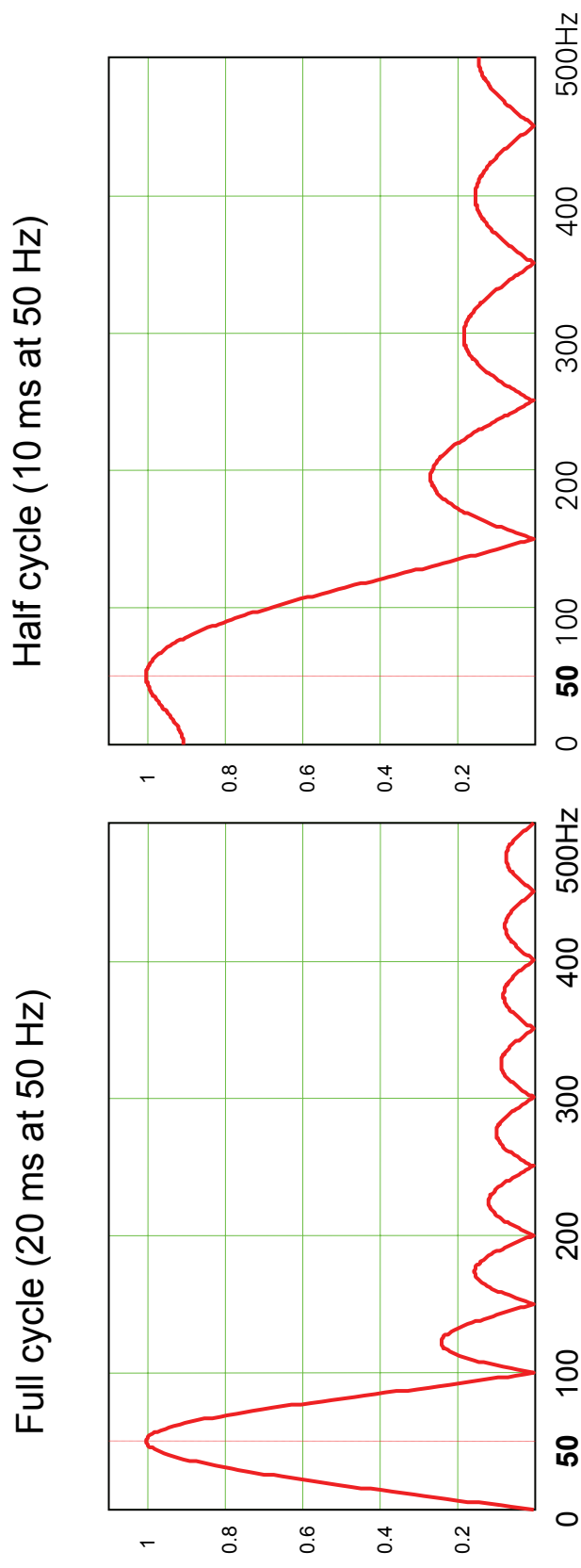
Discrete Fourier transform



$$I_s = \frac{2}{N} \left[\sum_{n=1}^{N-1} \sin(\omega \cdot n \cdot \Delta t) \cdot i_n \right]$$

$$I_c = \frac{2}{N} \left[\frac{i_0}{2} + \frac{i_N}{2} + \sum_{n=1}^{N-1} \cos(\omega \cdot n \cdot \Delta t) \cdot i_n \right]$$

Fourier analysis: Filtering characteristics



Determination of Voltage and current phasors

$$u_L(t) = R_L \cdot i_L(t) + L_L \cdot \frac{di_L(t)}{dt}$$

$$Re\{U_L\} = \frac{1}{T} \cdot \int_{-T/2}^{+T/2} u_L(t) \cdot \cos(\omega_0 \cdot t) dt$$

$$\text{Im}\{\underline{U}_L\} = \frac{1}{T} \cdot \int_{-T/2}^{+T/2} u_L(t) \cdot \sin(\omega_0 \cdot t) dt$$

$$U_{-L} = \text{Re}\{U_{-L}\} + j\text{Im}\{U_{-L}\}$$

$$\text{Re}\{I_{\underline{L}}\} = \frac{1}{T} \cdot \int_{-T/2}^{+T/2} i_{\underline{L}}(t) \cdot \cos(\omega_0 \cdot t) dt$$

$$Im\{I_{\perp}\} = \frac{1}{T} \int_{-T/2}^{+T/2} i_L(t) \cdot \sin(\omega_0 \cdot t) dt$$

$$I_{-L} = \text{Re}\{I_{-L}\} + j\text{Im}\{I_{-L}\}$$

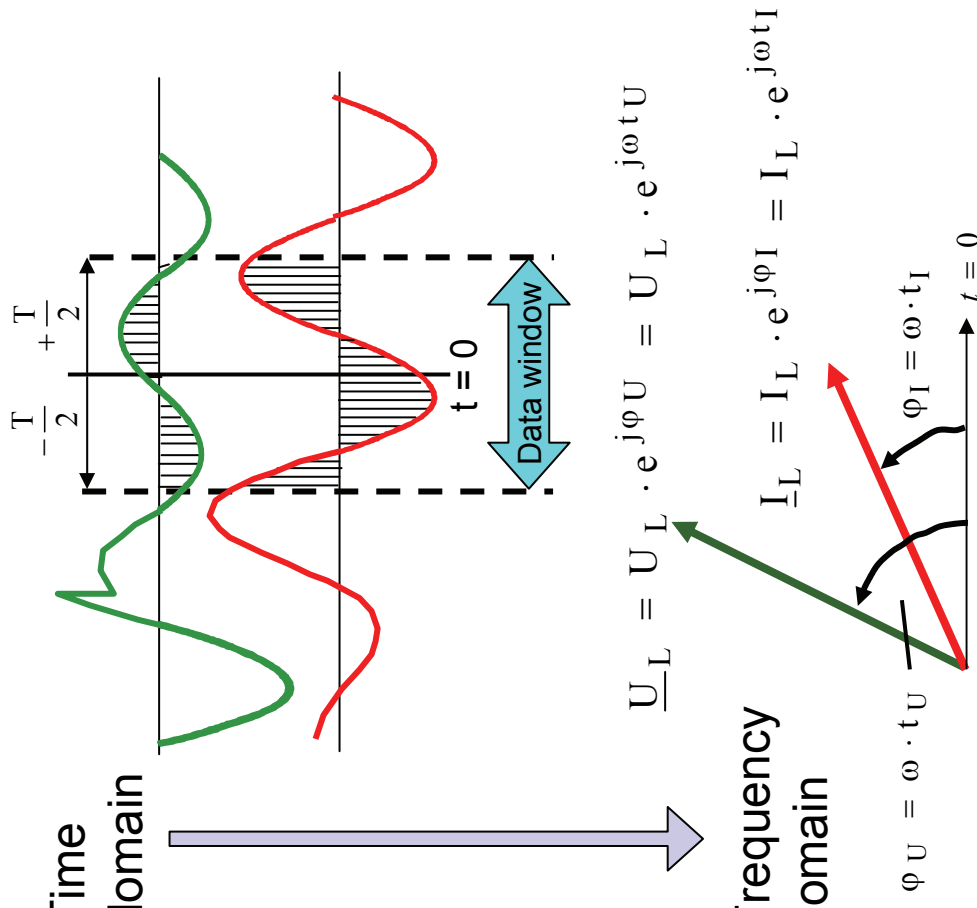
Time domain

Frequency
domain

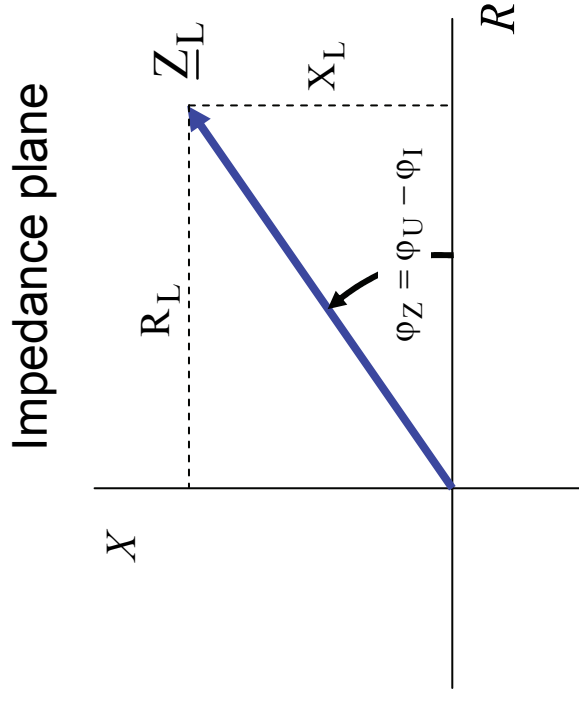
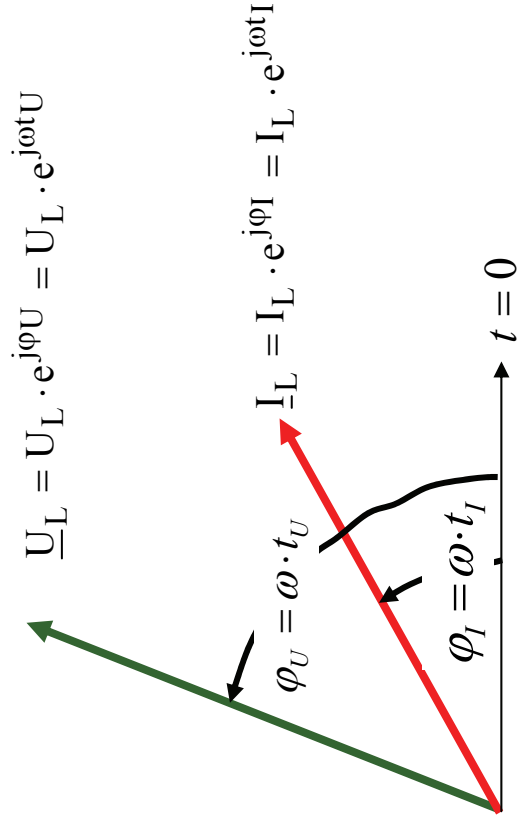
$$U_{\Gamma} = U_{\Gamma'} \cdot e^{j\varphi U} = U_{\Gamma'} \cdot e^{j\omega t U}$$

$$U_I = U_I \cdot [\cos(\omega \cdot t + \phi_U) + j \sin(\omega \cdot t + \phi_U)] = U_I \cdot e^{j(\omega \cdot t + \phi_U)}$$

$$I_{\Gamma} = I_{\Gamma} \cdot [\cos(\omega \cdot t + \varphi_1) + j \sin(\omega \cdot t + \varphi_1)] = I_{\Gamma} \cdot \mathbf{e}^{j(\omega \cdot t + \varphi_1)}$$



Fault impedance calculation from complex U- and I-phasors



$$\begin{aligned}
 \underline{Z}_L &= \frac{\underline{U}_L}{\underline{I}_L} = \frac{U_L \cdot e^{j\varphi_U}}{I_L \cdot e^{j\varphi_I}} = \frac{U_L}{I_L} \cdot e^{j(\varphi_U - \varphi_I)} \\
 &= R_L + jX_L
 \end{aligned}$$

$R_L = \operatorname{Re}\{\underline{Z}_L\} = \frac{U_L}{I_L} \cdot \cos(\varphi_U - \varphi_I)$
 $X_L = \operatorname{Im}\{\underline{Z}_L\} = \frac{U_L}{I_L} \cdot \sin(\varphi_U - \varphi_I)$

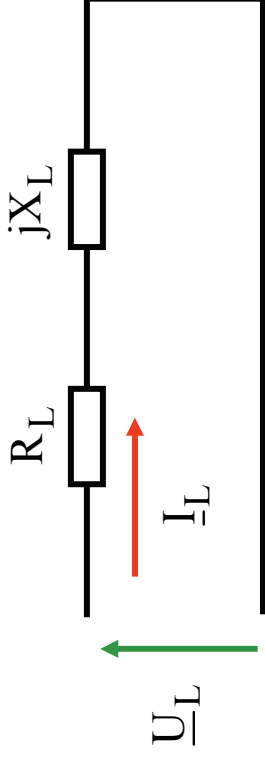
Calculation of R_L and X_L from separate real and imaginary fault loops

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$$\underline{U}_L = R_L \cdot \underline{I}_L + jX_L \cdot \underline{I}_L$$

$$\operatorname{Re}\{\underline{U}_L\} + j\operatorname{Im}\{\underline{U}_L\} = (R_L + jX_L) \cdot (\operatorname{Re}\{\underline{I}_L\} + j\operatorname{Im}\{\underline{I}_L\})$$

$$\begin{aligned}\operatorname{Re}\{\underline{U}_L\} &= R_L \cdot \operatorname{Re}\{\underline{I}_L\} - X_L \cdot \operatorname{Im}\{\underline{I}_L\} \\ \operatorname{Im}\{\underline{U}_L\} &= X_L \cdot \operatorname{Re}\{\underline{I}_L\} + R_L \cdot \operatorname{Im}\{\underline{I}_L\}\end{aligned}$$



$$X_L = \frac{\operatorname{Im}\{\underline{U}_L\} \cdot \operatorname{Re}\{\underline{I}_L\} - \operatorname{Re}\{\underline{U}_L\} \cdot \operatorname{Im}\{\underline{I}_L\}}{\operatorname{Re}\{\underline{I}_L\}^2 + \operatorname{Im}\{\underline{I}_L\}^2}$$

$$R_L = \frac{\operatorname{Re}\{\underline{U}_L\} \cdot \operatorname{Re}\{\underline{I}_L\} + \operatorname{Im}\{\underline{U}_L\} \cdot \operatorname{Im}\{\underline{I}_L\}}{\operatorname{Re}\{\underline{I}_L\}^2 + \operatorname{Im}\{\underline{I}_L\}^2}$$

$$\underline{U}_L = U_L \cdot e^{j(\omega \cdot t + \varphi_U)} = U_L \cdot [\cos(\omega \cdot t + \varphi_U) + j\sin(\omega \cdot t + \varphi_U)]$$

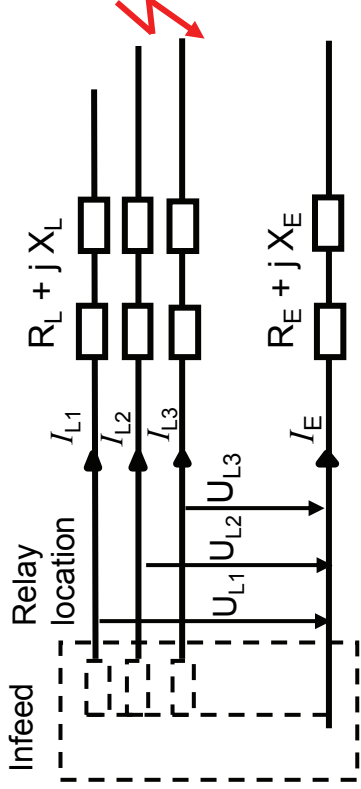
$$\underline{I}_L = I_L \cdot e^{j(\omega \cdot t + \varphi_I)} = I_L \cdot [\cos(\omega \cdot t + \varphi_I) + j\sin(\omega \cdot t + \varphi_I)]$$

$$X_L = \frac{U_L}{I_L} \cdot \sin(\varphi_{UL} - \varphi_{IL})$$

$$R_L = \frac{U_L}{I_L} \cdot \cos(\varphi_{UL} - \varphi_{IL})$$

$$\underline{Z}_L = R_L + jX_L$$

Complex fault impedance calculation compared to real and imaginary fault loop equation, Single-Ph-Ph fault



Complex impedance calculation:

$$\underline{Z}_{L2-L3} = \frac{\underline{U}_{L2} - \underline{U}_{L3}}{\underline{I}_{L2} - \underline{I}_{L3}}$$

For $\underline{I}_{L3} = -\underline{I}_{L2} = \underline{I}_{SC}$:

$$R_{L2-L3} = \frac{\underline{U}_{L2-L3} \cdot \cos \varphi_{SC}}{2 \cdot I_{SC}}$$

$$X_{L2-L3} = \frac{\underline{U}_{L2-L3} \cdot \sin \varphi_{SC}}{2 \cdot I_{SC}}$$

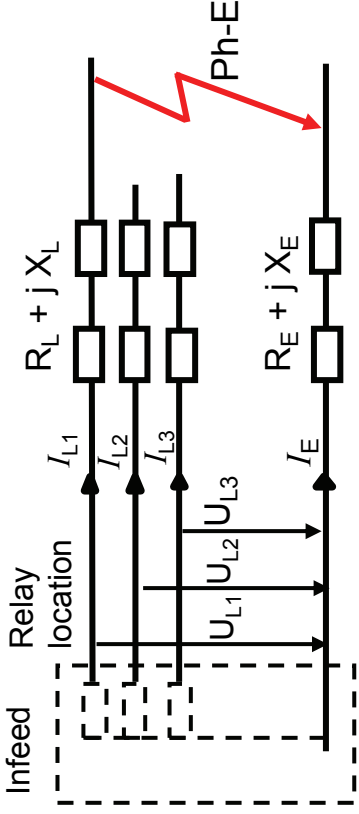
RL and XL calculation from real and imaginary fault loop equation:

$$X_L = \frac{\text{Im}\{\underline{U}_L\} \cdot \text{Re}\{\underline{I}_L\} - \text{Re}\{\underline{U}_L\} \cdot \text{Im}\{\underline{I}_L\}}{\text{Re}\{\underline{I}_L\}^2 + \text{Im}\{\underline{I}_L\}^2}$$

$$R_L = \frac{\text{Re}\{\underline{U}_L\} \cdot \text{Re}\{\underline{I}_L\} + \text{Im}\{\underline{U}_L\} \cdot \text{Im}\{\underline{I}_L\}}{\text{Re}\{\underline{I}_L\}^2 + \text{Im}\{\underline{I}_L\}^2}$$

$$\underline{U}_L = \underline{U}_{L2} - \underline{U}_{L3} \quad \text{and} \quad \underline{I}_L = \underline{I}_{L2} - \underline{I}_{L3}$$

Complex fault impedance calculation compared to real and imaginary fault loop evaluation, Single-Ph-E fault



Complex impedance calculation:

$$\underline{Z}_L = \frac{\underline{U}_L}{\underline{I}_L - \underline{k}_0 \cdot \underline{I}_E} \quad \underline{k}_0 = \frac{\underline{Z}_E}{\underline{Z}_L} = \frac{\underline{Z}_0 - \underline{Z}_1}{3 \cdot \underline{Z}_1}$$

For $\underline{I}_L = -\underline{I}_E = \underline{I}_{SC}$:

$$R_{Ph-E} = \frac{U_{Ph-E} \cdot \cos \varphi_{SC}}{I_{SC} \cdot (1 + \underline{k}_0)}$$

$$X_{Ph-E} = \frac{U_{Ph-E} \cdot \sin \varphi_{SC}}{I_{SC} \cdot (1 + \underline{k}_0)}$$

RL and XL calculation from real and imaginary fault loop equation:

$$R_{ph-E} = \frac{\operatorname{Re}\{\underline{U}_{ph-E}\} \cdot \operatorname{Re}\{\underline{I}_X\} + \operatorname{Im}\{\underline{U}_{ph-E}\} \cdot \operatorname{Im}\{\underline{I}_X\}}{\operatorname{Re}\{\underline{I}_R\} \cdot \operatorname{Re}\{\underline{I}_X\} + \operatorname{Im}\{\underline{I}_R\} \cdot \operatorname{Im}\{\underline{I}_X\}}$$

$$X_{ph-E} = \frac{\operatorname{Im}\{\underline{U}_{ph-E}\} \cdot \operatorname{Re}\{\underline{I}_R\} - \operatorname{Re}\{\underline{U}_{ph-E}\} \cdot \operatorname{Im}\{\underline{I}_R\}}{\operatorname{Re}\{\underline{I}_R\} \cdot \operatorname{Re}\{\underline{I}_X\} + \operatorname{Im}\{\underline{I}_R\} \cdot \operatorname{Im}\{\underline{I}_X\}}$$

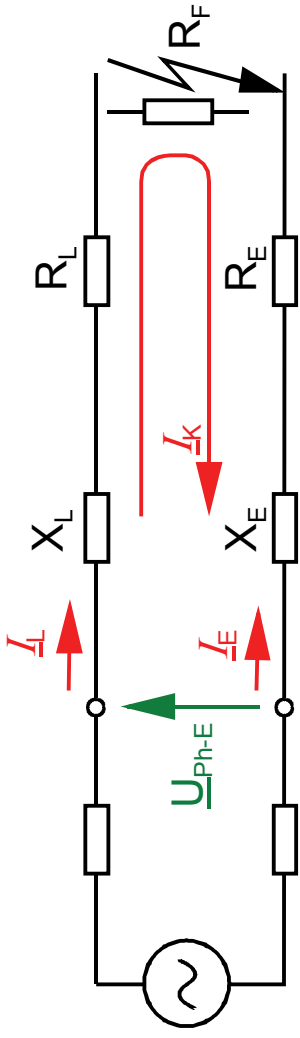
$$\underline{I}_R = \underline{I}_{ph} - \frac{R_E}{R_L} \cdot \underline{I}_E \quad \text{and} \quad \underline{I}_X = \underline{I}_{ph} - \frac{X_E}{X_L} \cdot \underline{I}_E$$

For $\underline{I}_L = -\underline{I}_E = \underline{I}_{SC}$:

$$R_{Ph-E} = \frac{U_{Ph-E} \cdot \cos \varphi_{SC}}{I_{SC} \left(1 + \frac{R_E}{R_L} \right)}$$

$$X_{Ph-E} = \frac{U_{Ph-E} \cdot \sin \varphi_{SC}}{I_{SC} \cdot \left(1 + \frac{X_E}{X_L} \right)}$$

Distance measurement (Ph-E-loop) - influence of fault resistance at separate residual compensation factors

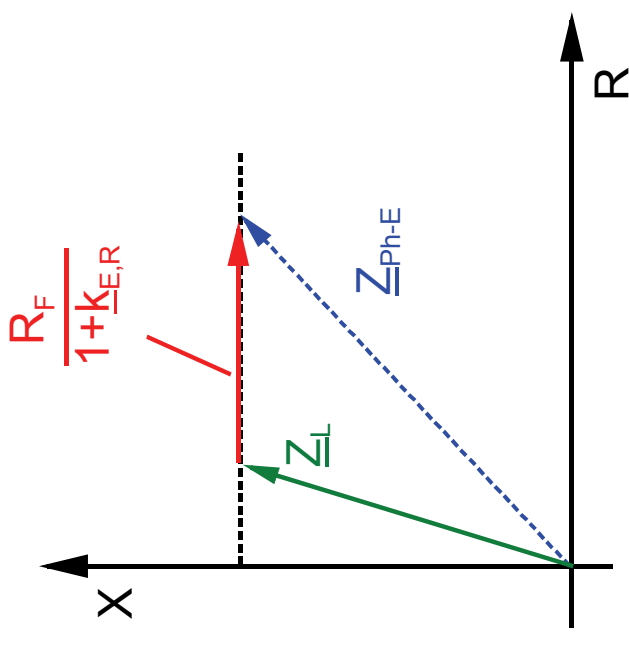


$$\underline{U}_{Ph-E} = \underline{I}_L (\underline{R}_L + j \underline{X}_L) - \underline{I}_E (\underline{R}_E + j \underline{X}_E) + R_F \cdot \underline{I}_L$$

$$\underline{X}_{Ph-E} = \frac{\text{Im} \left[\frac{\underline{U}_{Ph-E}}{\underline{I}_L} \right]}{1 + \frac{\underline{X}_E}{\underline{X}_L}} = \underline{X}_L$$

$$\underline{R}_{Ph-E} = \frac{\text{Re} \left[\frac{\underline{U}_{Ph-E}}{\underline{I}_L} \right]}{1 + \frac{\underline{R}_E}{\underline{R}_L}} = \underline{R}_L + \frac{R_F}{1 + k_{E,R}}$$

with $\underline{I}_E = -\underline{I}_L$

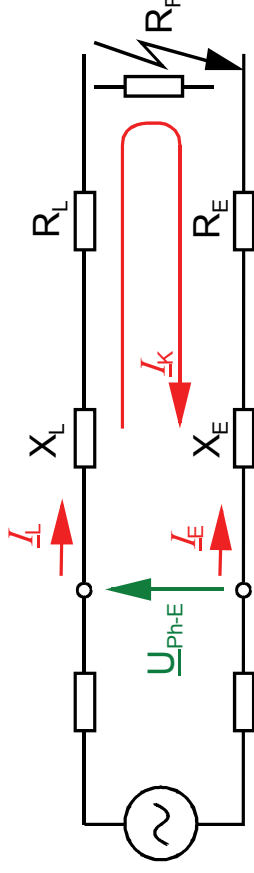


No measuring error in the X-direction

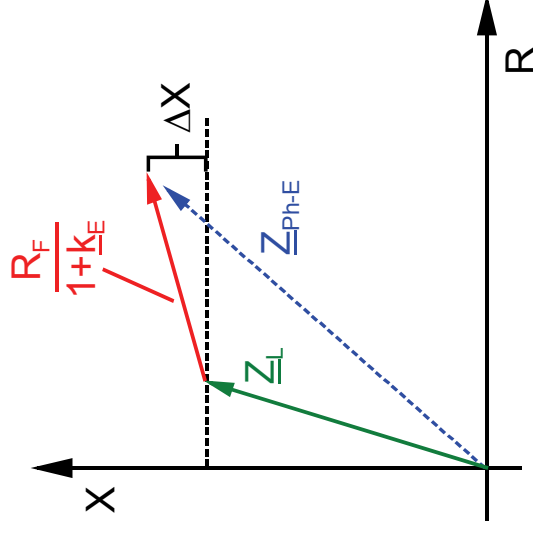


Distance measurement (Ph-E-loop) influence of fault resistance

SIEMENS



This method is not used by SIEMENS



$$\underline{U}_{\text{Ph} - \text{E}} = \underline{I}_L (\underline{Z}_L + \underline{Z}_E) + R_F \cdot \underline{I}_L \quad \text{assume} \quad \underline{I}_L = -\underline{I}_E$$

$$\underline{Z}_{\text{Ph} - \text{E}} = \frac{\underline{U}_{\text{Ph} - \text{E}}}{\underline{I}_L - k_E \cdot \underline{I}_E} = \underline{Z}_L \cdot \frac{1 + \frac{\underline{Z}_E}{\underline{Z}_L}}{1 + k_E} + \frac{R_F}{1 + k_E}$$

If k_E setting adapted to $\frac{\underline{Z}_E}{\underline{Z}_L}$, then $\underline{Z}_{\text{Ph} - \text{E}} = \underline{Z}_L + \frac{R_F}{1 + \frac{\underline{Z}_E}{\underline{Z}_L}} = \underline{Z}_L + \frac{R_F}{1 + \left| \frac{\underline{Z}_E}{\underline{Z}_L} \right| \cdot e^{j(\varphi_E - \varphi_L)}}$

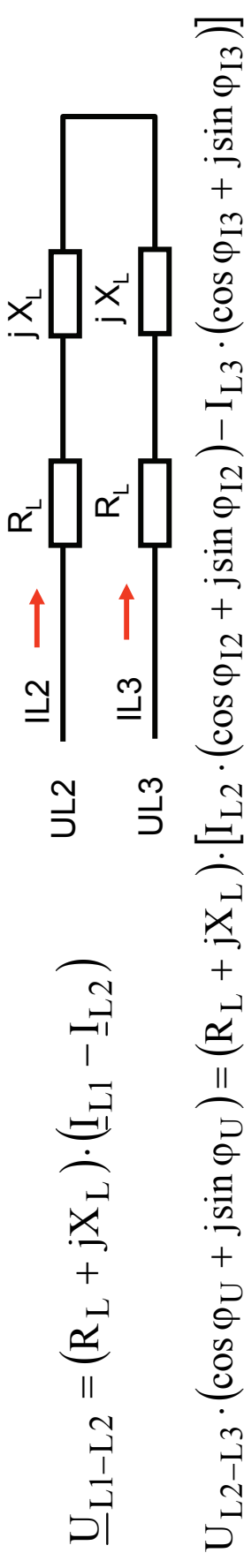


Also an additional measuring error in the X-direction

Numerical Impedance calculation (7SA5, 7SA6)

Evaluation of the complex Ph-Ph fault loop equation

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$$U_{L2-L3} \cdot \cos \varphi_U = R_L \cdot (I_{L2} \cdot \cos \varphi_{I2} - I_{L3} \cdot \cos \varphi_{I3}) - X_L \cdot (I_{L2} \cdot \sin \varphi_{I2} - I_{L3} \cdot \sin \varphi_{I3})$$

$$U_{L2-L3} \cdot \sin \varphi_U = R_L \cdot (I_{L2} \cdot \sin \varphi_{I2} - I_{L3} \cdot \sin \varphi_{I3}) + X_L \cdot (I_{L2} \cdot \cos \varphi_{I2} - I_{L3} \cdot \cos \varphi_{I3})$$

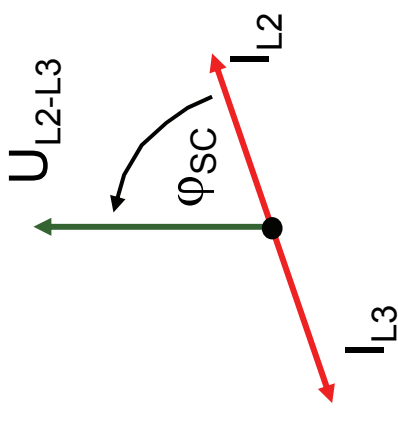
$$R_{L2-L3} = \frac{U_{L2-L3} [I_{L2} \cdot \cos(\varphi_{UL2-L3} - \varphi_{IL2}) - I_{L3} \cdot \cos(\varphi_{UL2-L3} - \varphi_{IL3})]}{I_{L2}^2 - 2 \cdot I_{L2} \cdot I_{L3} \cdot \cos(\varphi_{IL2} - \varphi_{IL3}) + I_{L3}^2}$$

$$X_{L2-L3} = \frac{U_{L2-L3} [I_{L2} \cdot \sin(\varphi_{UL2-L3} - \varphi_{IL2}) - I_{L3} \cdot \sin(\varphi_{UL2-L3} - \varphi_{IL3})]}{I_{L2}^2 - 2 \cdot I_{L2} \cdot I_{L3} \cdot \cos(\varphi_{IL2} - \varphi_{IL3}) + I_{L3}^2}$$

With $\varphi_{IL2} = 0$ and $I_{L3} = -I_{L2} \cdot \varphi_{IL3} = -\varphi_{IL2} = 180^\circ$, and $\varphi_{UL2-L3} = \varphi_{SC}$:

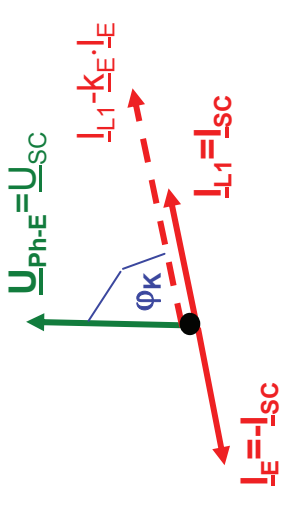
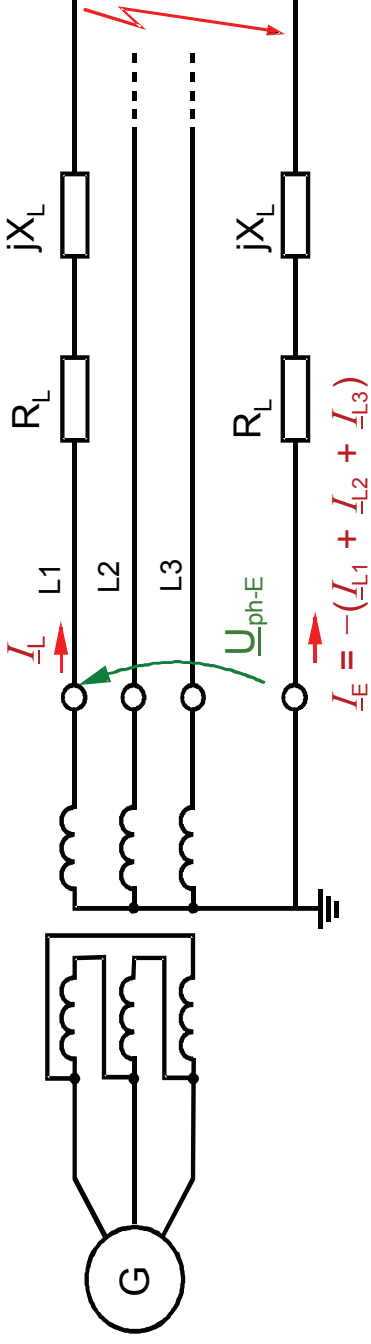
$$R_{L2-L3} = \frac{U_{L2-L3} \cdot \cos \varphi_{SC}}{I_{L2} - I_{L3}}$$

$$X_{L2-L3} = \frac{U_{L2-L3} \cdot \sin \varphi_{SC}}{I_{L2} - I_{L3}}$$



Numerical Impedance calculation (7SA5, 7SA6)

Evaluation of the complex Ph-E fault loop equation



With $\varphi_{IL} = 0$, $\varphi_{IE} = -\varphi_{IL} = 180^\circ$ and $\varphi_U = \varphi_K$:

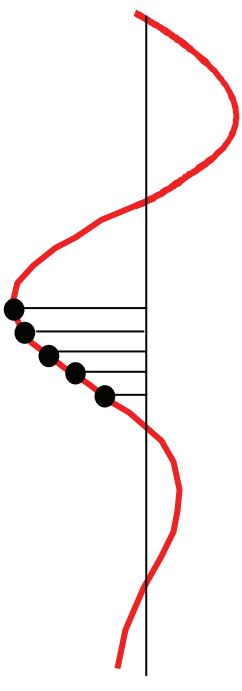
$$X_{Ph-E} = \frac{U_{Ph-E}}{I_L} \cdot \frac{\sin(\varphi_U - \varphi_{IL}) - \frac{I_E}{I_L} \cdot \frac{R_E}{R_L} \cdot \sin(\varphi_U - \varphi_{IE})}{1 - \left(\frac{X_E}{X_L} + \frac{R_E}{R_L} \right) \cdot \frac{I_E}{I_L} \cdot \cos(\varphi_{IE} - \varphi_{IL}) + \frac{R_E}{R_L} \cdot \frac{X_E}{X_L} \cdot \left(\frac{I_E}{I_L} \right)^2}$$

$$X_{Ph-E} = \frac{U_{Ph-E} \cdot \sin \varphi_K}{I_L + \frac{X_E}{X_L} \cdot I_E}$$

$$R_{Ph-E} = \frac{U_{Ph-E}}{I_L} \cdot \frac{\cos(\varphi_U - \varphi_{IL}) - \frac{I_E}{I_L} \cdot \frac{X_E}{X_L} \cdot \cos(\varphi_U - \varphi_{IE})}{1 - \left(\frac{X_E}{X_L} + \frac{R_E}{R_L} \right) \cdot \frac{I_E}{I_L} \cdot \cos(\varphi_{IE} - \varphi_{IL}) + \frac{R_E}{R_L} \cdot \frac{X_E}{X_L} \cdot \left(\frac{I_E}{I_L} \right)^2}$$

$$R_{Ph-E} = \frac{U_{Ph-E} \cdot \cos \varphi_K}{I_L + \frac{R_E}{R_L} \cdot I_E}$$

$$i_{(t)} = A \cdot \sin(\omega t) + B \cdot \cos(\omega t) - e^{-\frac{t}{\tau}} + C \cdot \cos(\omega t)$$



Task: Estimation of the coefficients A , B , C and τ on basis of measured current samples

Method: Gauß's *Minimization of error squares*:

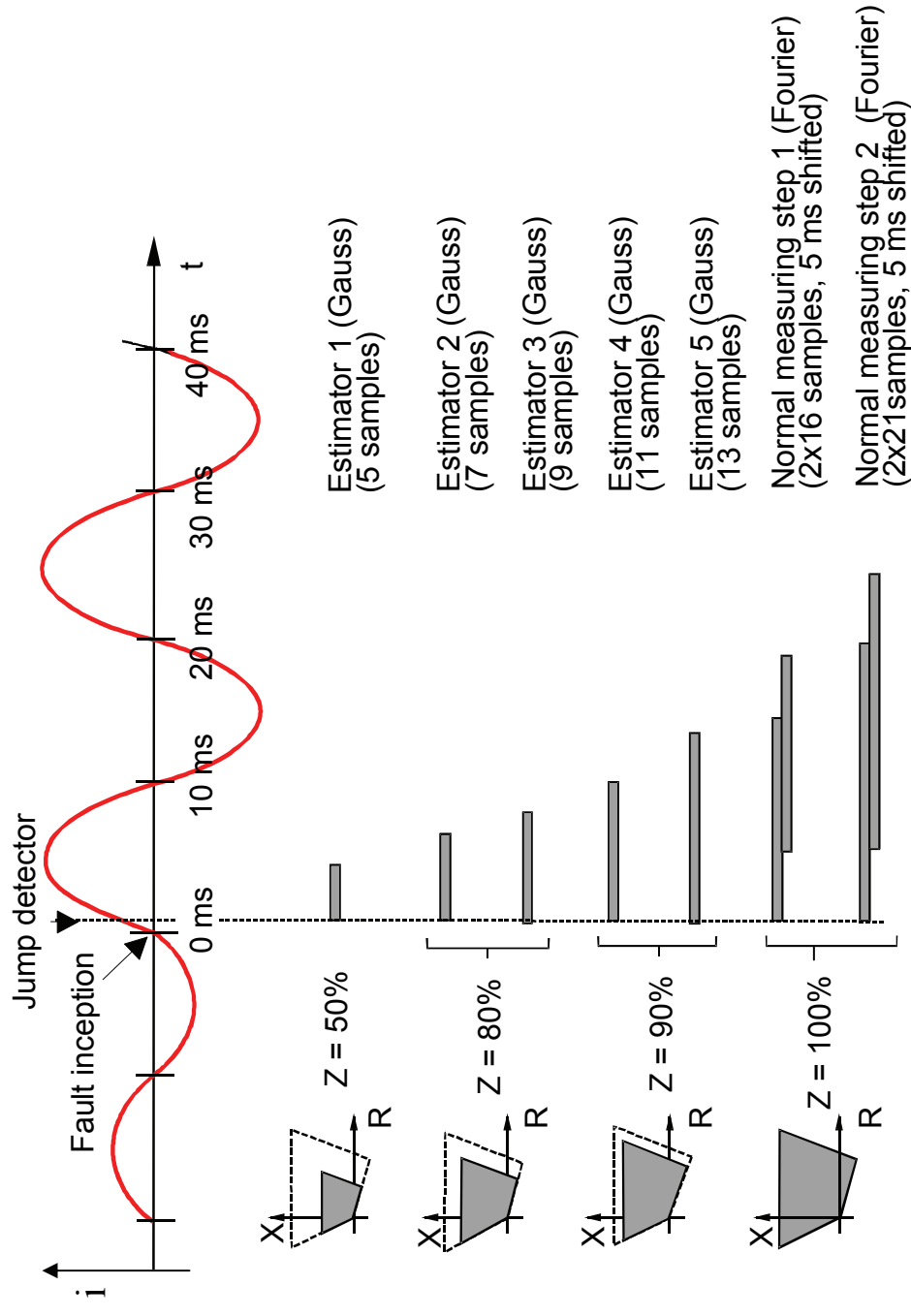
$$\Delta = \sum_{i=k-N}^k \left(u_{(i)} - f_{(i)} \right)^2 \rightarrow \text{MIN}$$



$$\frac{\Delta}{dA \, dB \, dC \, d\tau} = 0$$

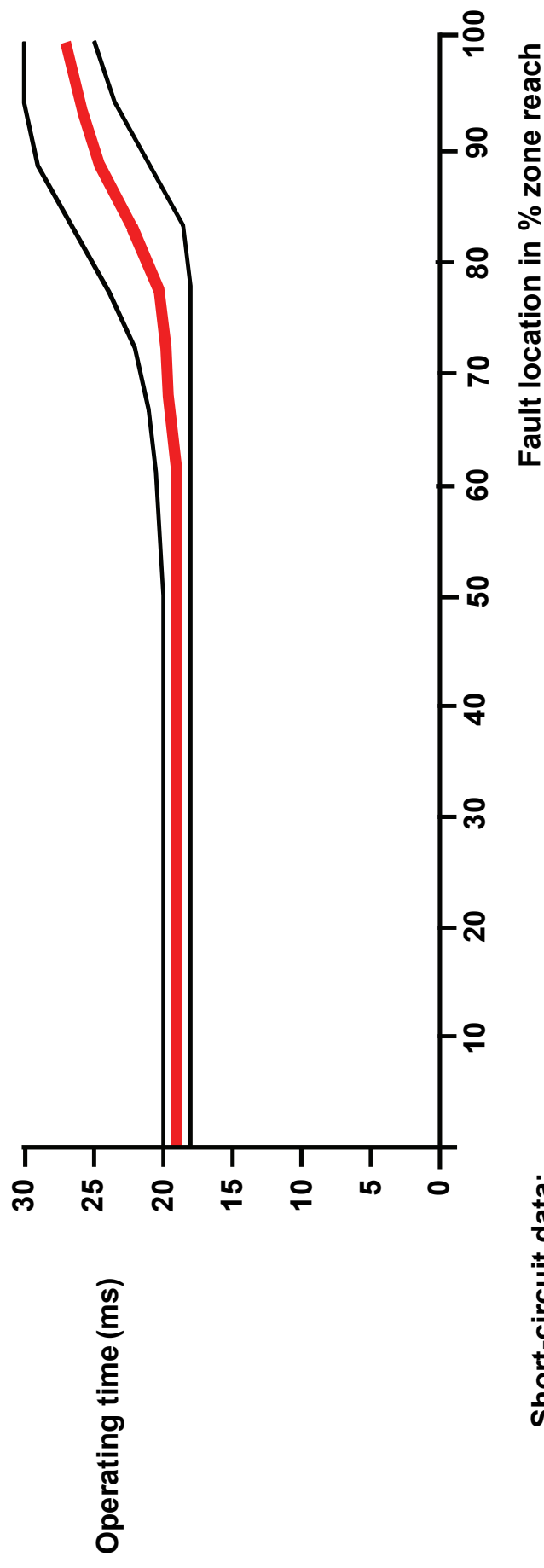
Δ = quality value
 k = sampling number
 N = length of data window
 i = variable

Distance protection: Adaptive measuring method



Distance protection, Typical operating time characteristic

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Short-circuit data:

SIR = 26

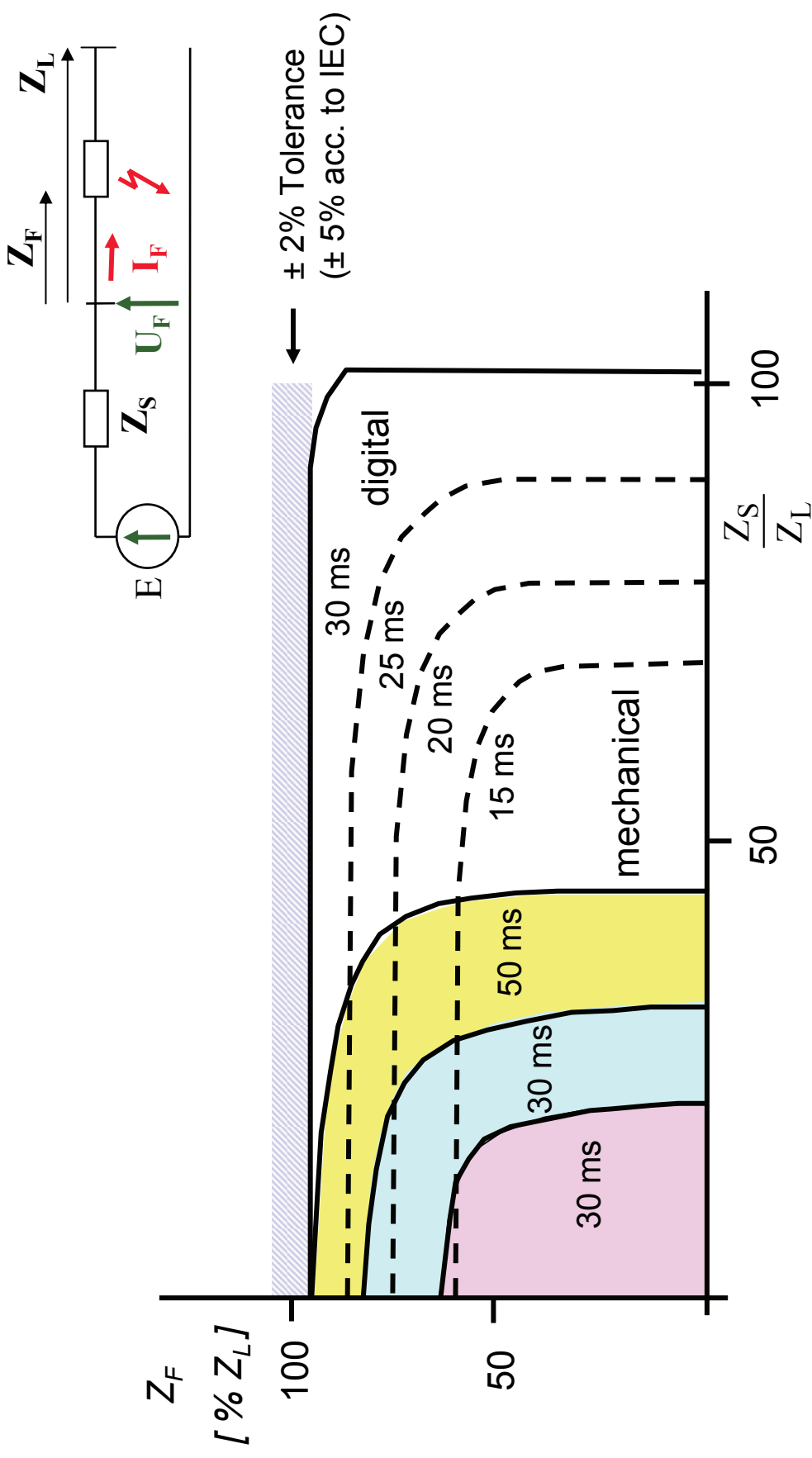
f = 50 Hz

Fault: L1-E

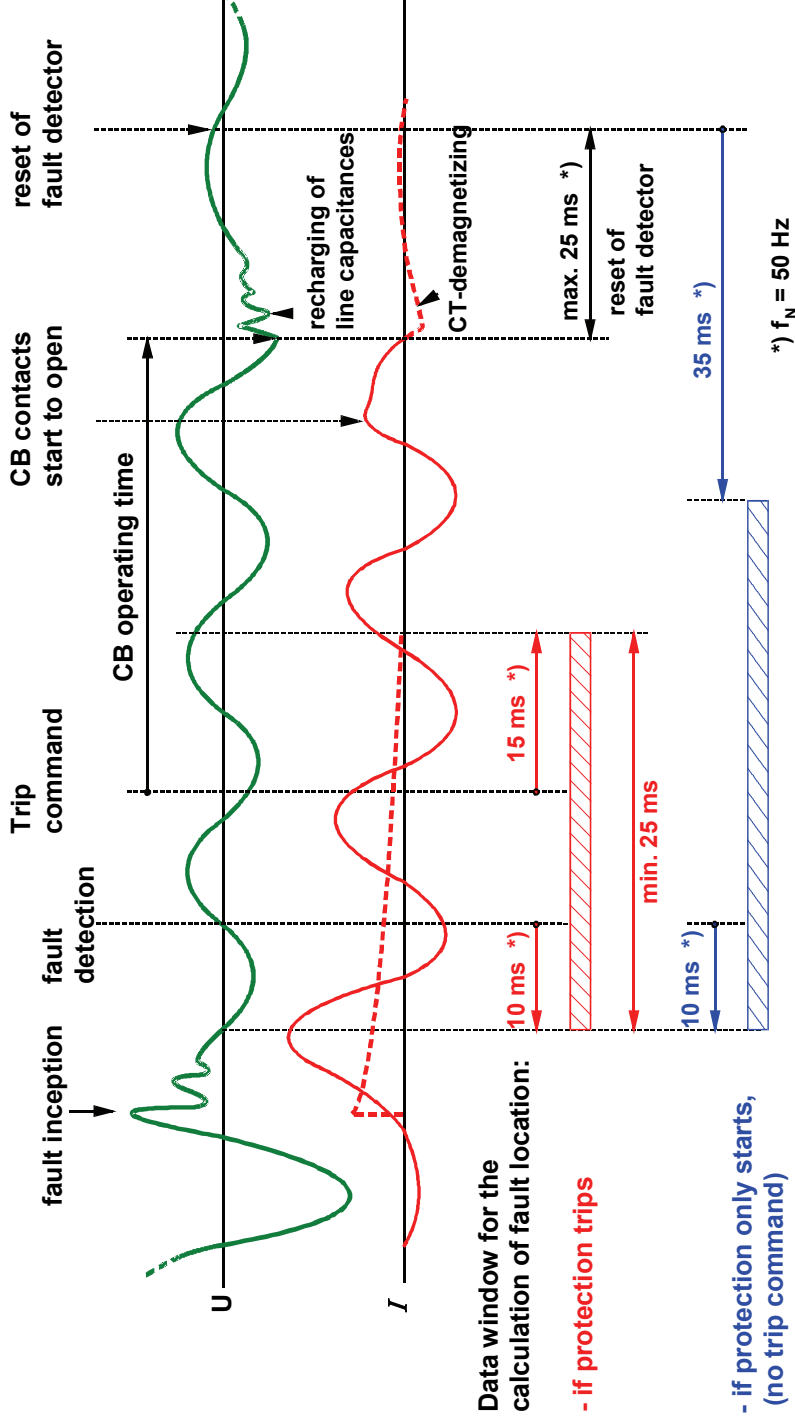
5 shots per fault case

Fault inception: 0° ... 90°

Contour diagram of distance relay performance

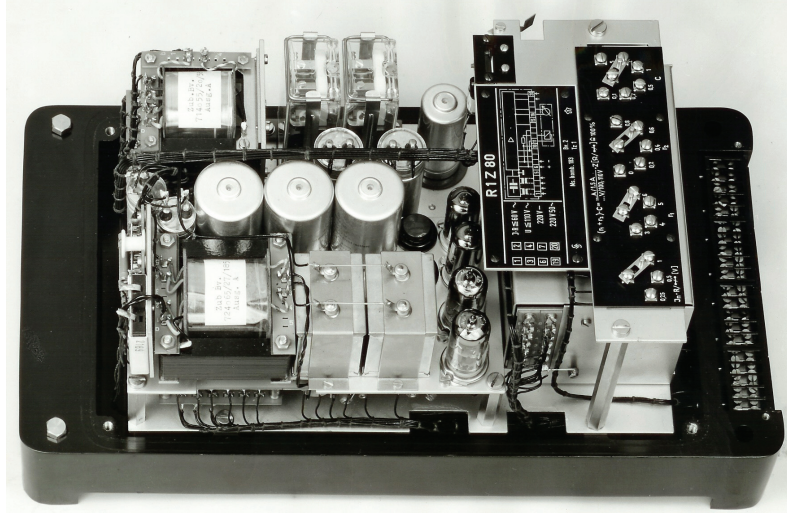


Placing of data window for distance to fault computation

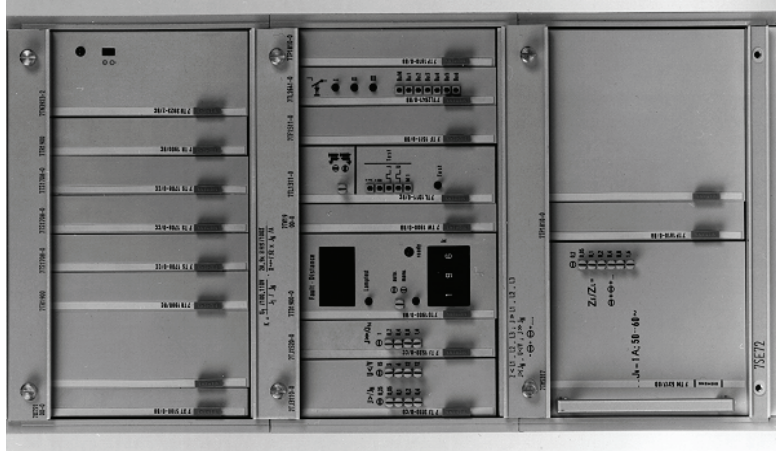


Historic fault locator relays

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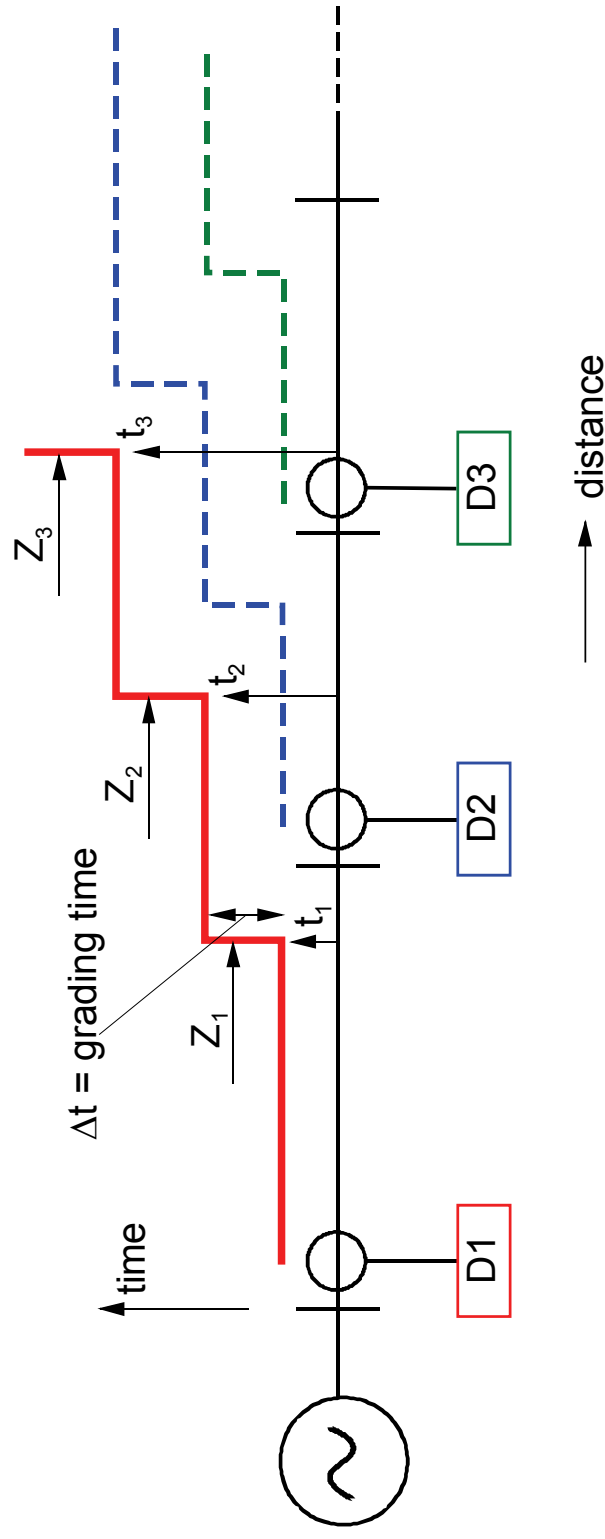
Electromechanical
(with cold cathode tubes)



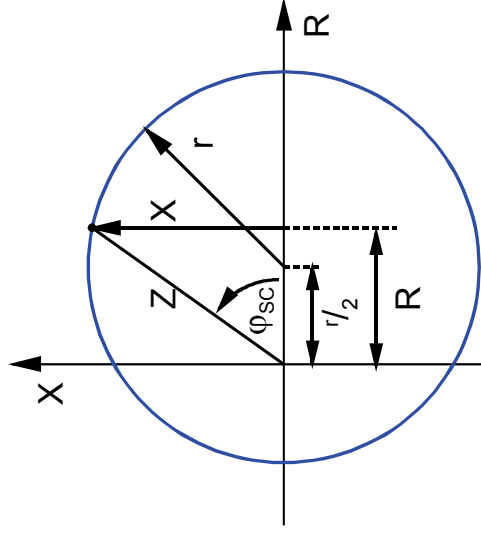
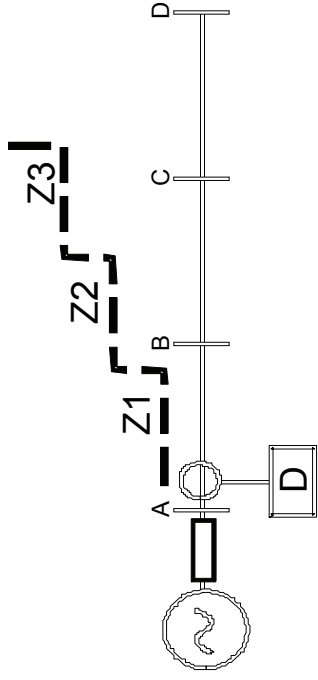
Static (electronic)

Graded distance zones

SIEMENS

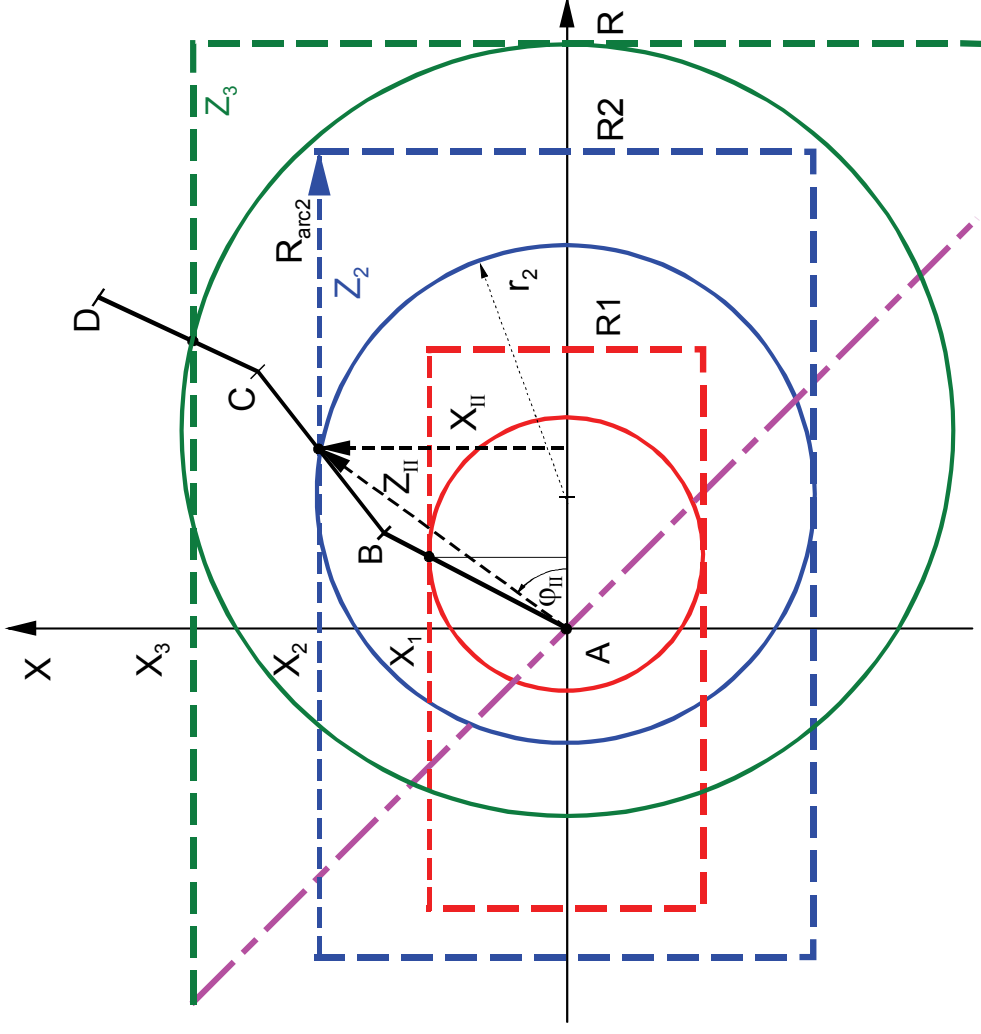


Distance zone setting - electromechanical and digital

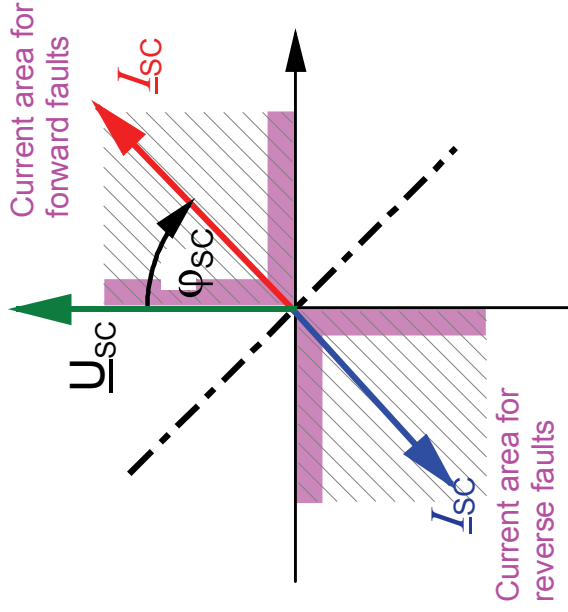


$$r = \frac{-R \pm \sqrt{R^2 + 3 \cdot Z^2}}{3/2}$$

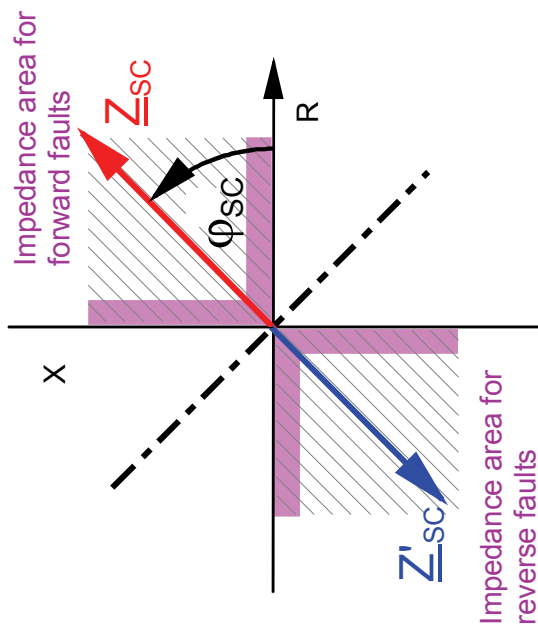
electro-mechanical



Determination of fault direction



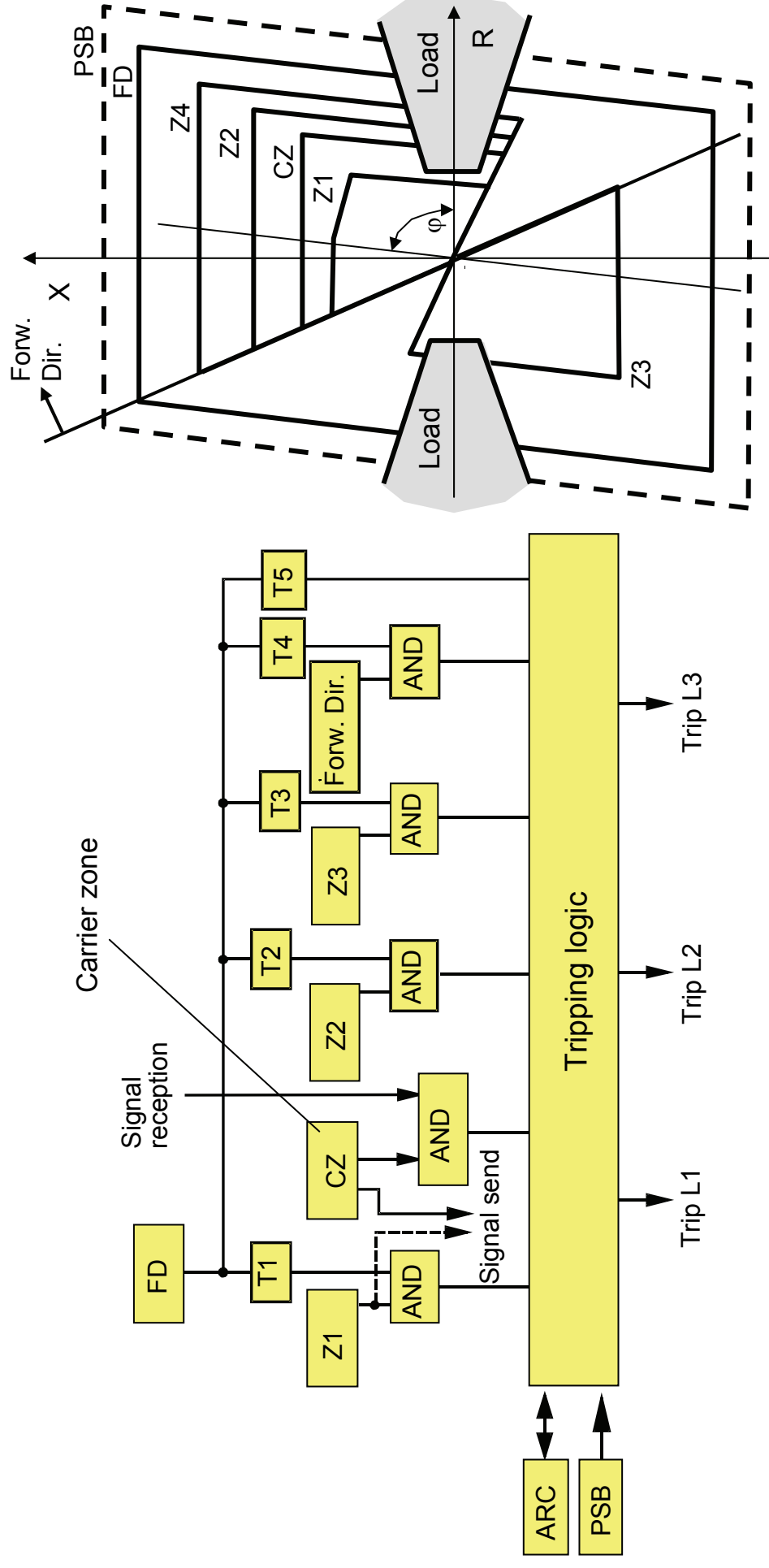
current / voltage diagram



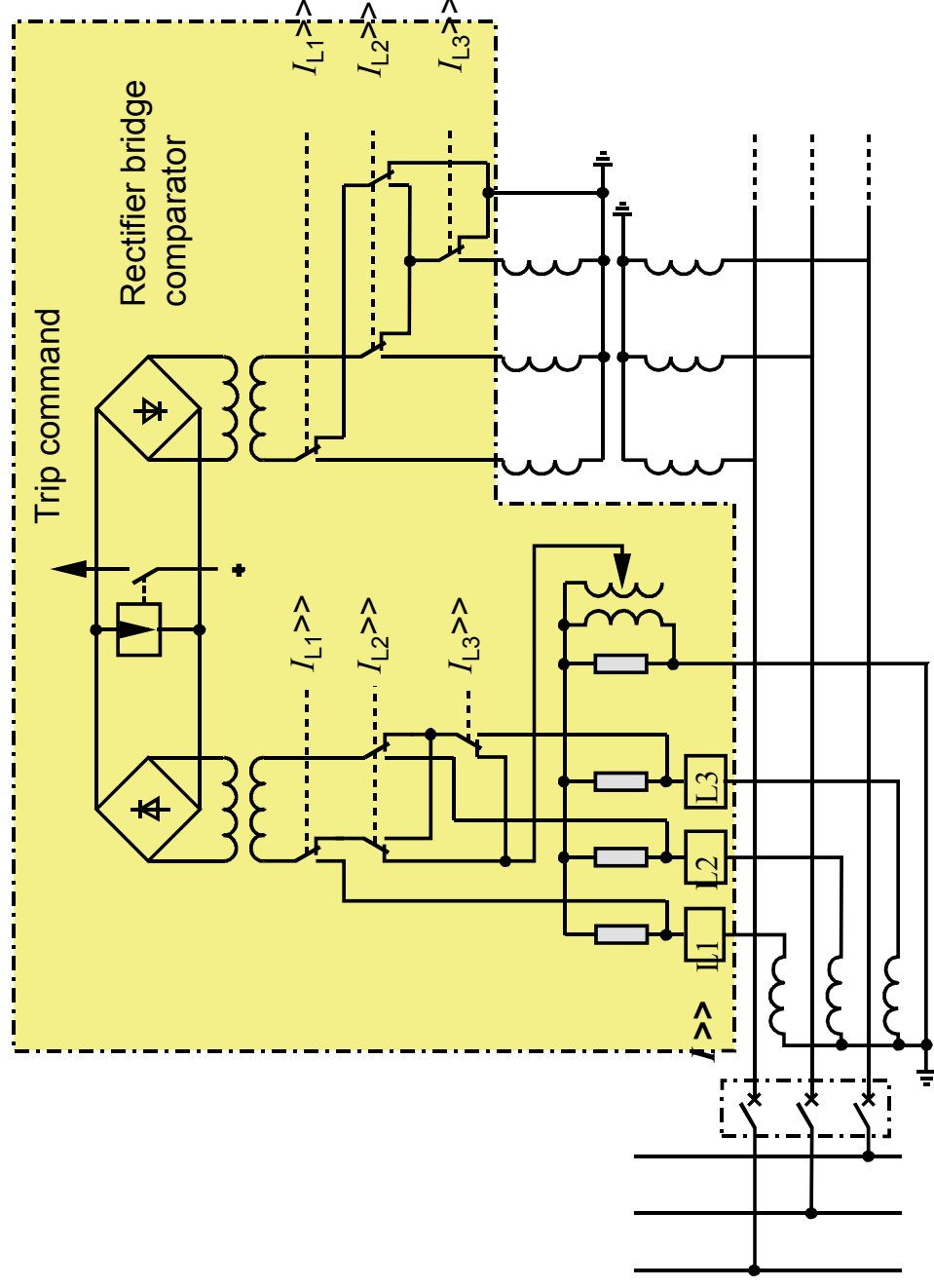
impedance diagram

Distance protection, fault detector controlled timing

SIEMENS

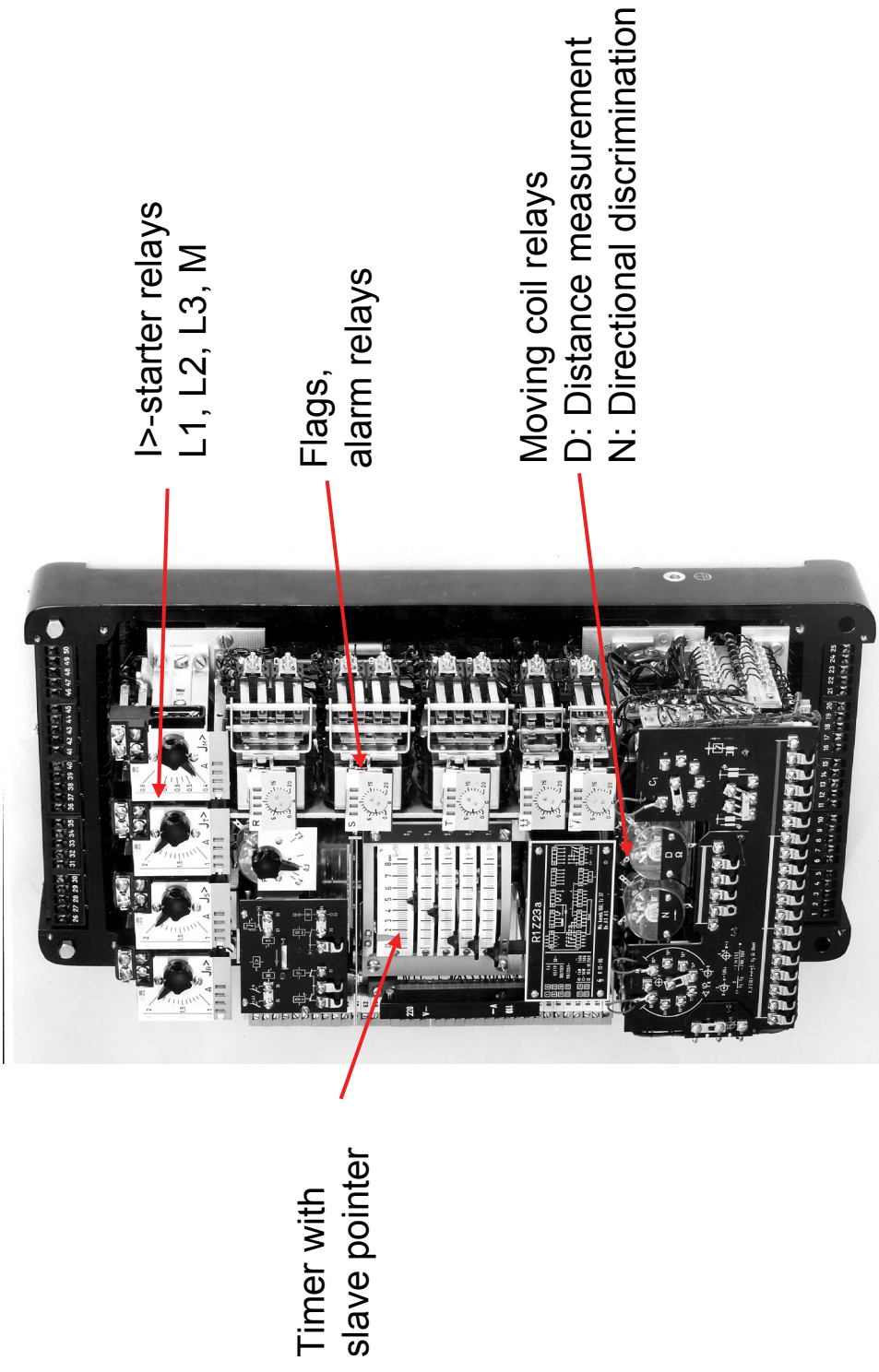


Electro-mechanical switched distance protection (principle of measured value switching)



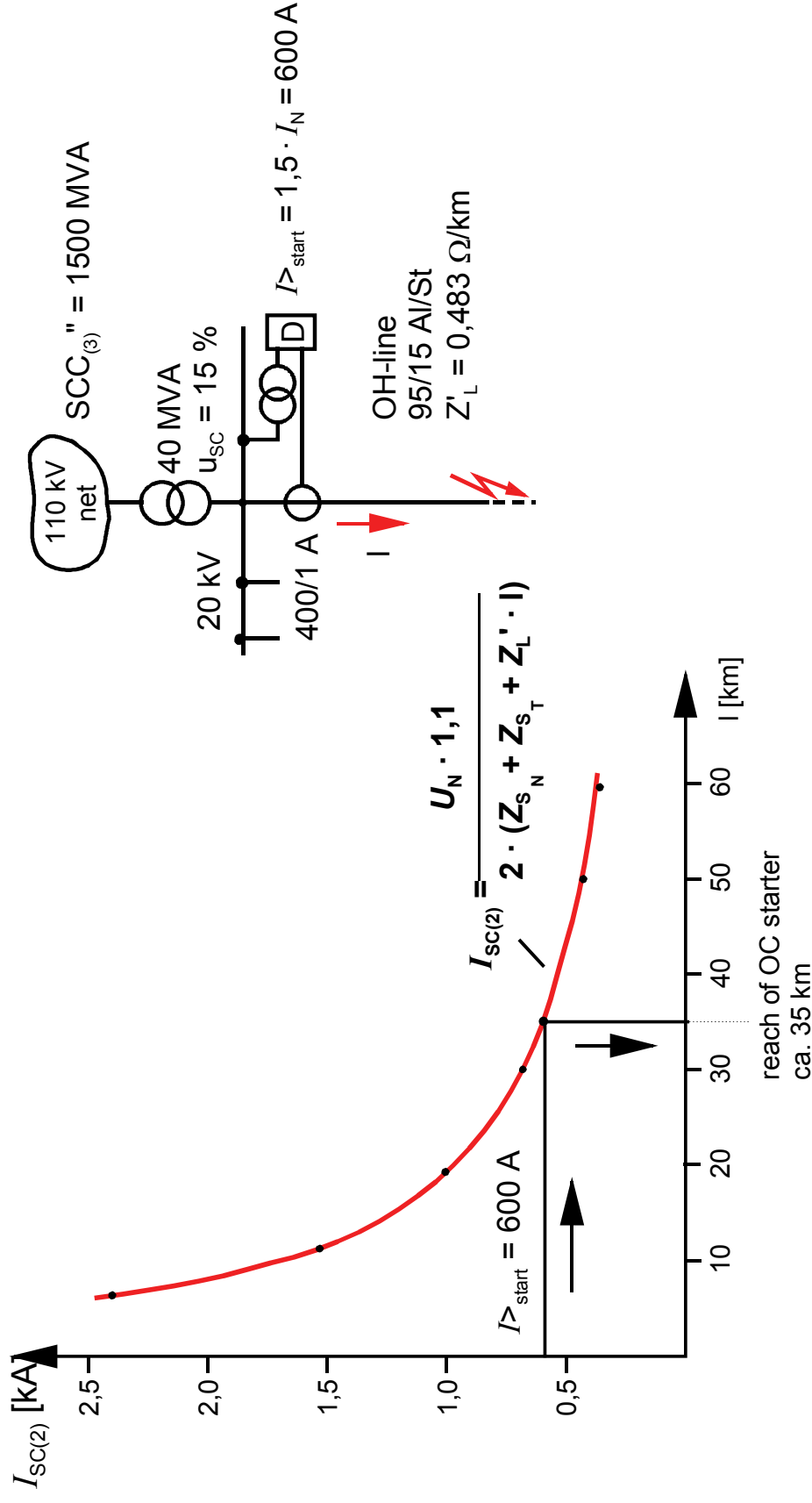
Electro-mechanical switched distance protection (Version for subtransmission networks)

SIEMENS



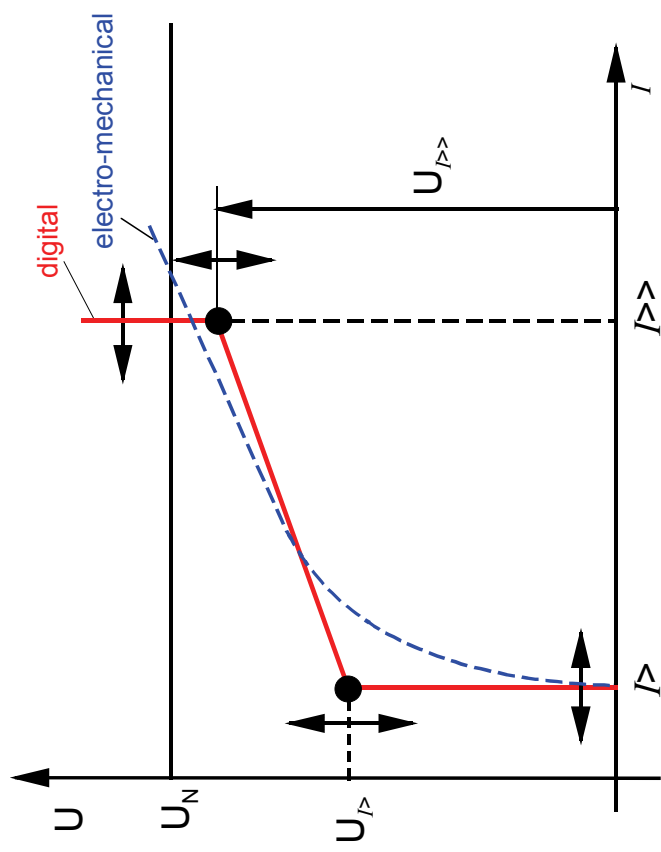
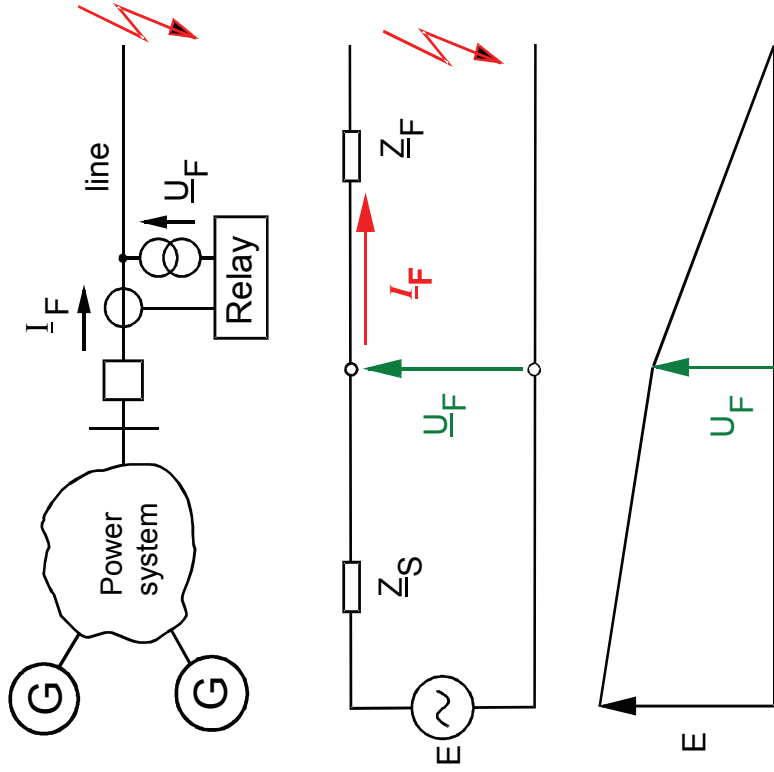
Reach of overcurrent starter ph-ph fault as an example

SIEMENS

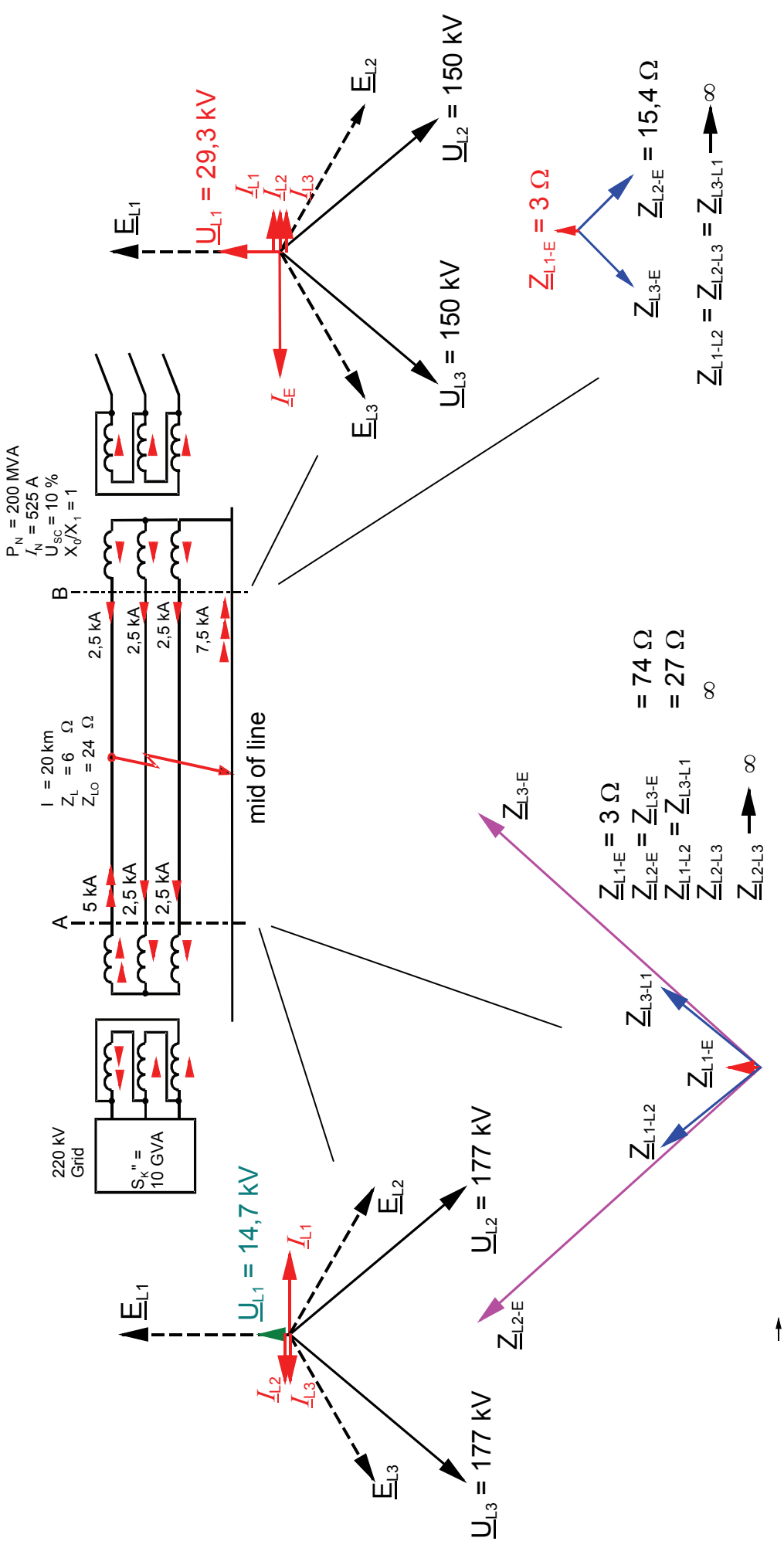


Voltage controlled overcurrent starter

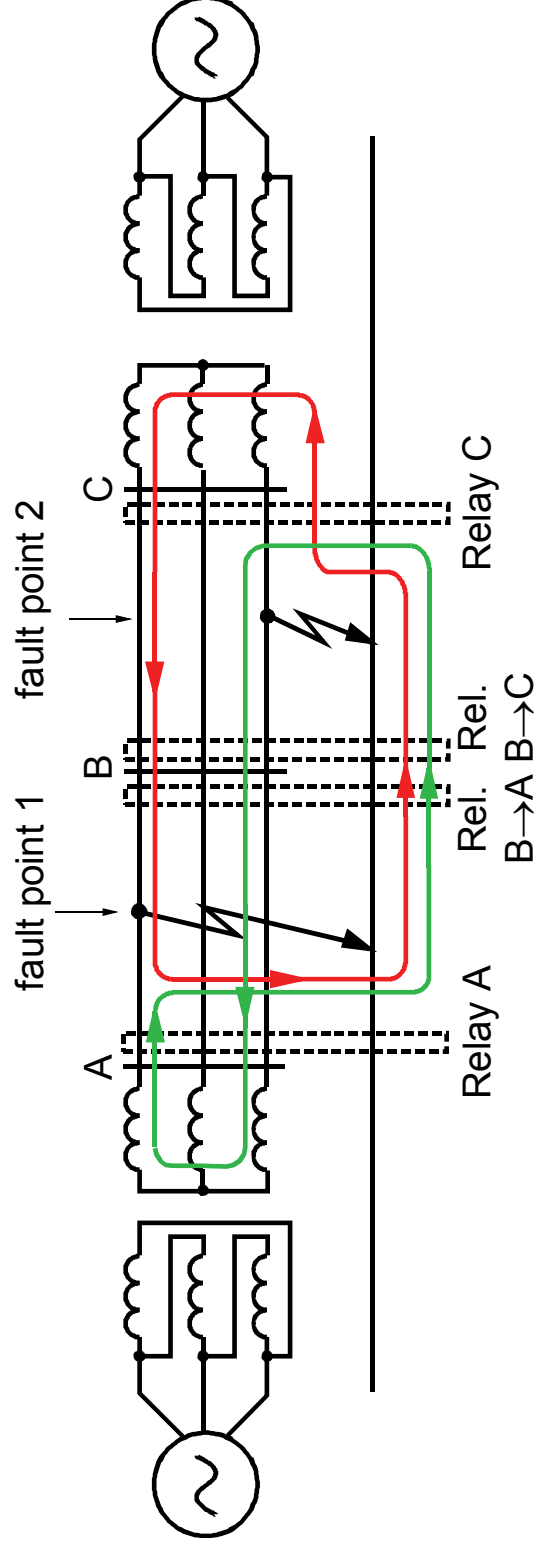
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Short circuit in an effectively earthed system with unequal source and earthing conditions

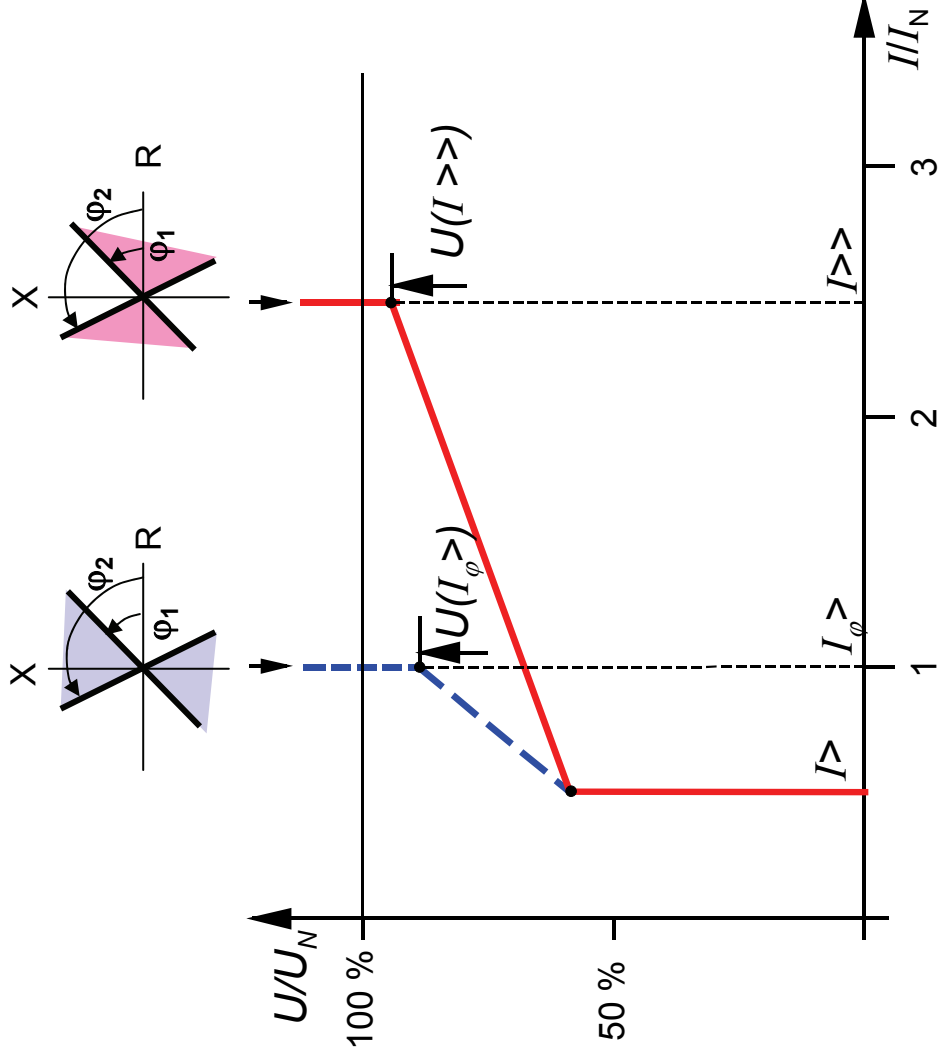


Cross country earth fault in the isolated/compensated network

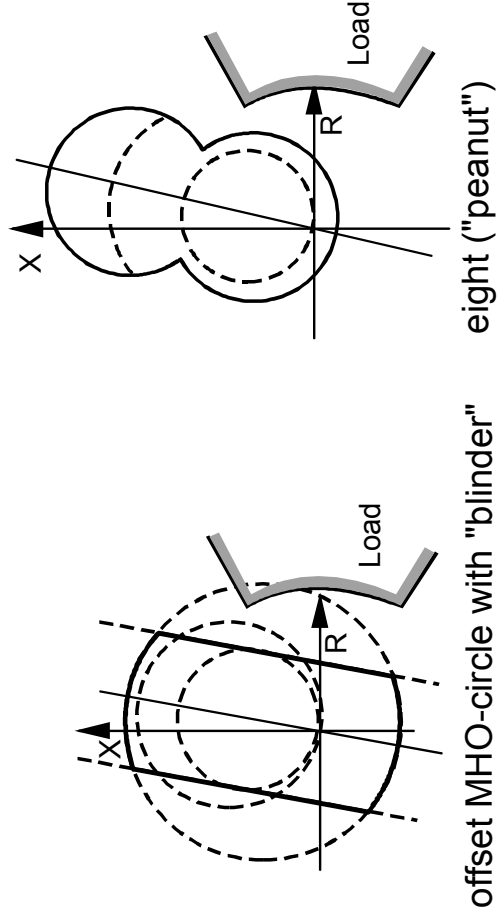
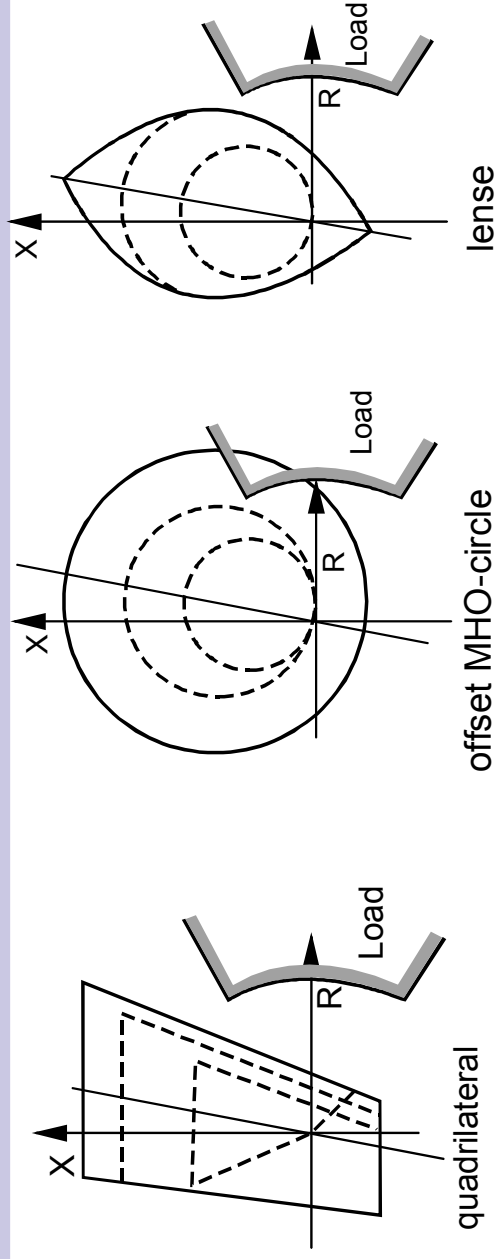


Voltage and angle controlled overcurrent starter (U-I- φ -starting)

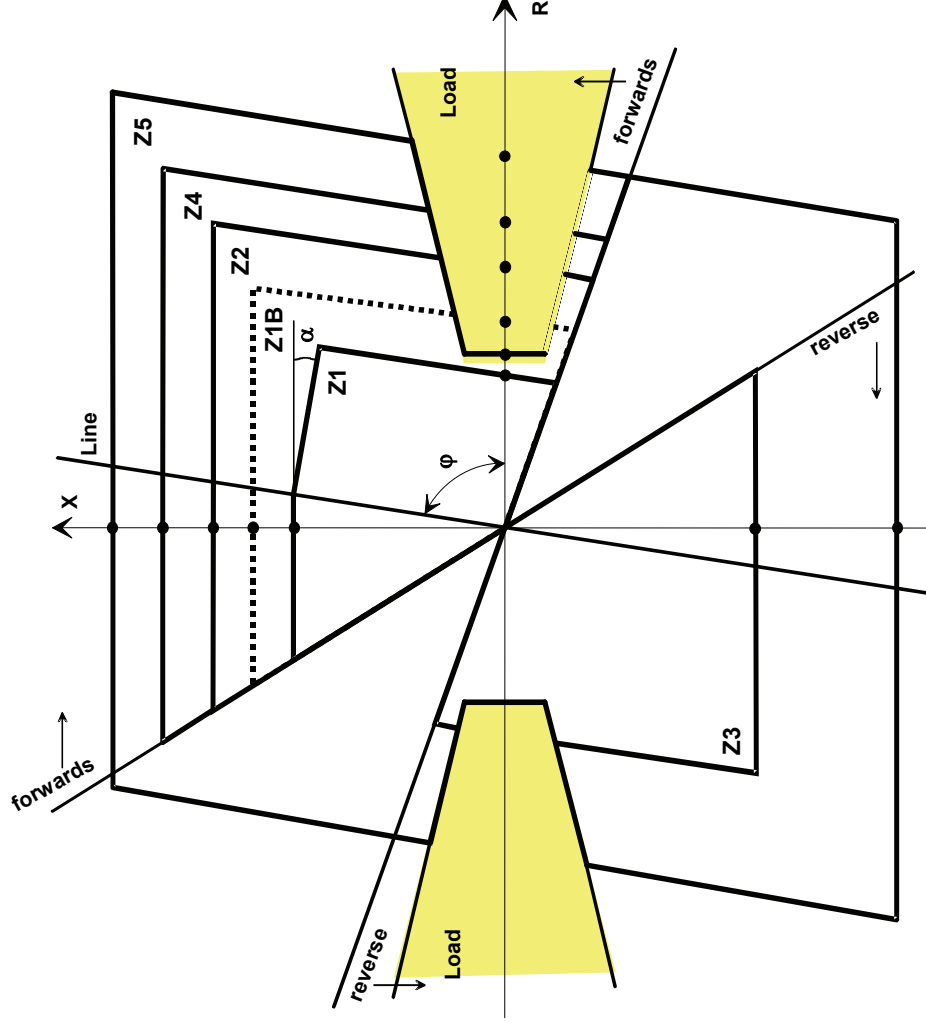
SIEMENS



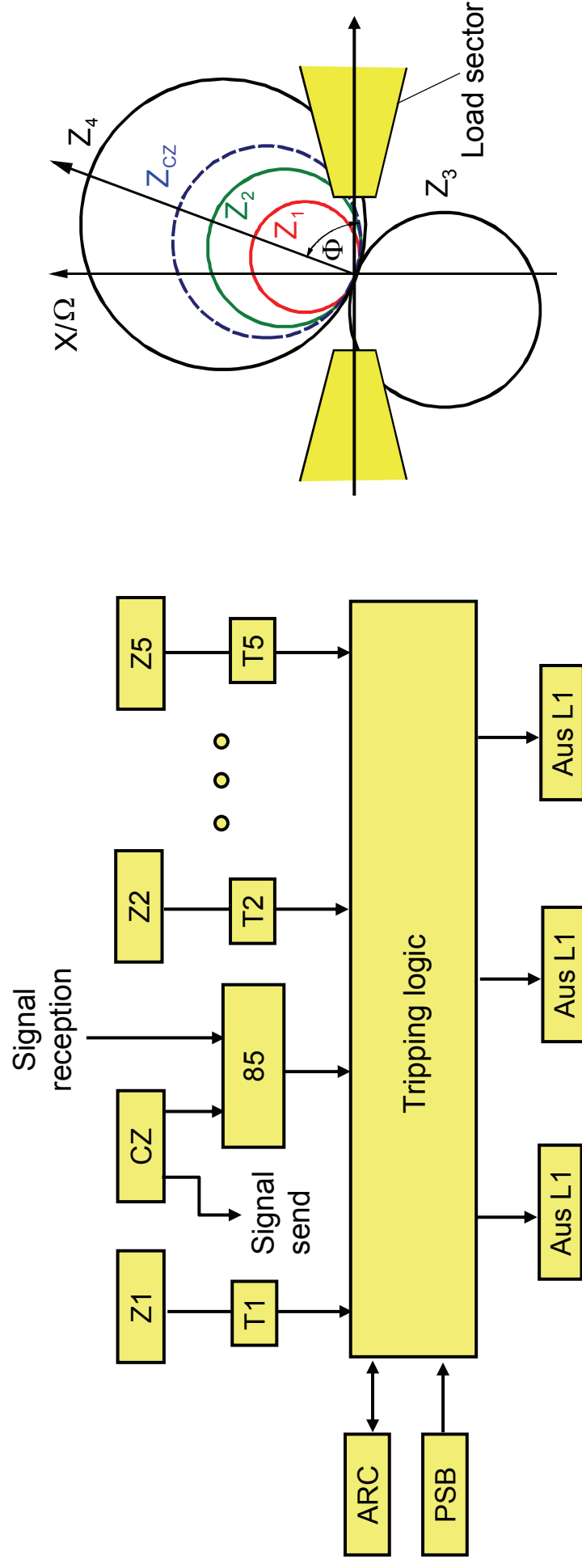
Impedance starting with conventional technology



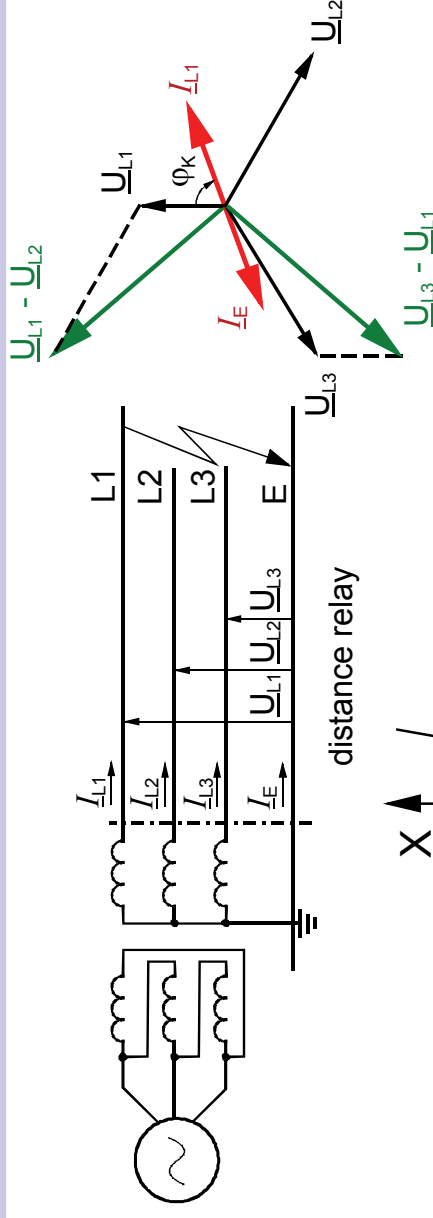
Impedance zones of modern digital relays (7SA6 und 7SA52)



Distance protection with zone dedicated time control “Zone Packaged” design (7SA6 und 7SA522)



Conventional relays: limiting of the starting characteristic area for phase-selective fault detection



impedance of
faulted loop:

$$Z_{L1-E} = \frac{U_{L1}}{I_{L1} - K_E \cdot I_E}$$

impedance of
healthy loops:

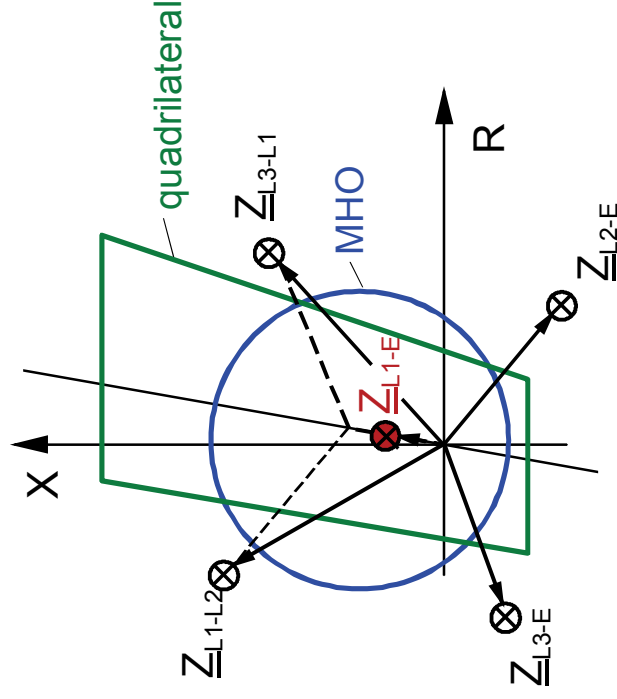
$$Z_{L2-E} = \frac{U_{L2}}{I_{L2} - K_E \cdot I_E}$$

$$Z_{L3-E} = \frac{U_{L3}}{I_{L3} - K_E \cdot I_E}$$

$$Z_{L1-L2} = \frac{U_{L1} - U_{L2}}{I_{L1} - I_{L2}}$$

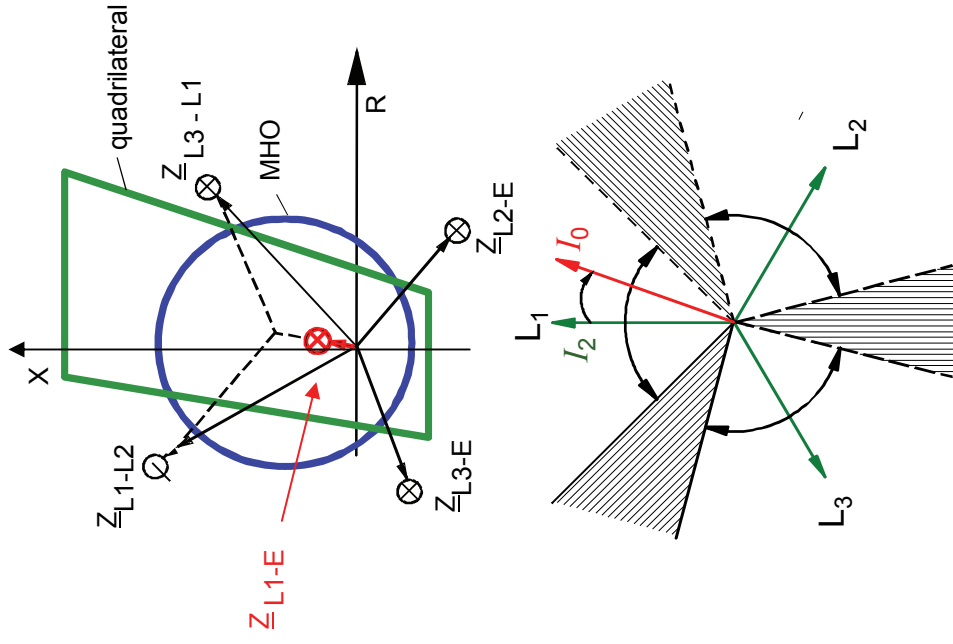
$$Z_{L2-L3} = \frac{U_{L2} - U_{L3}}{I_{L2} - I_{L3}}$$

$$Z_{L3-L1} = \frac{U_{L3} - U_{L1}}{I_{L3} - I_{L1}}$$



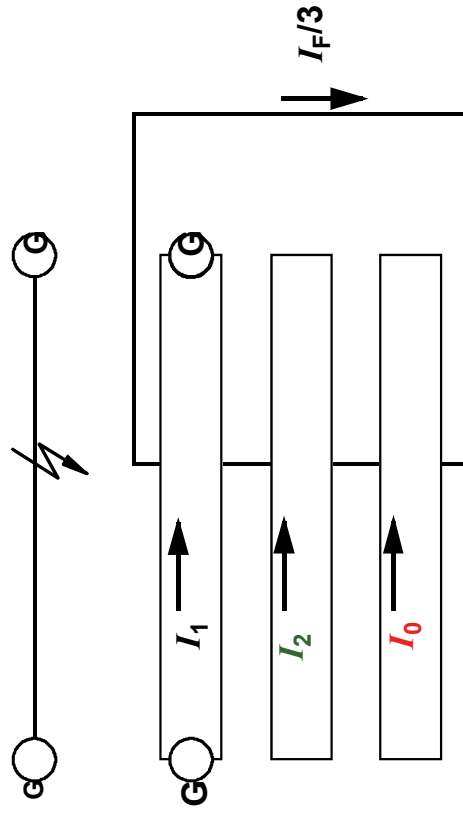
Distance protection

Modern methods of phase selection



■ Intelligent phase selection:

- ☐ Impedance comparison
- ☐ Symmetrical component analysis
- ☐ Load compensation
- ☐ Pattern recognition



Phase selection

Differentiating between single and double Ph-E fault

$$I_{\underline{0}} = \frac{1}{3} (\underline{I}_{L1} + \underline{I}_{L2} + \underline{I}_{L3})$$

$$I_{\underline{2}} = \frac{1}{3} (\underline{I}_{L1} + \underline{a}^2 \underline{I}_{L2} + \underline{a} \underline{I}_{L3})$$

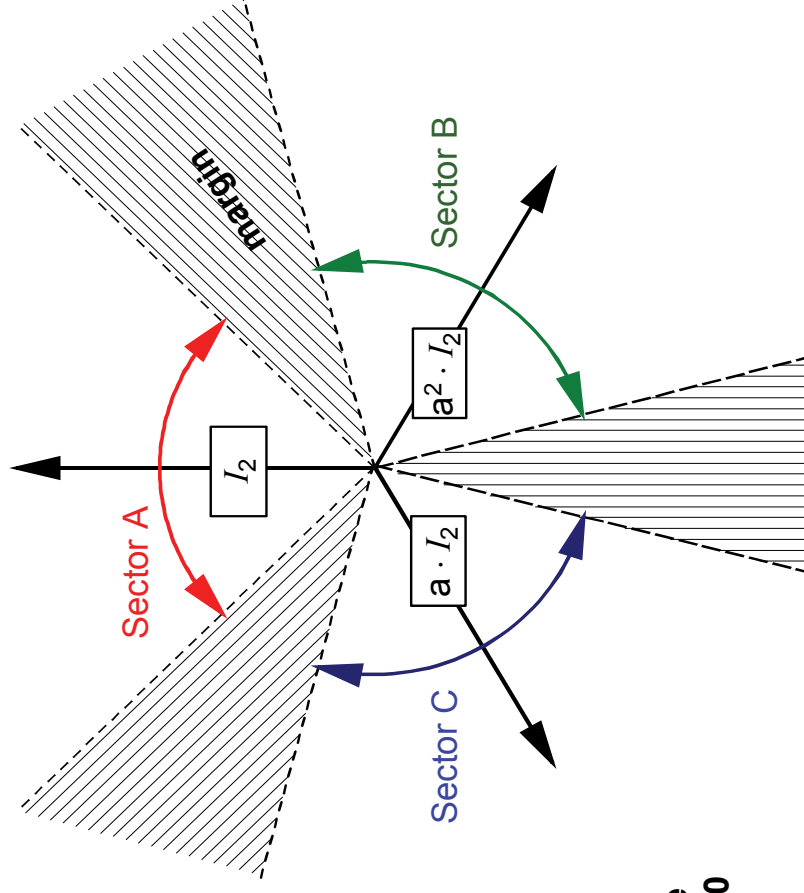
- $I_{\underline{0}} \approx \underline{I}_{\underline{2}}$: L₁-E or L₂-L₃-E fault
- $I_{\underline{0}} \approx \underline{a}^2 \underline{I}_{\underline{2}}$: L₂-E or L₃-L₁-E fault
- $I_{\underline{0}} \approx \underline{a} \underline{I}_{\underline{2}}$: L₃-E or L₁-L₂-E fault

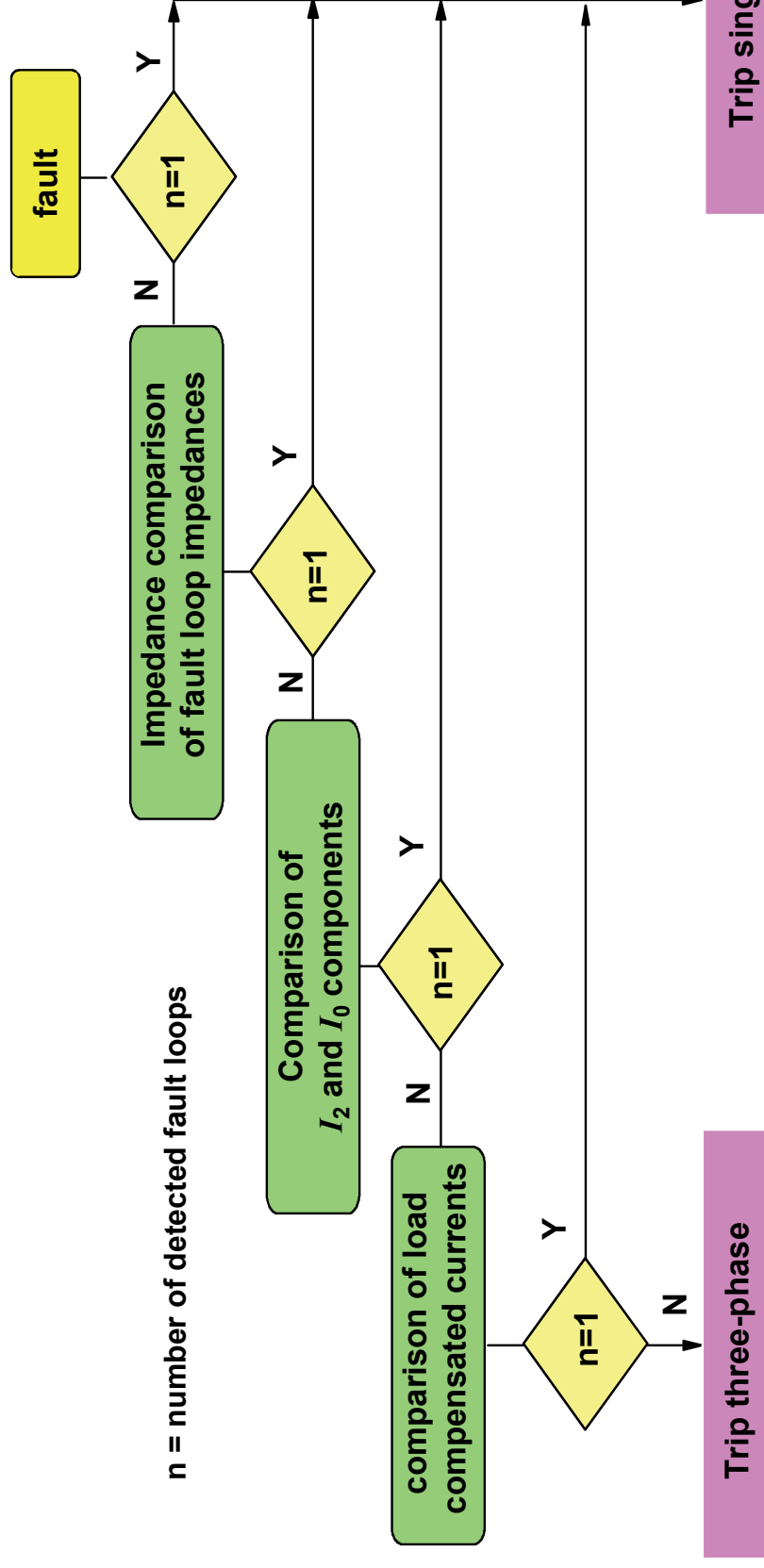
1-Ph-E fault:

After load compensation: Currents in the healthy phases are zero or have opposite phase position

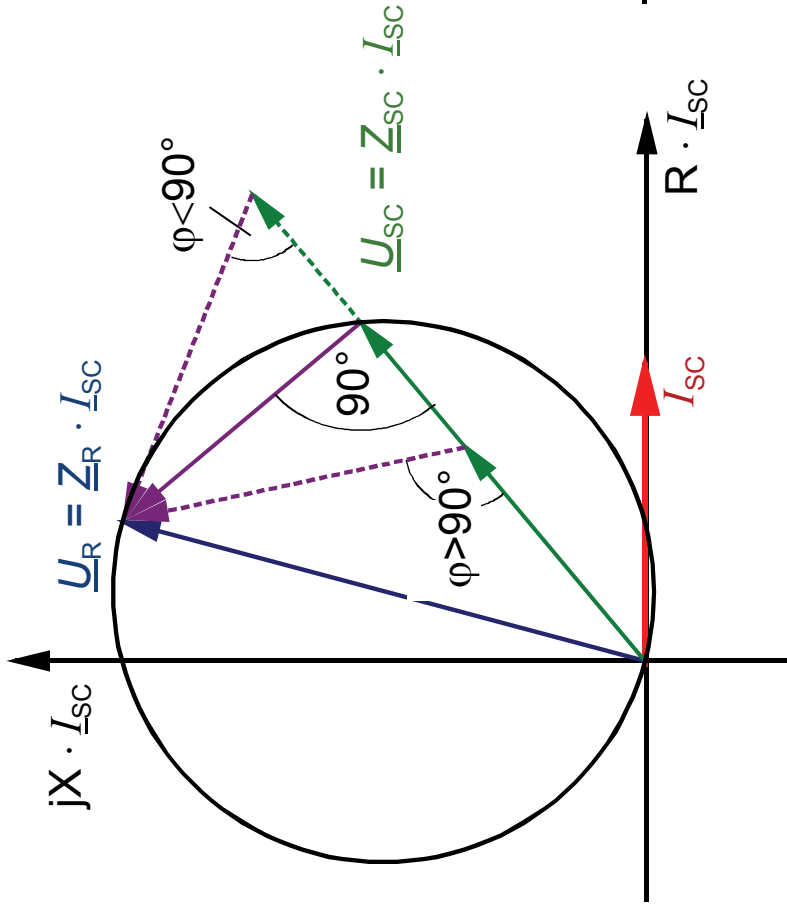
Ph-Ph-E fault:

After load compensation: Currents in faulted phases have same amplitude and show a phase difference of 120 to 180 degree dependent on earthing conditions

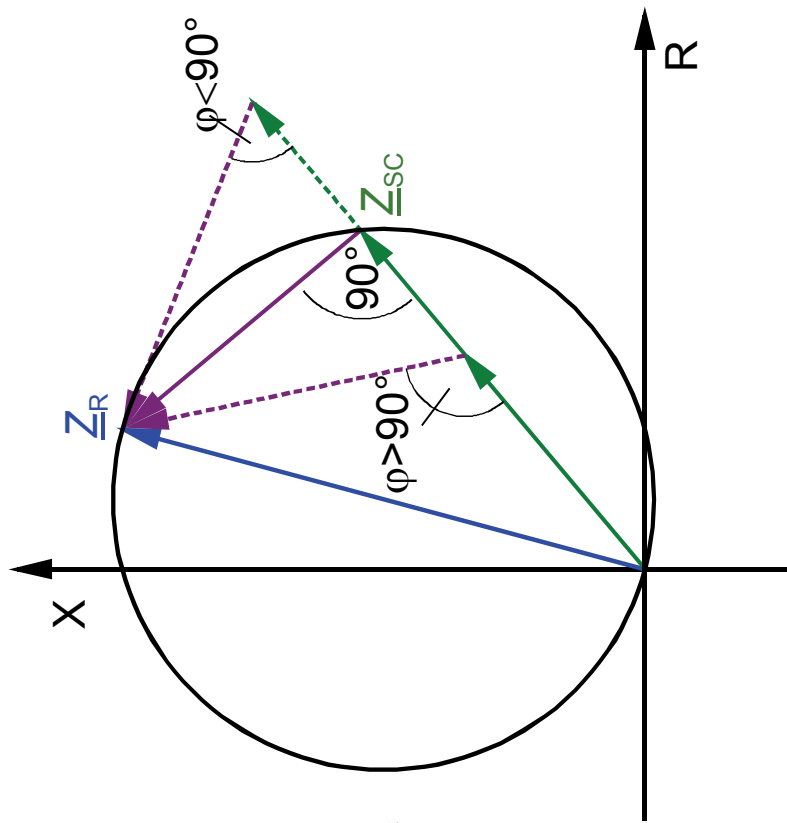




MHO-Characteristic

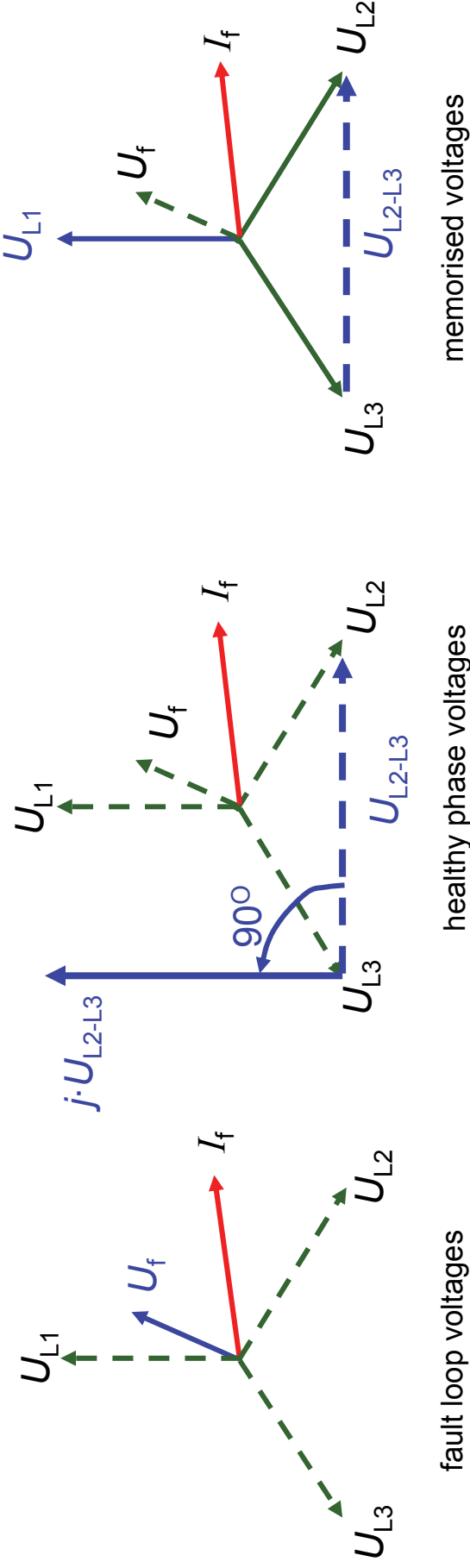
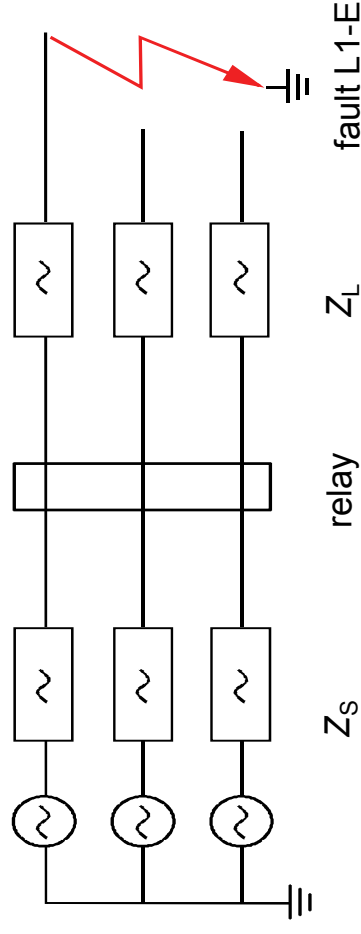


voltage diagram

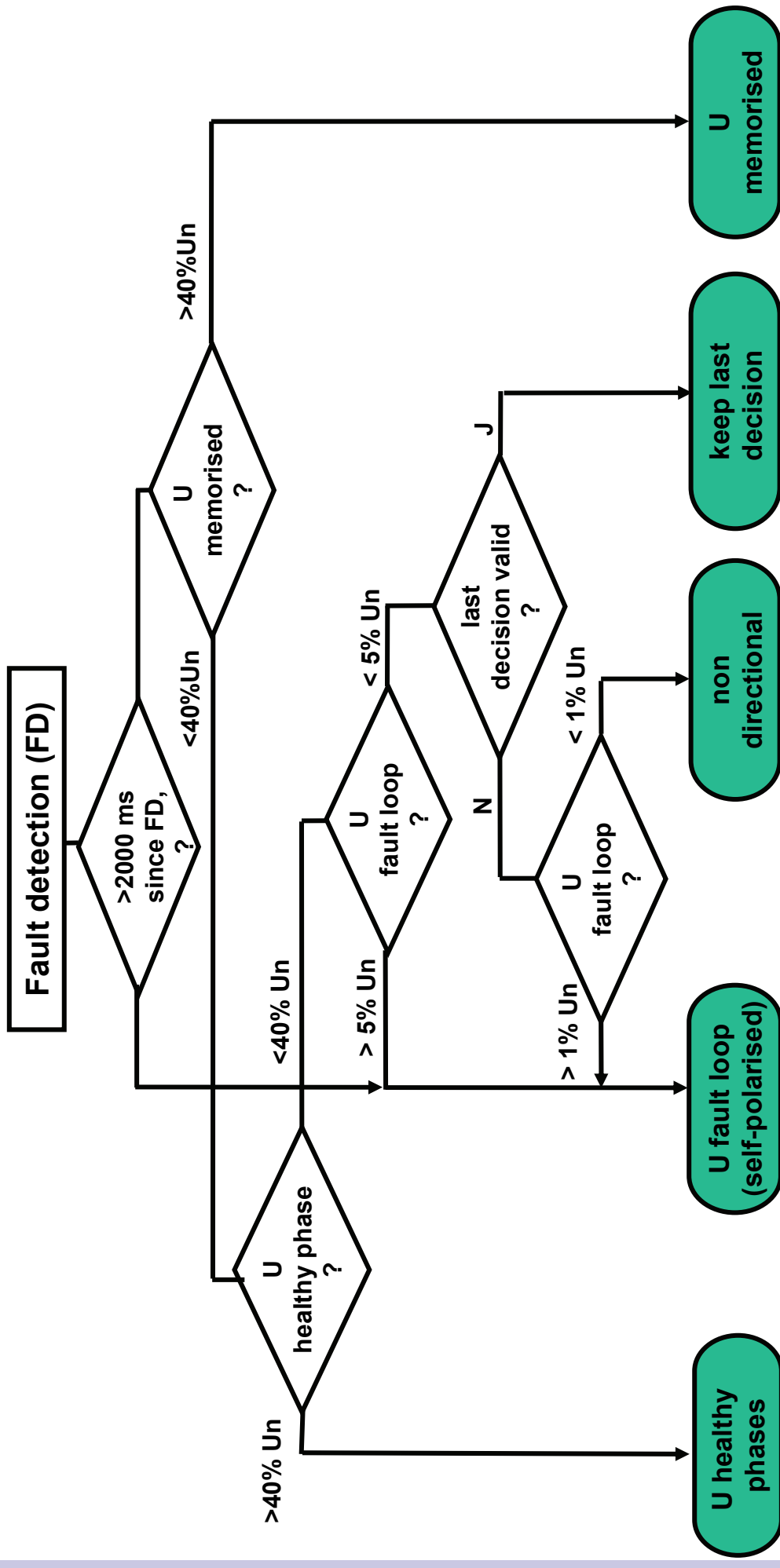


impedance diagram

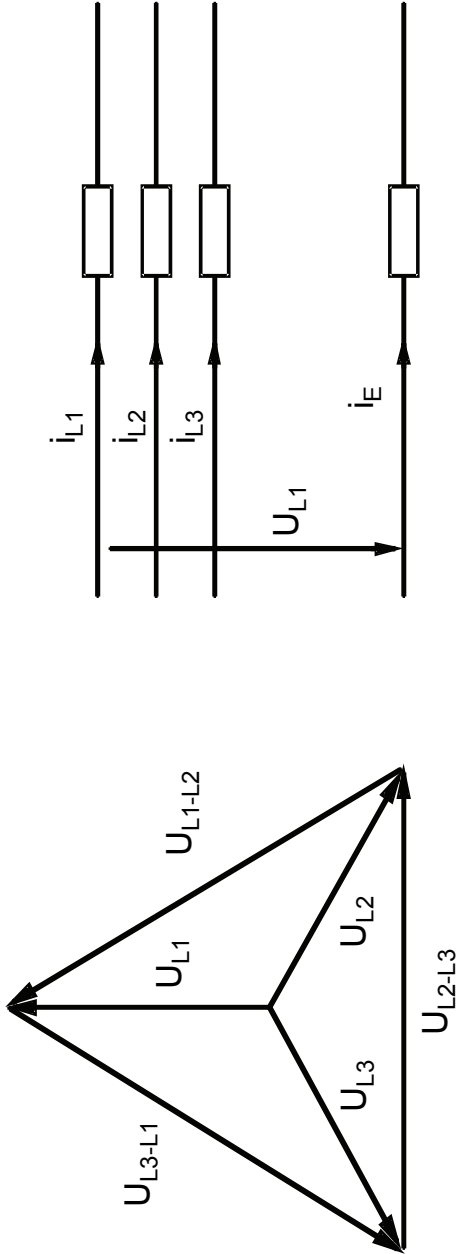
Directional determination, alternatives of voltage polarization



Directional determination: adaptive voltage polarisation



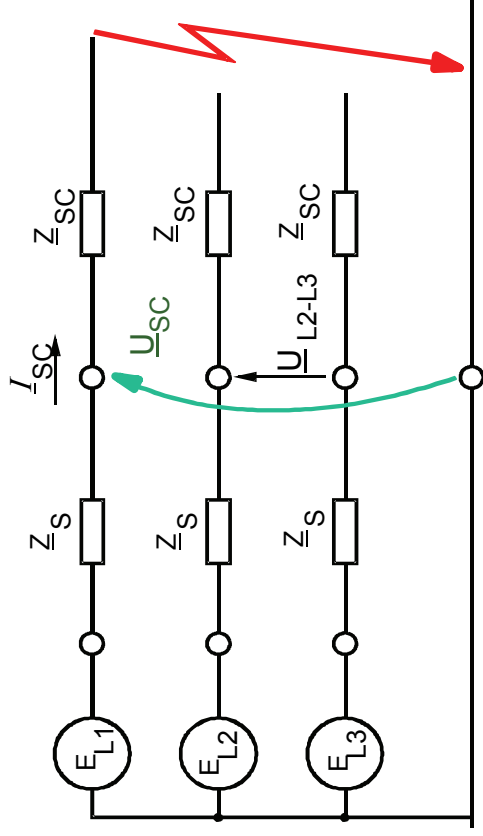
Determination of fault direction using healthy phase voltages



Measured values for directional decision

Fault loop	currents	voltages
$L1 - E$ $L2 - E$ $L3 - E$ $L1 - L2$ $L2 - L3$ $L3 - L1$	$i_{L1} - k_E \cdot i_E$ $i_{L2} - k_E \cdot i_E$ $i_{L3} - k_E \cdot i_E$ $i_{L1} - i_{L2}$ $i_{L2} - i_{L3}$ $i_{L3} - i_{L1}$	U_{L2-L3} U_{L3-L1} U_{L1-L2} $U_{L2-L3} - U_{L3-L1}$ $U_{L3-L1} - U_{L1-L2}$ $U_{L1-L2} - U_{L2-L3}$

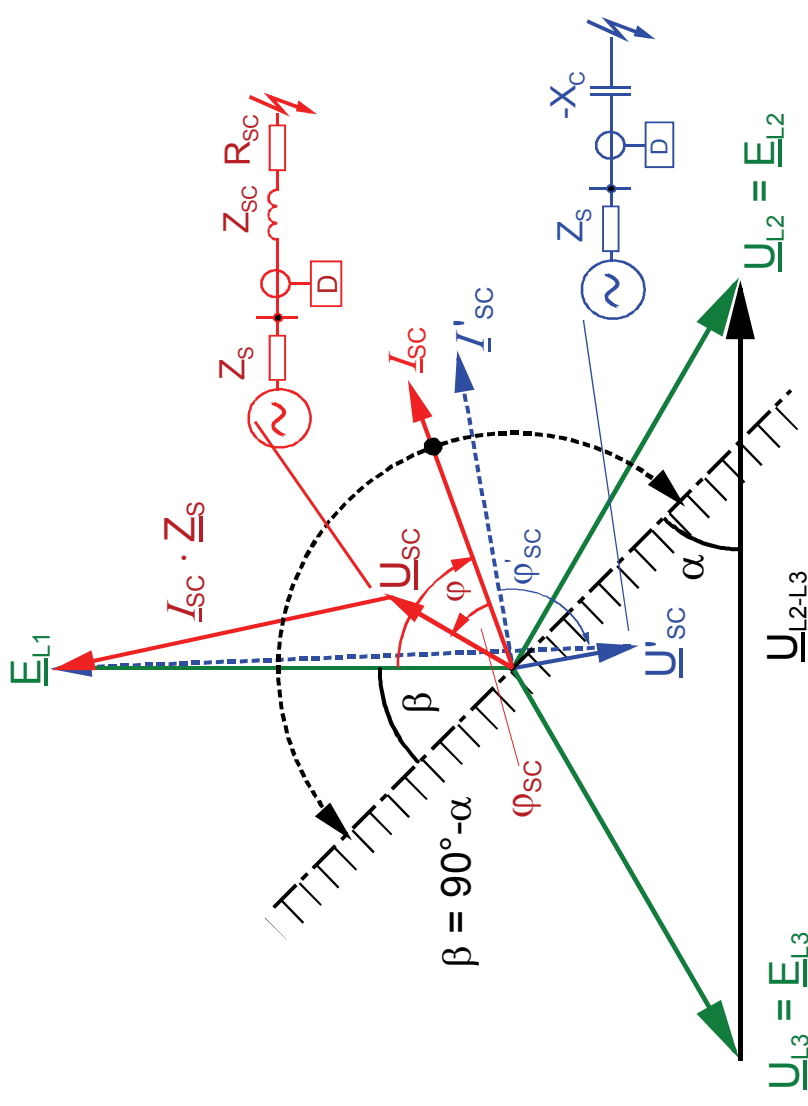
Directional determination using healthy phase voltages: Cross-polarisation



$$\underline{E}_{L1} = \underline{U}_{SC} + \underline{Z}_S \cdot \underline{I}_{SC}$$

$$\underline{U}_{L2-L3} = \underline{E}_{L2-L3} = \underline{E}_{L1} \cdot \sqrt{3} \cdot e^{-j90^\circ}$$

Equivalent circuit

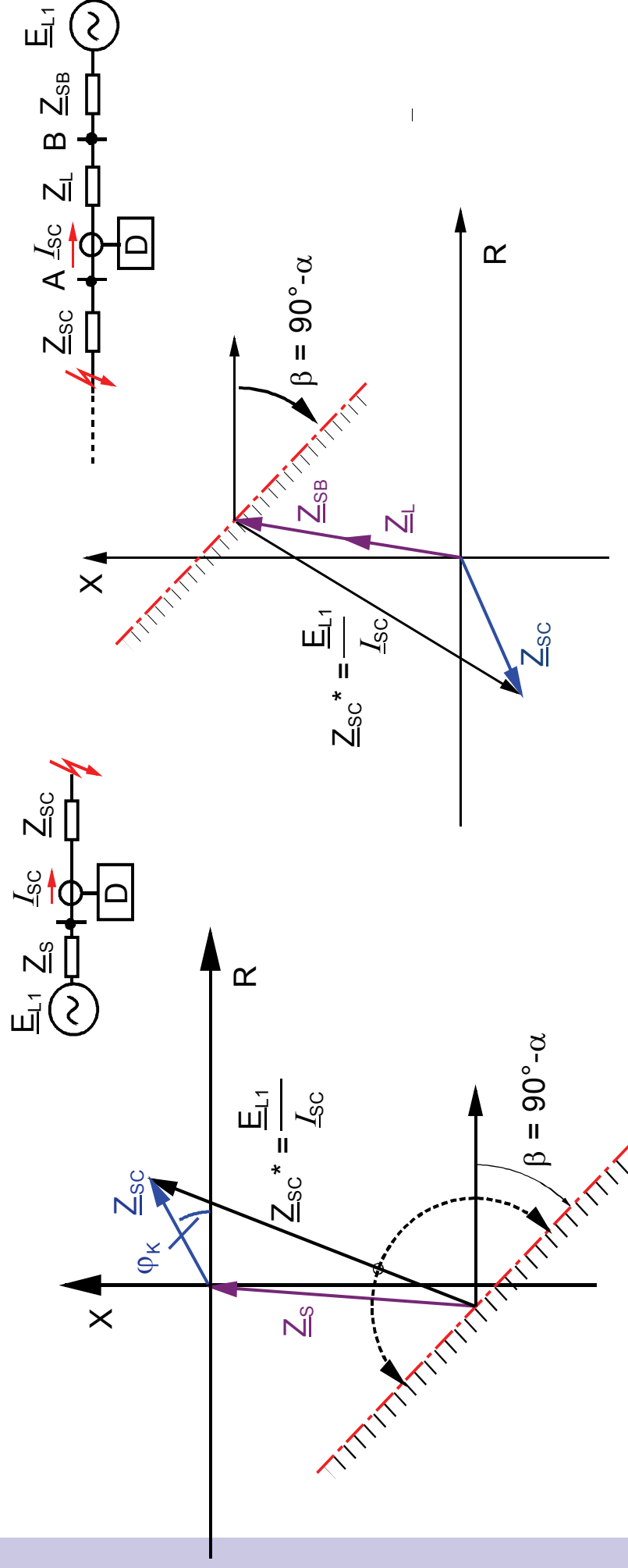


Voltage diagram

Cross-polarisation

Shift of directional characteristic with forward and reverse faults

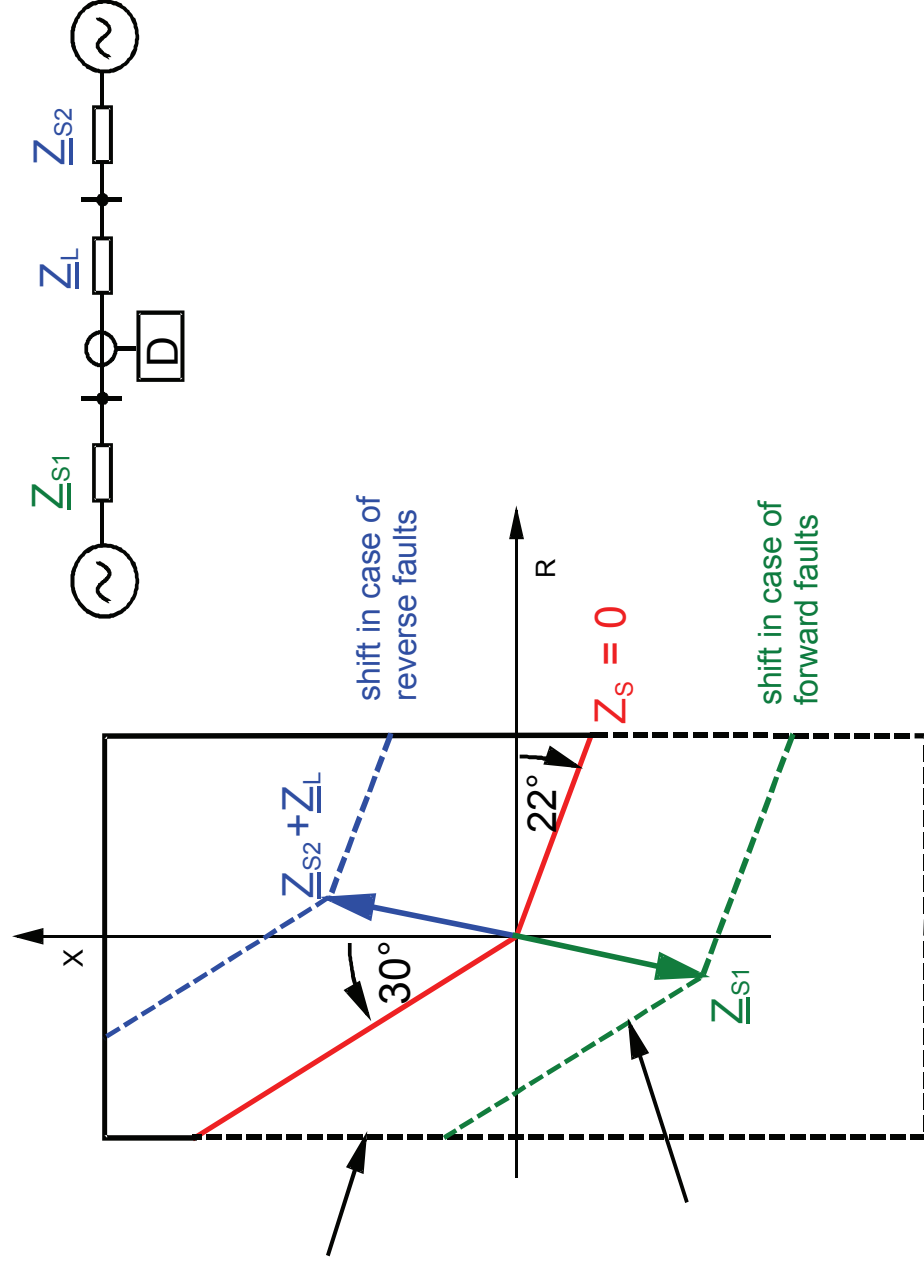
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Directional characteristic in the impedance plane
for faults in the forward direction

Directional characteristic in the impedance plane
for faults in the reverse direction

Quadrilateral impedance characteristic and directional determination with healthy phase voltage



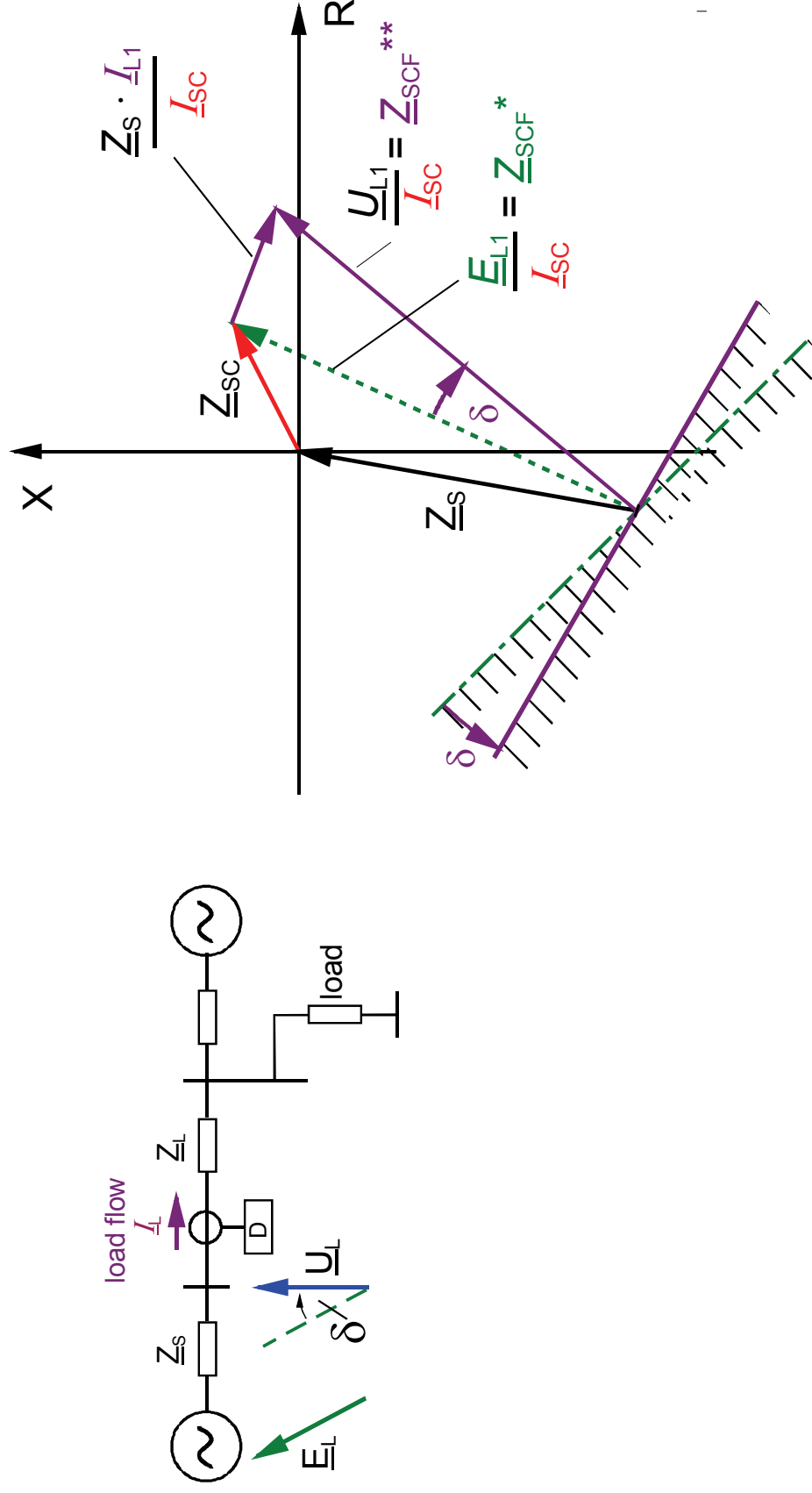
Impedance measurement:
with fault loop voltages
(fixed characteristic)

Directional determination:
with healthy phase voltages
(characteristic shifted proportional
to source impedance)

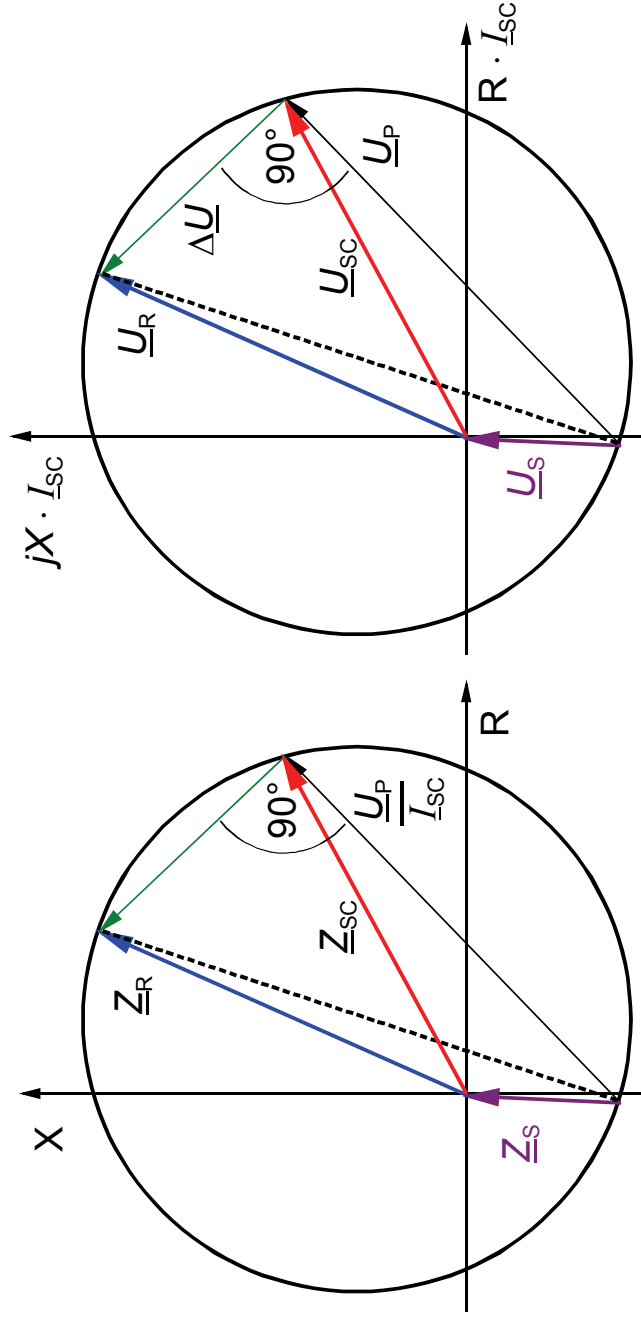
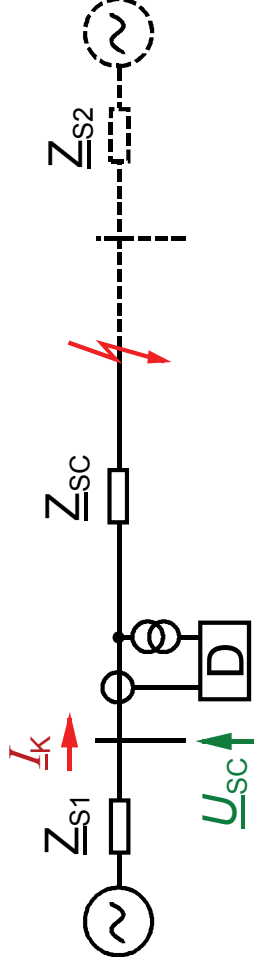
Cross polarisation:

The influence of load transfer on the position of the directional characteristic

SIEMENS



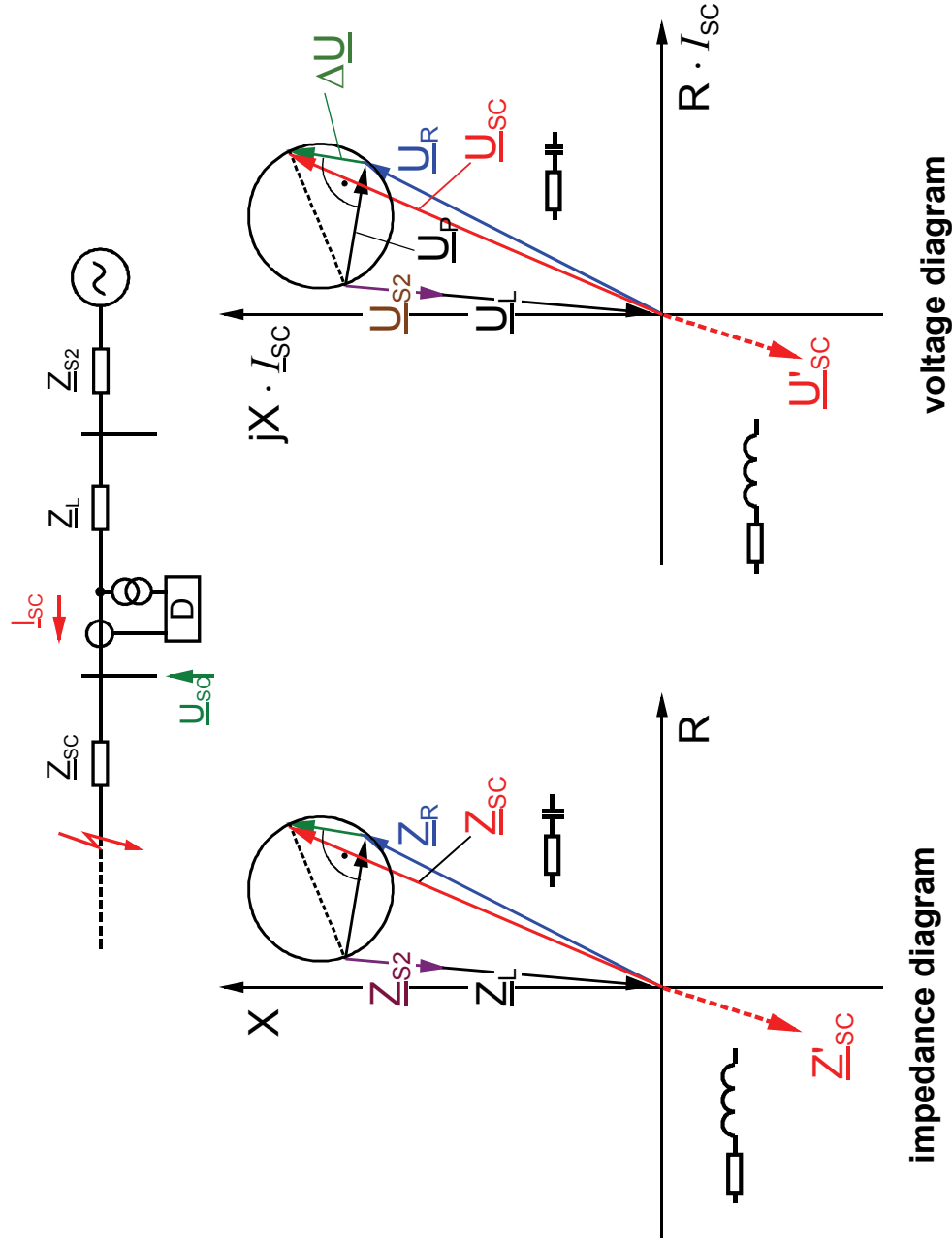
Polarised MHO-circle, fault in the forward direction



impedance diagram

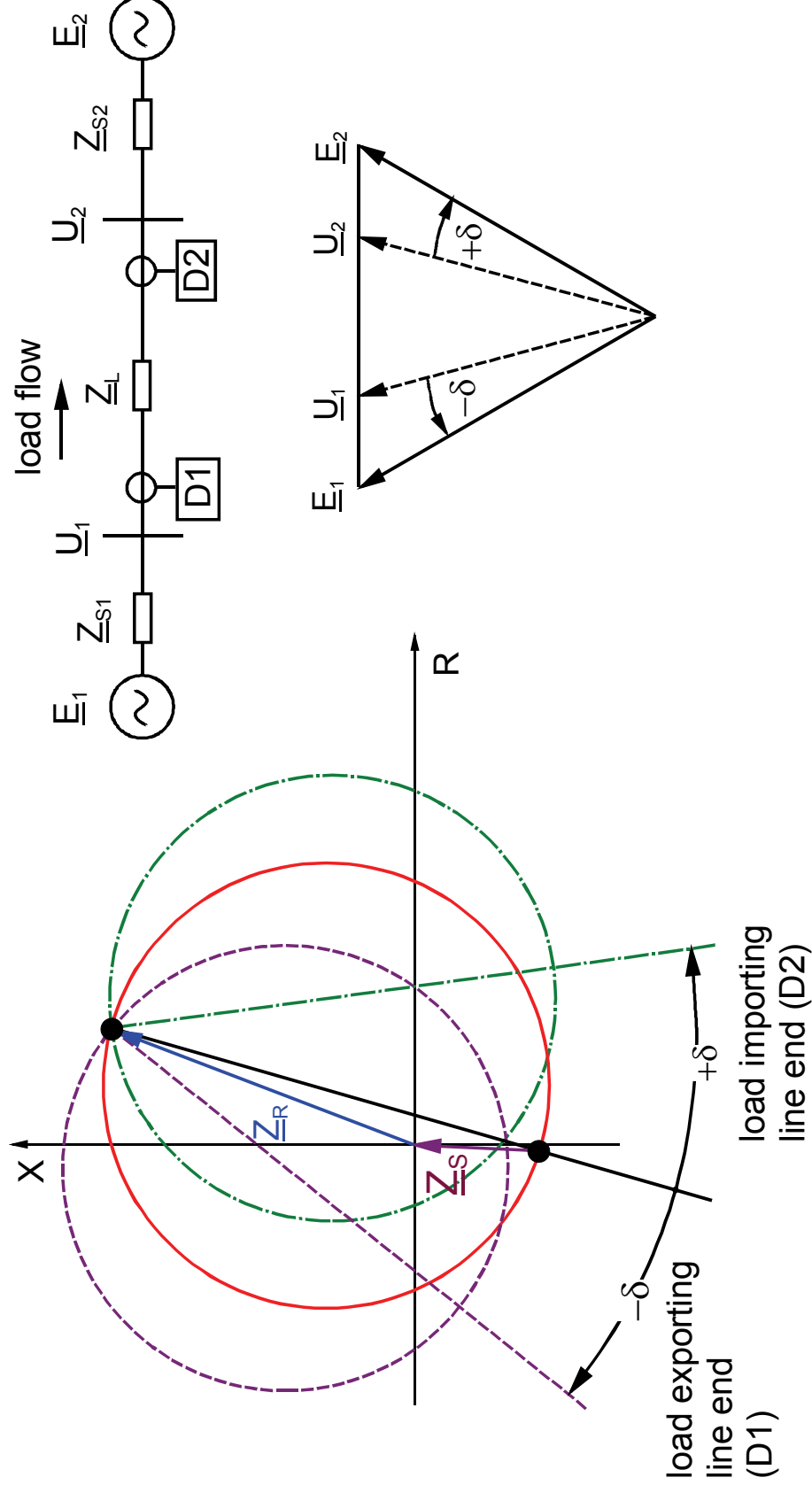
Voltage diagram

Polarised MHO-circle, fault in reverse direction

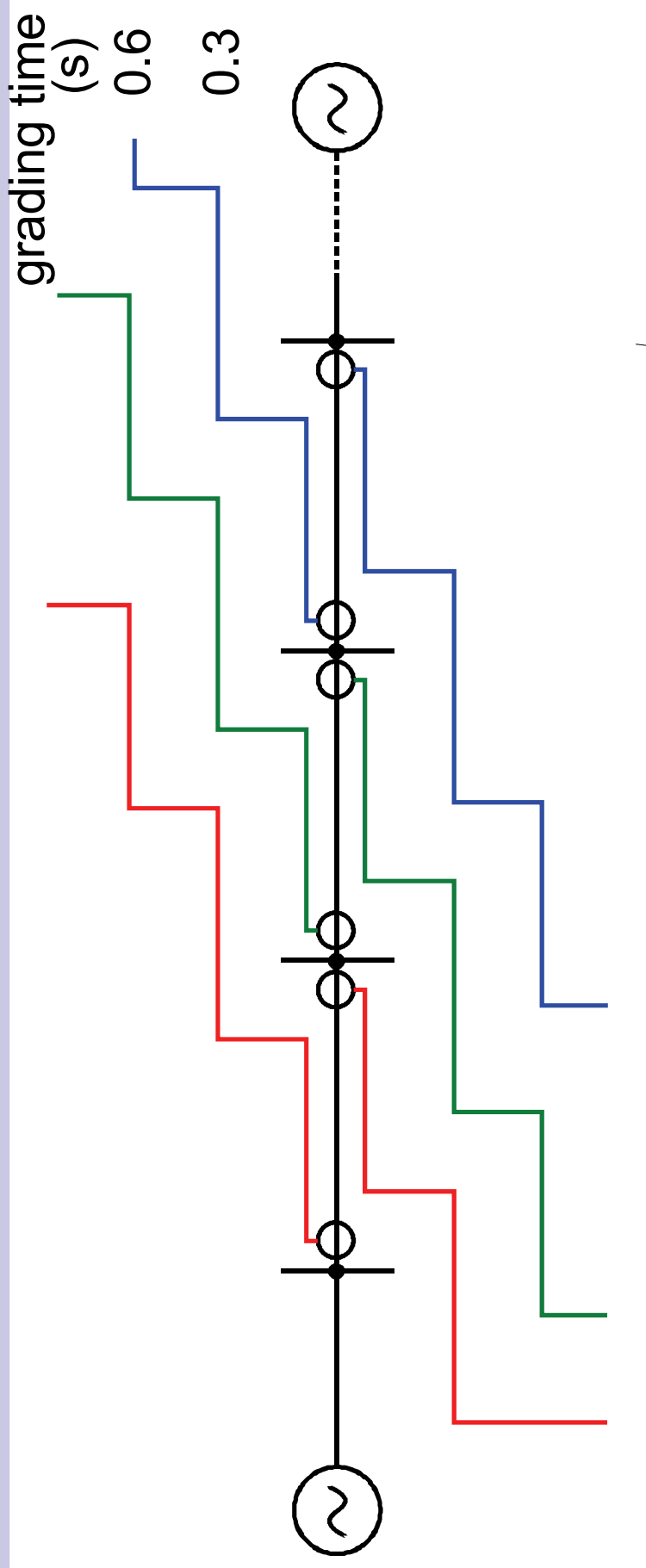


Influence of load transfer on the position of the polarised MHO-circle (100% healthy phase voltage polarisation)

SIEMENS



Ring feeder: with grading against opposite end



Determination of grading times

2nd Zone:

It must initially allow the 1st zone on the neighbouring feeder(s) to clear the fault.
The grading time therefore results from the addition of the following times:

- **operating time of the adjacent feeder**

mechanical:	25 – 80 ms
static	15 – 40 ms
digital	15 – 30 ms

- + **circuit breaker operating time**

MV:	HV / EHV: 60 ms (3 cycles) / 40 ms (2 cycles)
	up to about 80 ms (4 cycles)

- + **distance relay reset time**

static:	mechanical: ca. 60-100 ms	(Over-
travel time)	ca. 30 ms	
	digital:	ca. 20 ms.

- + **errors of the relay internal timers**

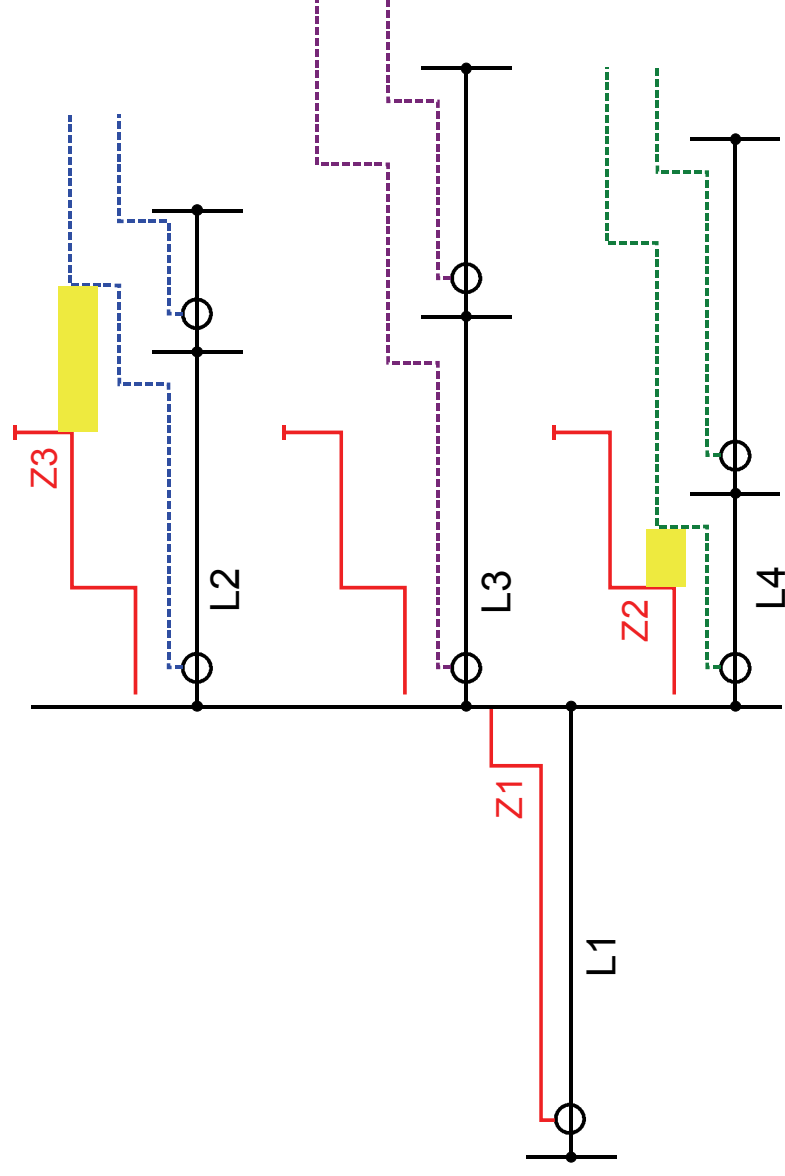
mechanical:	5% of the set time, minimum 60-100 ms
static:	3% of the set time, minimum 10 ms
digital:	1% of the set time, minimum 10 ms

- + **safety margin (ca.)**

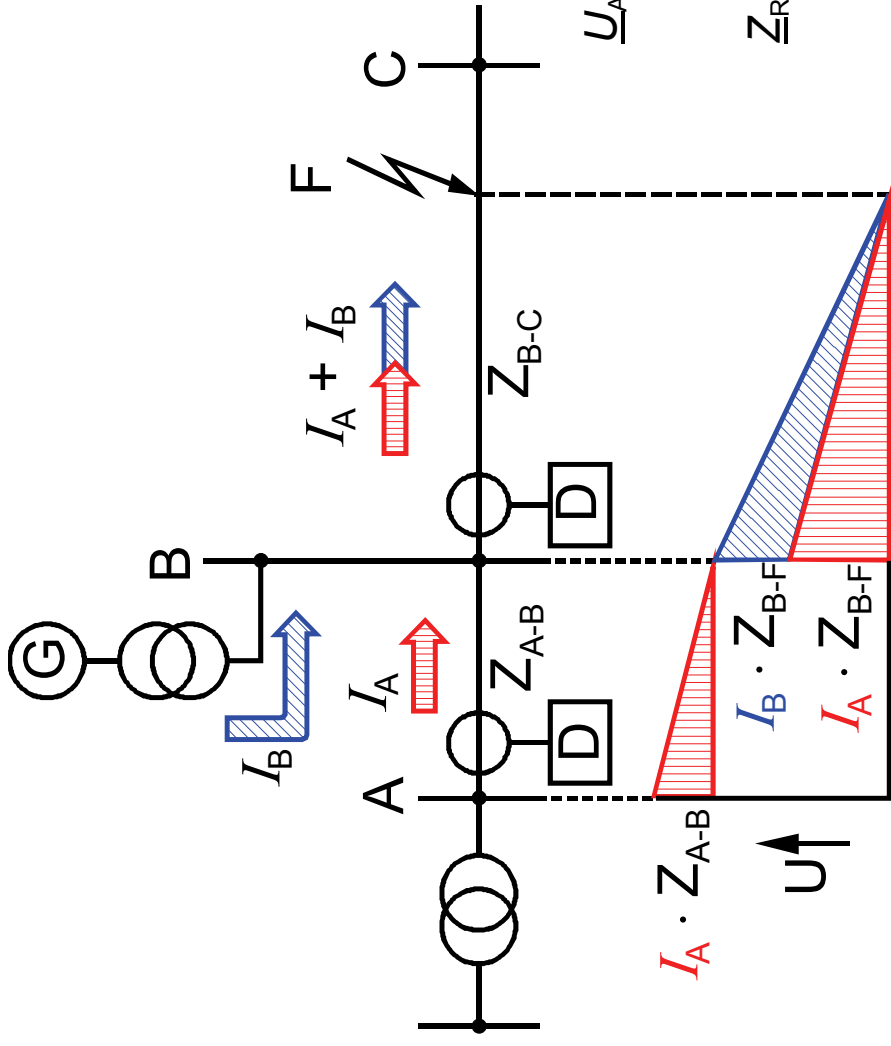
grading:	mechanical-mechanical:	100 m
	static/digital-mechanical or vice versa:	75 m
	digital-digital or static-static	50 ms

Grading in a branched radial system

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Effect of intermediate infeeds on distance measurement (1)



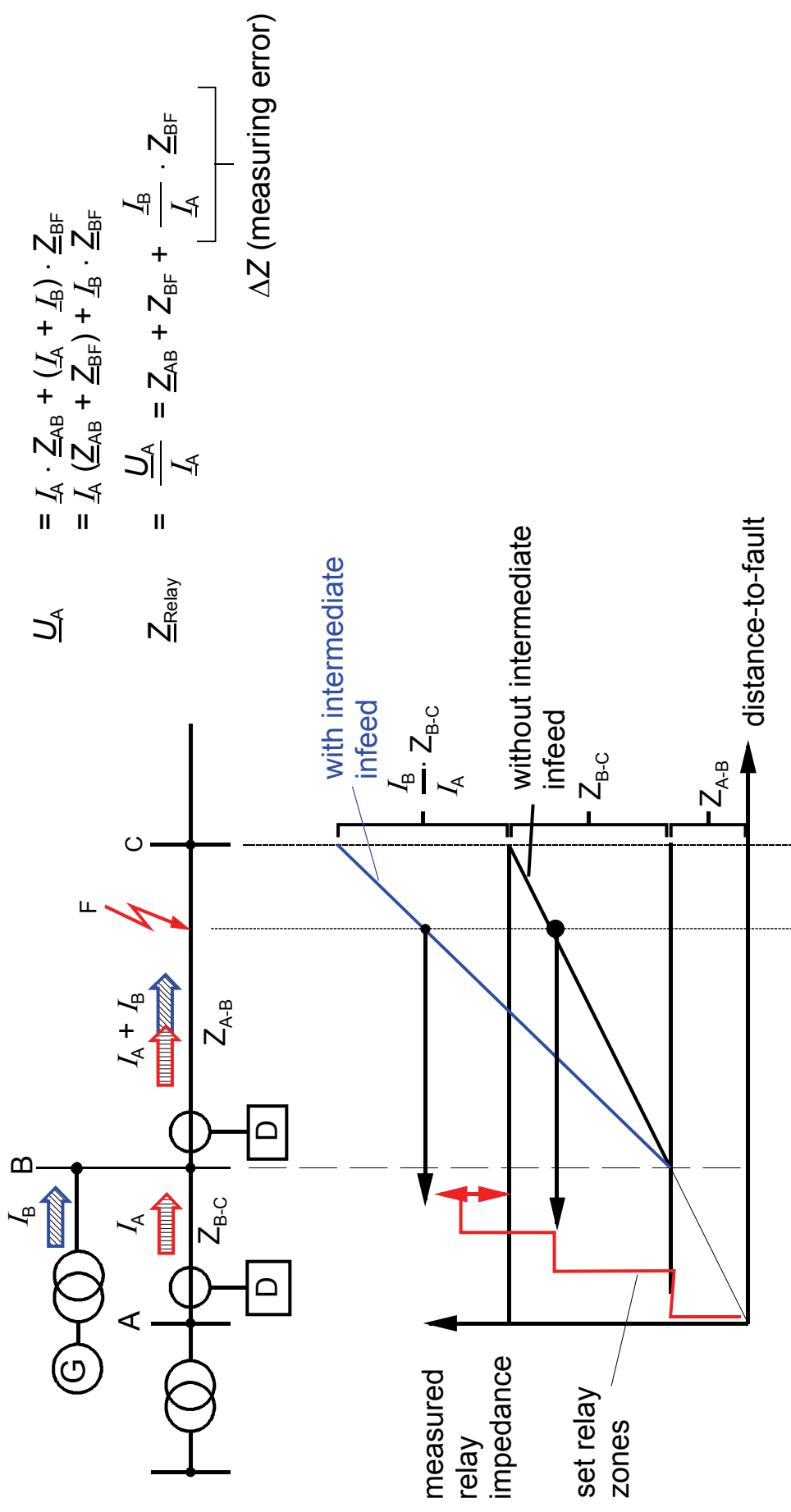
$$= \underline{I}_A \cdot \underline{Z}_{AB} + (\underline{I}_A + \underline{I}_B) \cdot \underline{Z}_{BF}$$

$$= \underline{I}_A (\underline{Z}_{AB} + \underline{Z}_{BF}) + \underline{I}_B \cdot \underline{Z}_{BF}$$

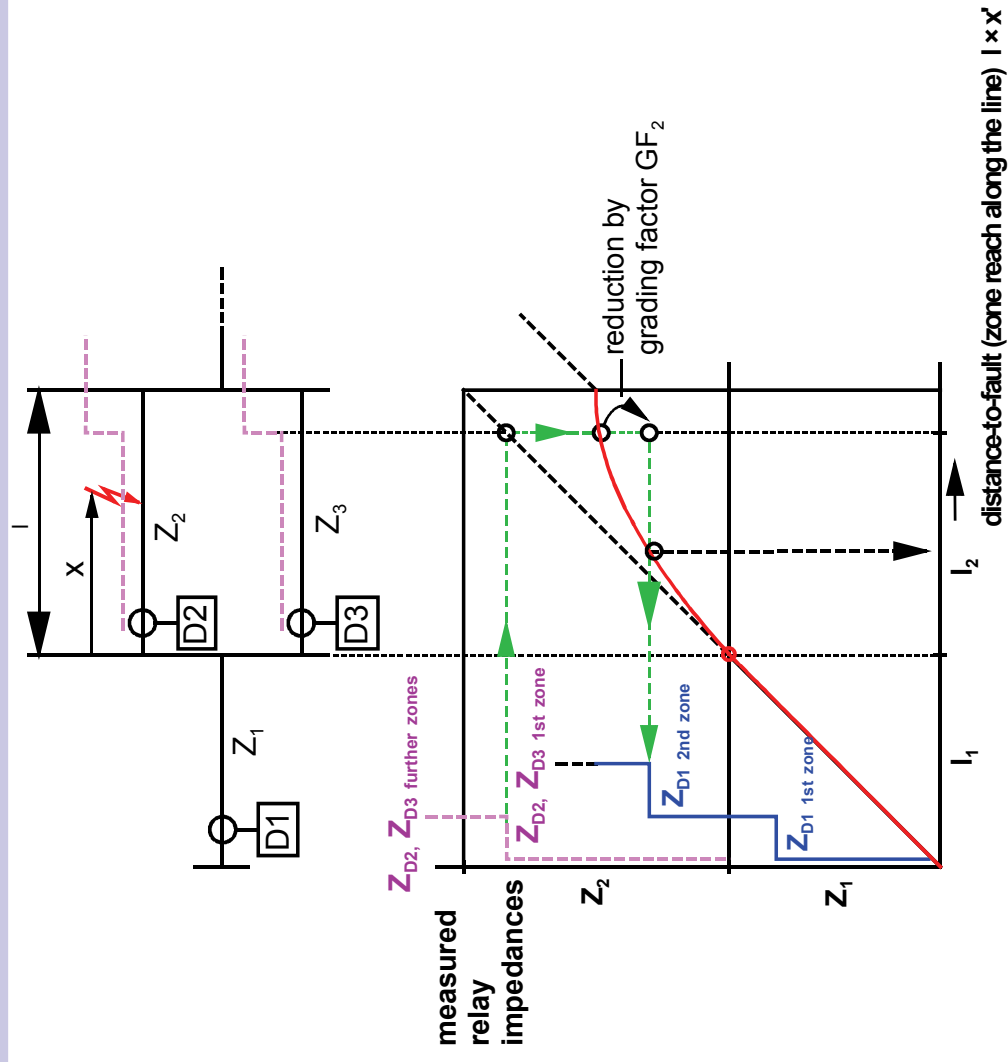
$$= \frac{\underline{U}_A}{\underline{I}_A} = \underline{Z}_{AB} + \underline{Z}_{BF} + \underbrace{\frac{\underline{I}_B}{\underline{I}_A} \cdot \underline{Z}_{BF}}_{\Delta Z \text{ (measuring error)}}$$

ΔZ (measuring error)

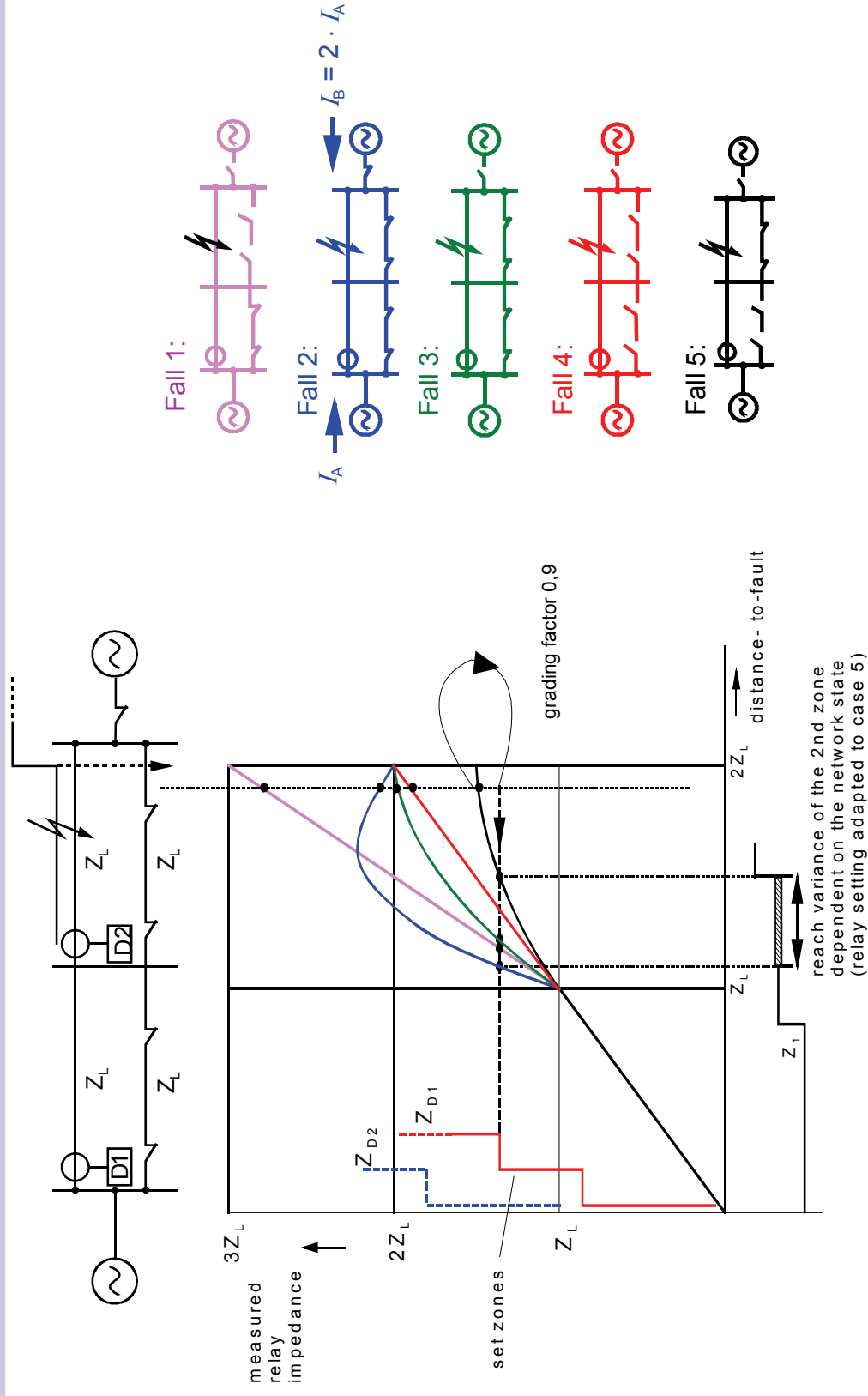
Effect of intermediate infeeds on distance measurement (2)



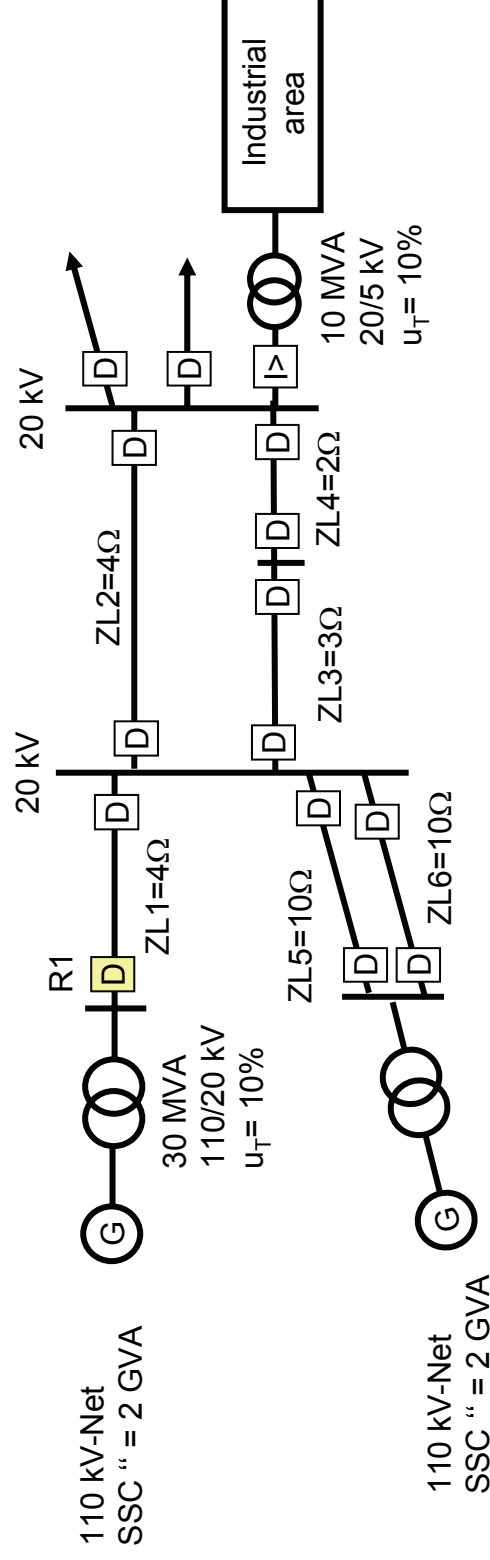
Grading for parallel feeders



Zone grading for parallel lines, influence of switching conditions



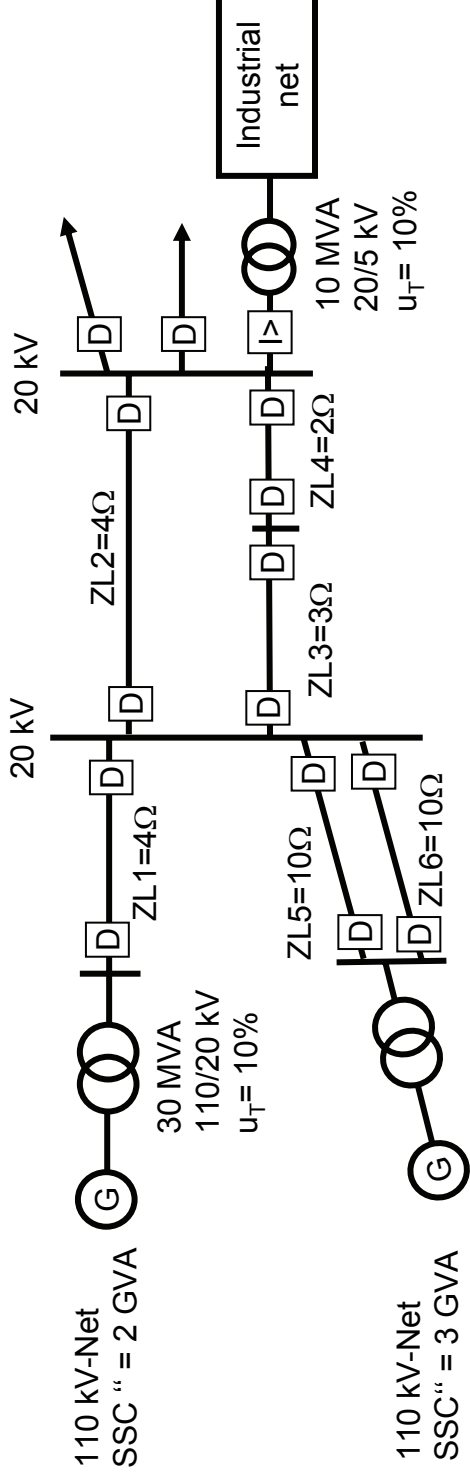
Zone grading: Example (1)



Task: Grading zones of relay 1

Zone grading: Example (2)

Calculation of equivalent impedances



$$Z_{S-N1} = \frac{20 \text{ kV}^2}{2000 \text{ MVA}} = 0.2 \Omega$$

$$Z_{T1} = \frac{10\%}{100} \cdot \frac{20^2}{30} = 1.33 \Omega$$

$$Z_{S1} = Z_{S-N1} + Z_{T1} = 0.2 + 1.33 = 1.53 \Omega$$

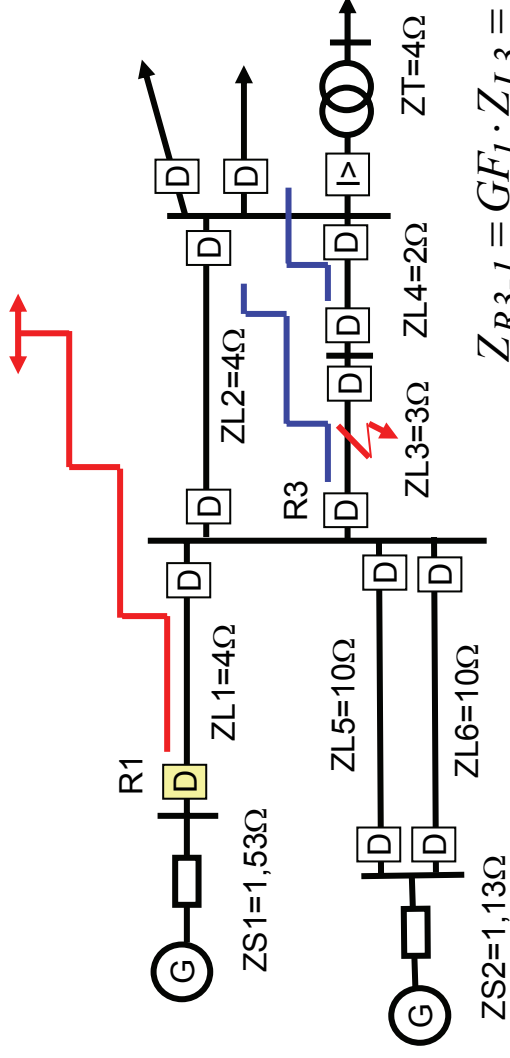
$$Z_{S-N2} = \frac{20 \text{ kV}^2}{3000 \text{ MVA}} = 0.13 \Omega$$

$$Z_{T2} = \frac{10\%}{100} \cdot \frac{20^2}{40} = 1.0 \Omega$$

$$Z_{S2} = Z_{S-N2} + Z_2 = 0.13 + 1.0 = 1.13 \Omega$$

Zone grading: Example (3)

Adopted grading philosophy



$$Z_{R3-1} = GF_1 \cdot Z_{L3} = 0.9 \cdot 3.0 = 2.7 \Omega$$

$$Z_{R3-2} = GF_2 \cdot (Z_{L3} + 0.9 \cdot Z_{L4}) = 0.9 \cdot (3 + 0.9 \cdot 2) = 4.32$$

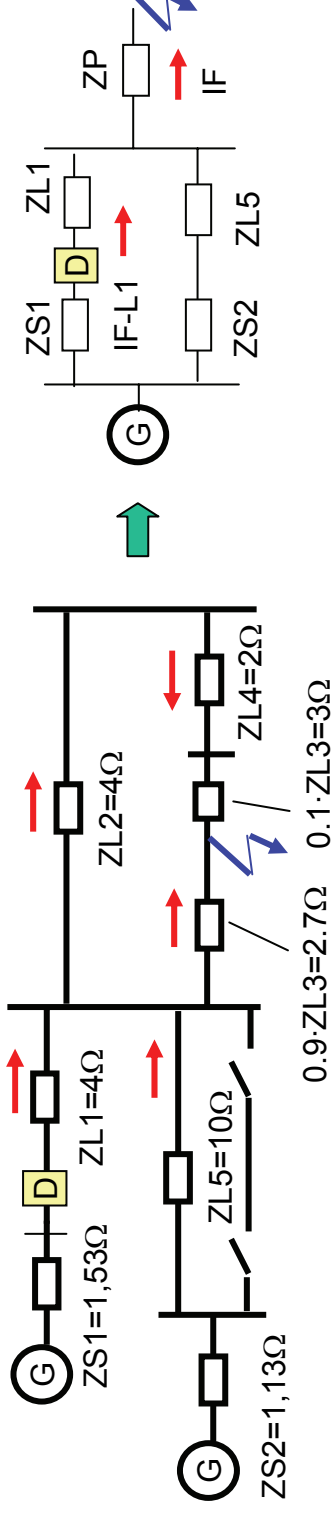
$$\text{Zone 1: } Z_{R1-1} = GF_1 \cdot Z_{L1} = 0.9 \cdot 4.0 = 3.6 \Omega$$

Zone 2 of relay 1 must be graded to the end of 1st Zone of relay 3 (shortest impedance). The parallel way via ZL2 + ZL4 and the intermediate infeed through ZL5 und ZL6 (only one line in service) have to be considered.

Zone 3 can be graded to the end of zone 2 of relay 3 (same procedure as with the grading of zone 2), or simply 10% beyond the longest following line.

Zone grading: Example (4)

Calculation of Zone 2



$$I_F = I_{F-L1} + I_{F-L5} = \frac{1.1 \cdot 20 / \sqrt{3}}{(Z_{S1} + Z_{S1}) // (Z_{S2} + Z_{L5}) + (Z_{L2} + Z_{L4} + 0.1 \cdot Z_{L3}) // 0.9 \cdot Z_{L3}} = 2.276 \text{ kA}$$

$$I_{F-L1} = \frac{Z_{S2} + Z_{L5}}{Z_{S1} + Z_{L1} + Z_{V2} + Z_{L5}} \cdot I_F = 1.520 \text{ kA} \quad \text{and} \quad I_{F-L5} = \frac{Z_{S1} + Z_{L1}}{Z_{S1} + Z_{L1} + Z_{V2} + Z_{L5}} \cdot I_F = 0.756 \text{ kA}$$

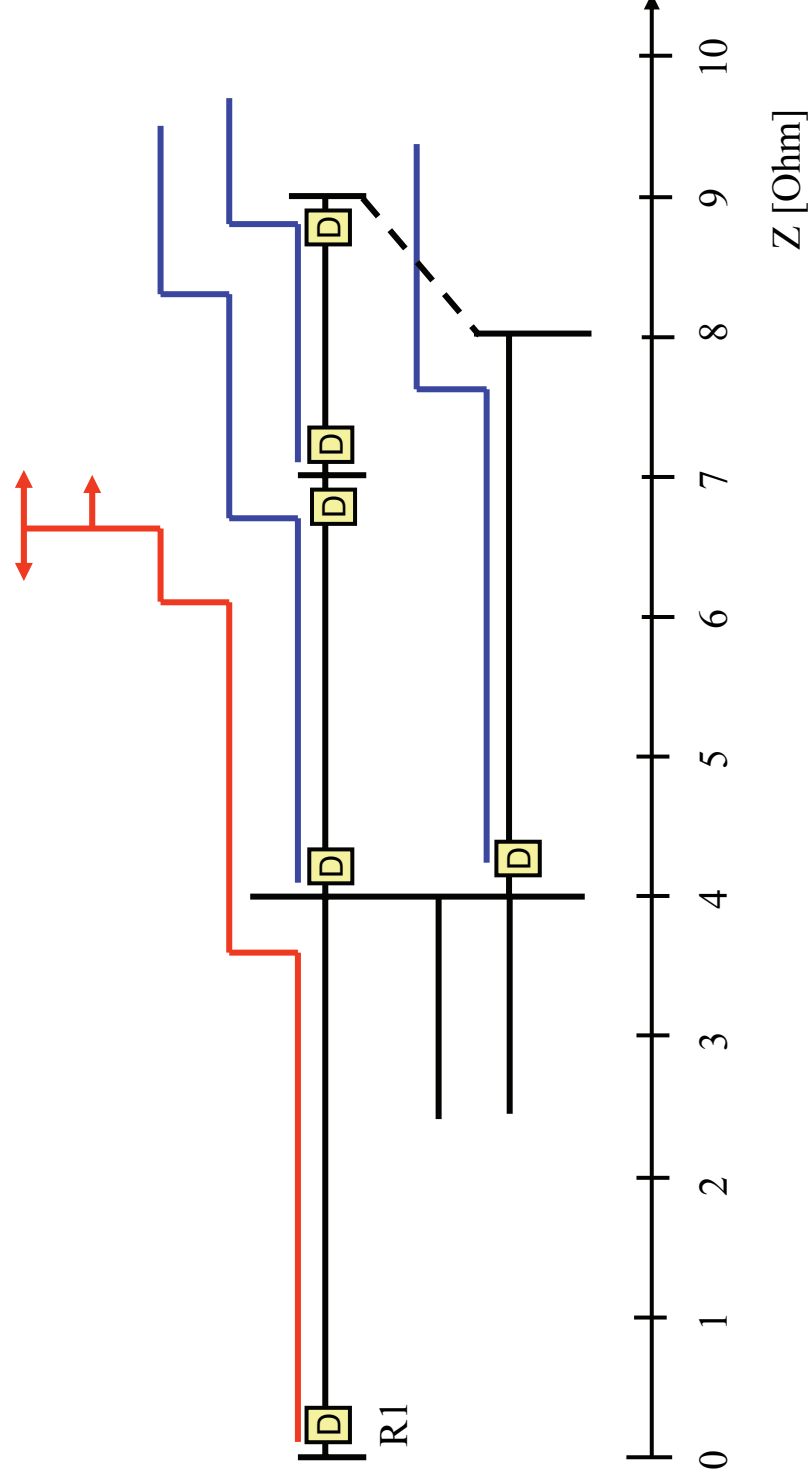
$$Z_P = (Z_{L2} + Z_{L4} + 0.1 \cdot Z_{L3}) // 0.9 \cdot Z_{L3} = 1.89 \Omega$$

$$Z_{R1-2} = G F_2 \cdot (Z_{L1} + Z_P \cdot \frac{I_F}{I_{F-L1}}) = 0.9 \cdot (4.0 + 1.89 \cdot \frac{2.276}{1.520}) = 6.14 \Omega = 1.535 \cdot Z_{L1}$$

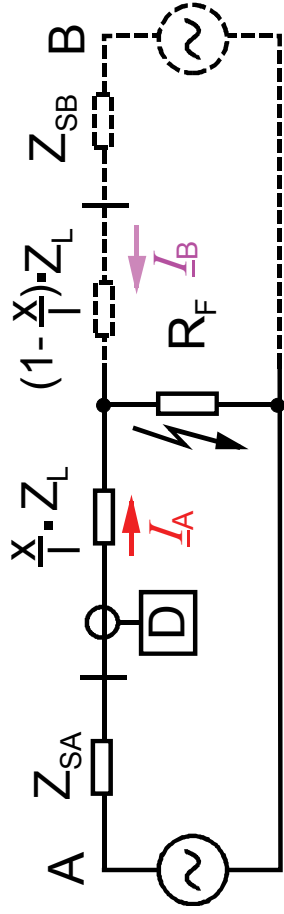
Zone grading: Example (6)

Grading plan for relay 1

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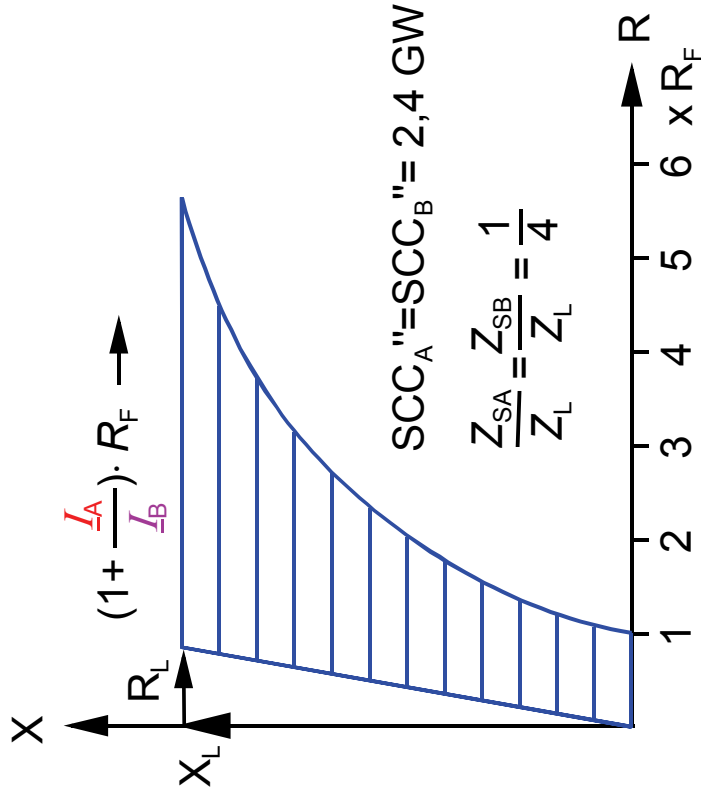


Apparent fault resistance dependent on fault location (influence of R_F on short-circuit currents neglected)



$$\frac{I_A}{I_B} = \frac{\frac{Z_{SA}}{Z_L} + \frac{x}{l}}{\frac{Z_{SB}}{Z_L} + 1 - \frac{x}{l}}$$

$$Z_D = x \cdot Z_L + \left(1 + \frac{I_B}{I_A}\right) \cdot R_F$$

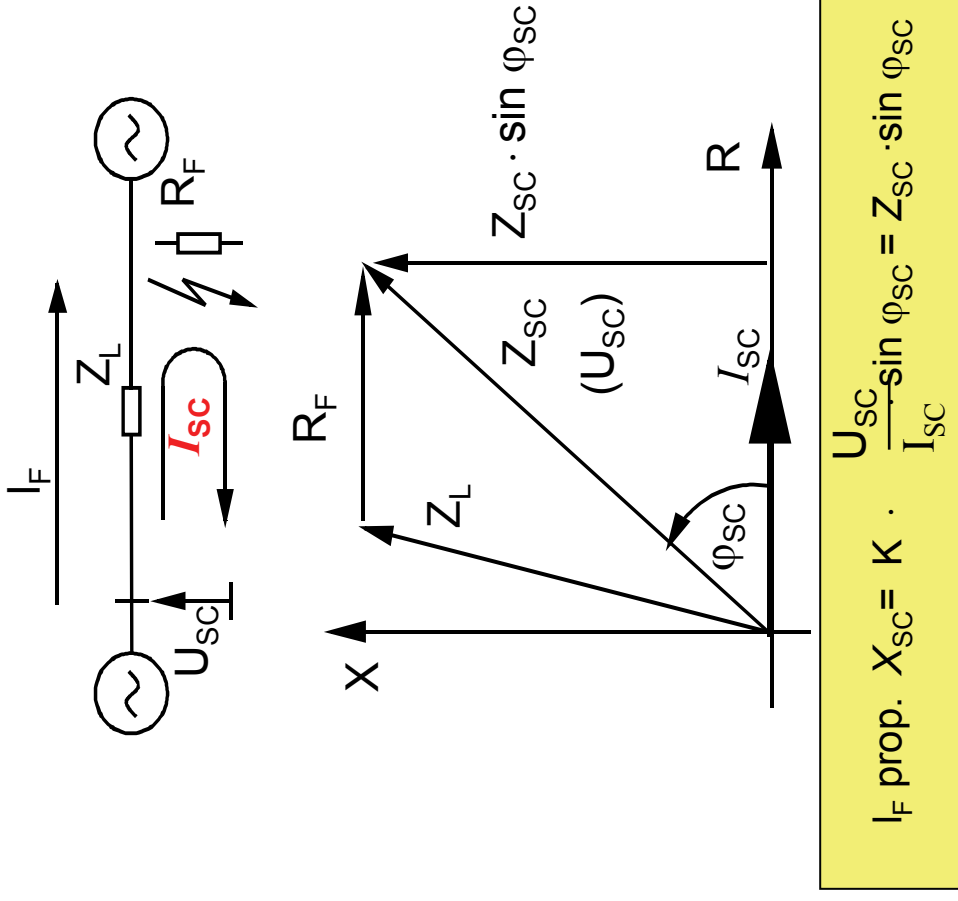


Example: 110 kV OH-line ($l = 50$ km)

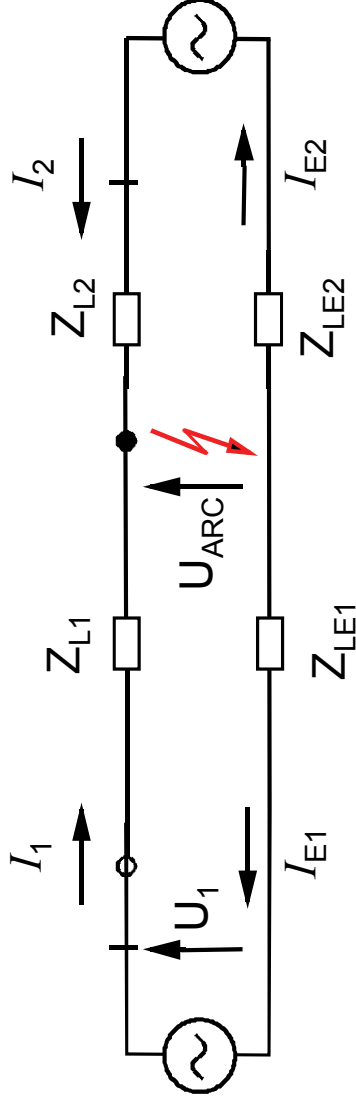
Fault locating:

distance-to-fault measurement with arc compensation

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Short-circuit with arc resistance and double-sided in-feed, influence on distance measurement

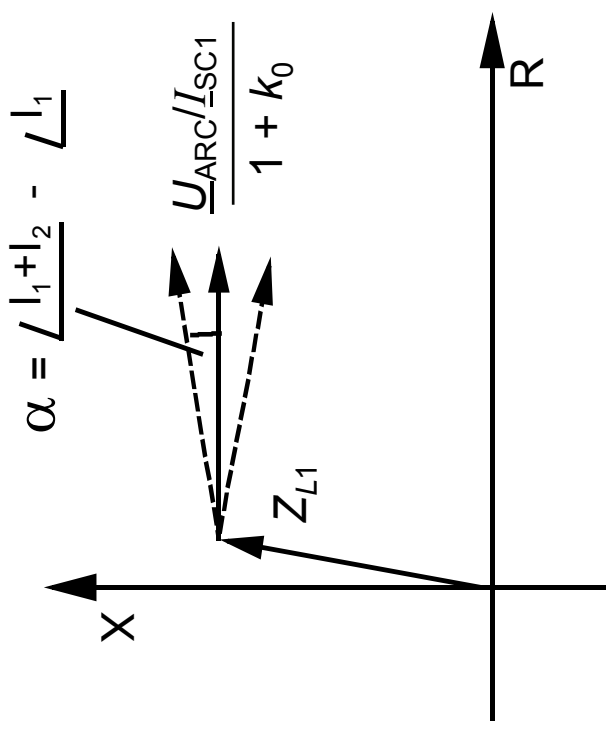


$$U_1 = I_1 \cdot Z_{L1} + I_{E1} \cdot Z_{E1} + U_{ARC}$$

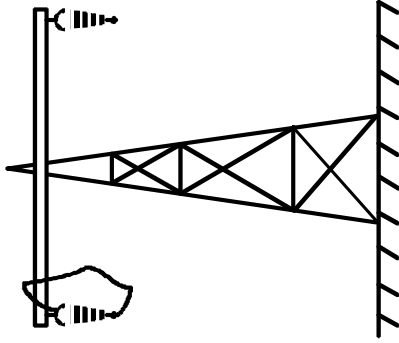
$$Z_{Rel} = \frac{U_1}{I_1 + k_0 \cdot I_{E1}} = \frac{I_1 \cdot Z_{L1} + I_{E1} \cdot Z_{E1} + \frac{U_{ARC}}{I_1 + k_0 \cdot I_{E1}}}{I_1 + k_0 \cdot I_{E1}}$$

$$\text{for } I_1 = I_{E1} = I_{SC1} \text{ and } k_0 = \frac{Z_{LE}}{Z_L} \quad \xrightarrow{\quad}$$

$$Z_{Rel} = Z_{L1} + \frac{U_{ARC}}{(1 + k_0) \cdot I_{SC1}}$$



Estimation of arc resistance



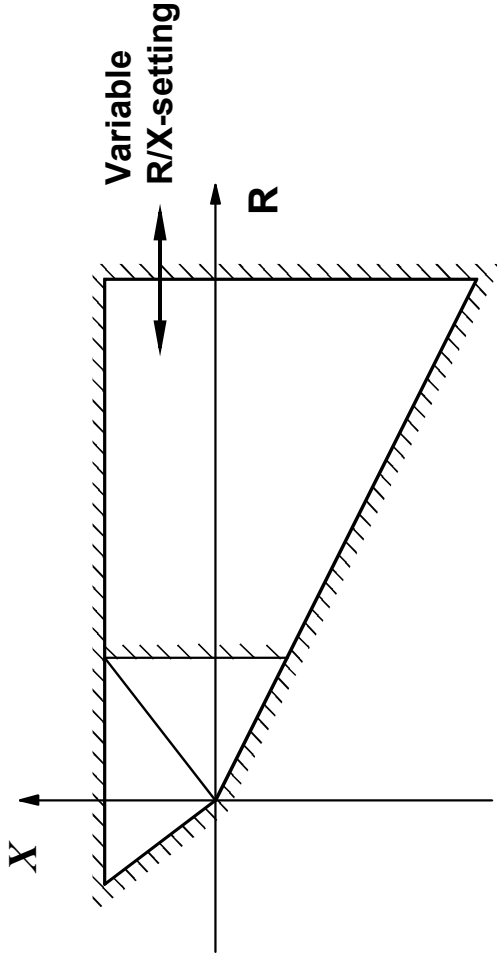
Worrington formula:

$$R_{ARC} = \frac{28700}{I[A]^{1,4}} \cdot l[m] \text{ Ohm}$$

Rough estimation:

$$U_{ARC} = 2500 \text{ V/m}$$

$$R_{ARC} = \frac{2500 [V/m] \cdot d[m]}{I_F [A]} \text{ Ohm}$$



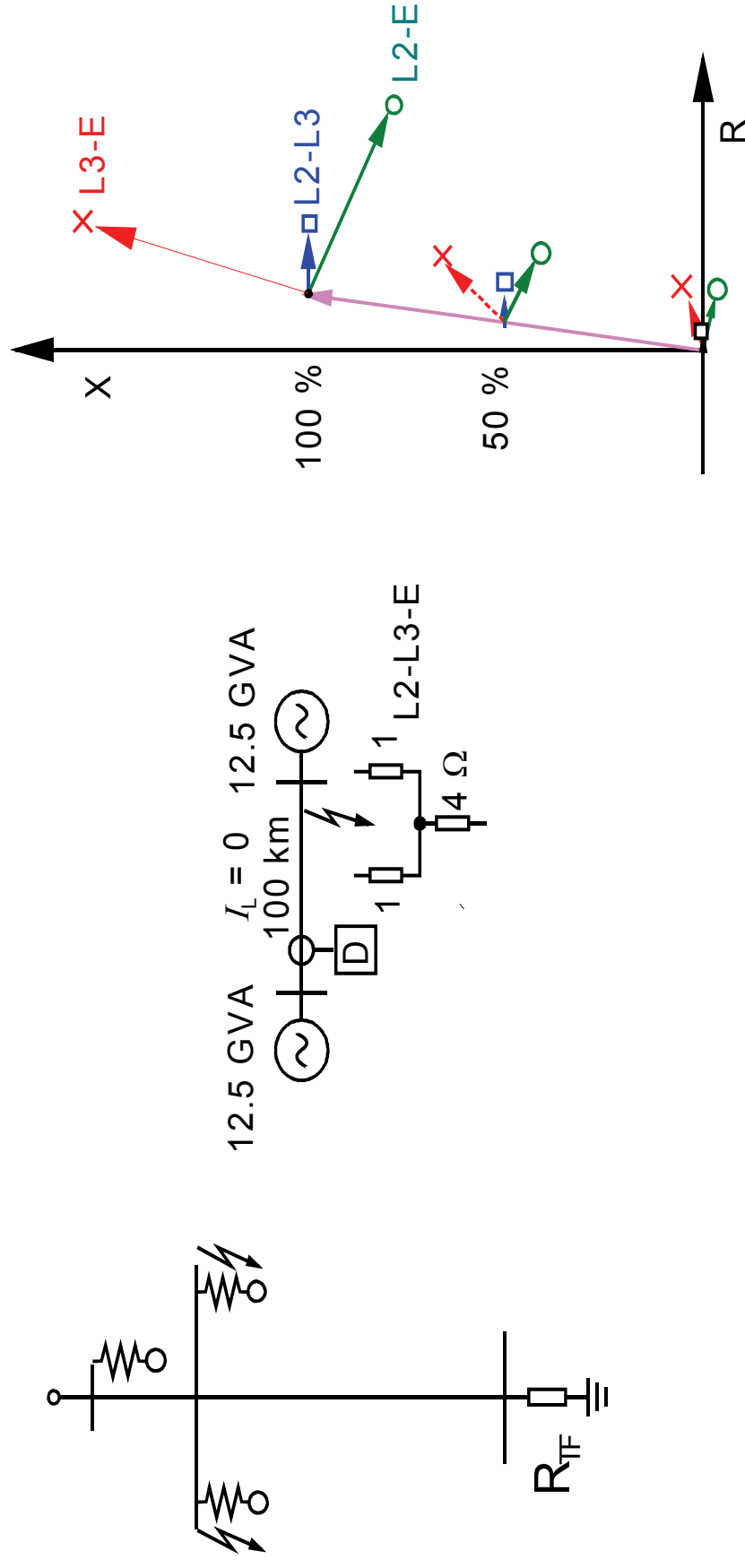
Phase-to-phase clearances

d =	3,5 m	(110 kV)
d =	7 m	(220 kV)
d =	11 m	(380 kV)

Insulator lengths (long-rod insulator)

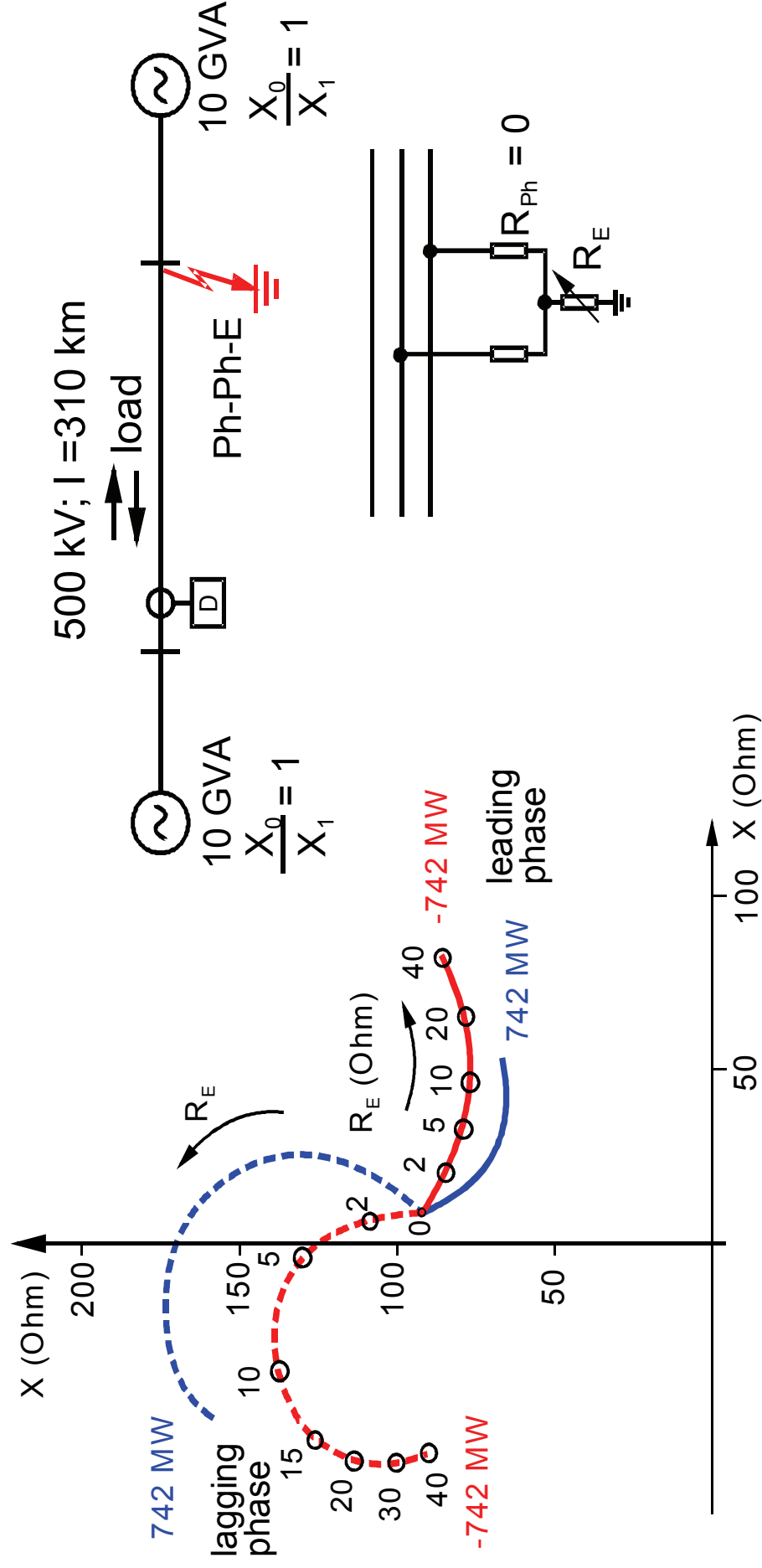
l =	1x1,3 = 1,3 m	(110 kV)
l =	2x1,3 = 2,6 m	(220 kV)
l =	3x1,3 = 3,9 m	(380 kV)

Ph-PH-E short-circuit with fault resistances, Measured loop impedances depending on fault location



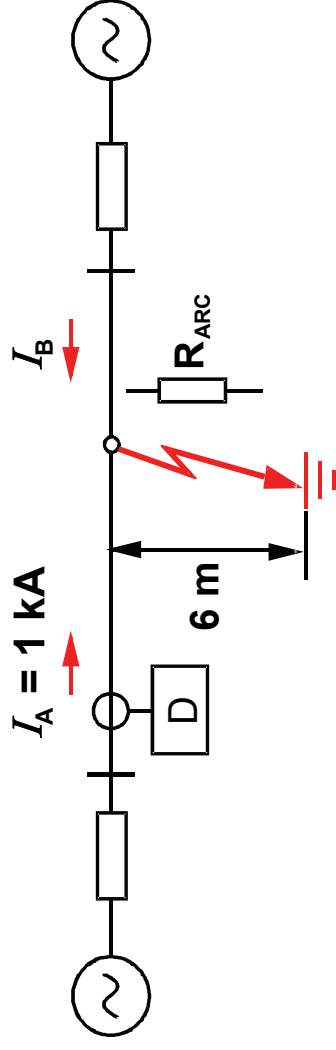
Loop impedances during Ph-Ph-E short-circuit, depending on fault resistance to earth and load conditions

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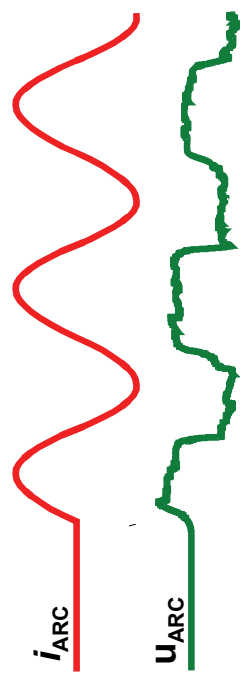
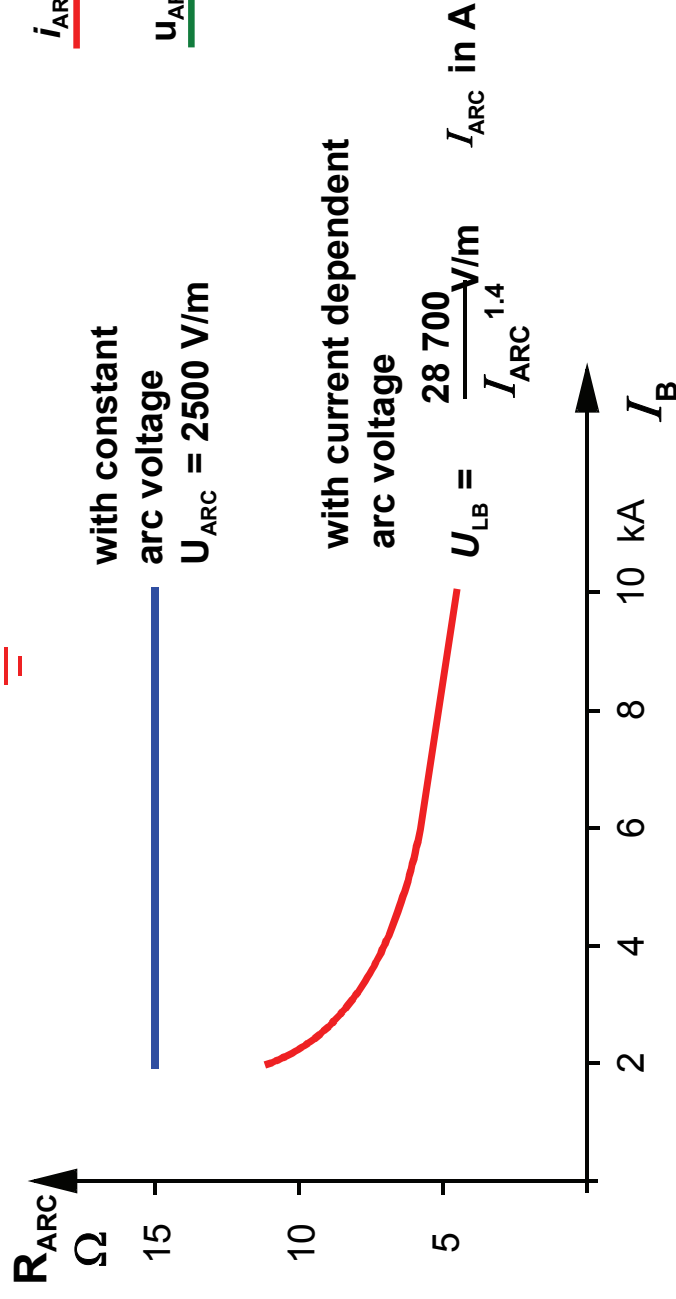
Effective arc resistance „seen“ by the distance relay with double-sided in-feed (example)

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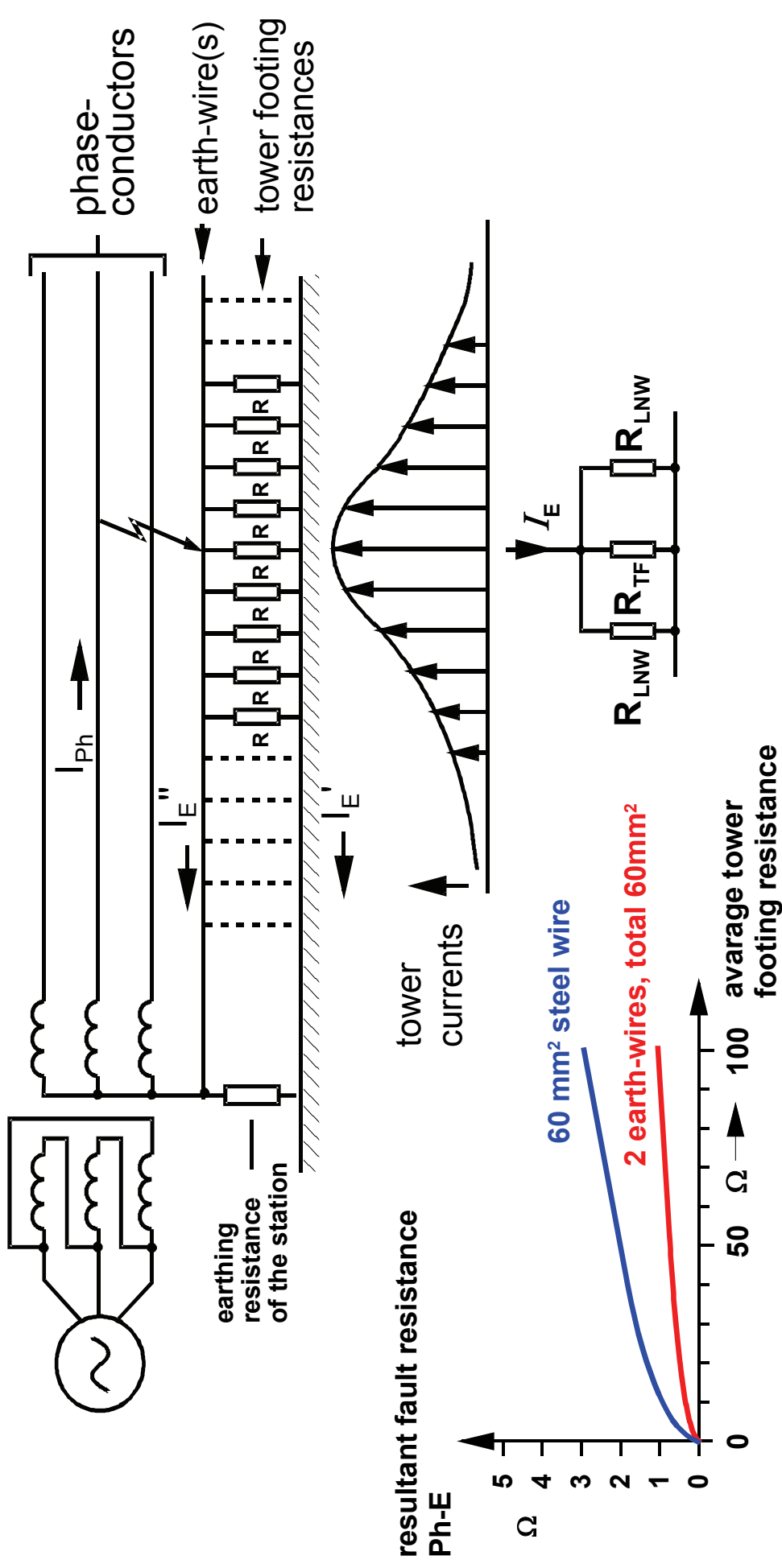


$$\underline{U}_A = \underline{I}_A \cdot \underline{Z}_L + \underline{U}_{ARC}$$

$$\underline{Z}_A = \frac{\underline{U}_A}{\underline{I}_A} = \underline{Z}_L + \frac{\underline{U}_{ARC}}{\underline{I}_A}$$

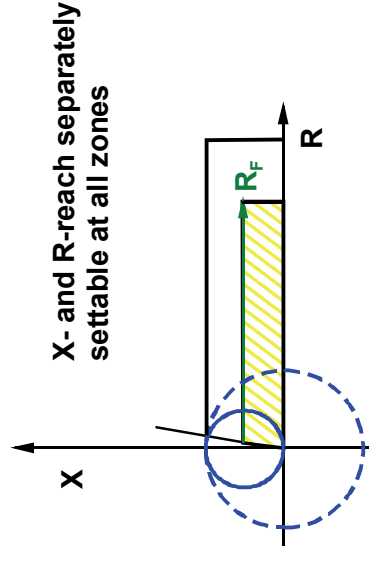
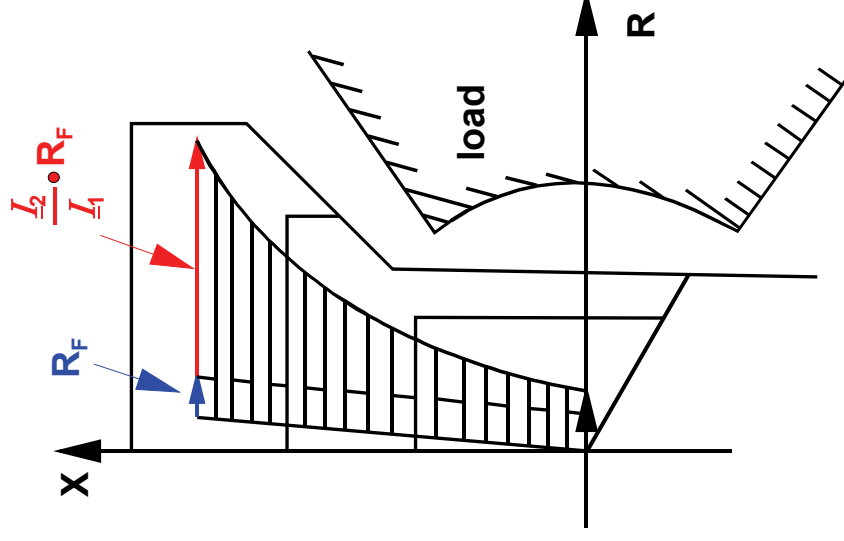
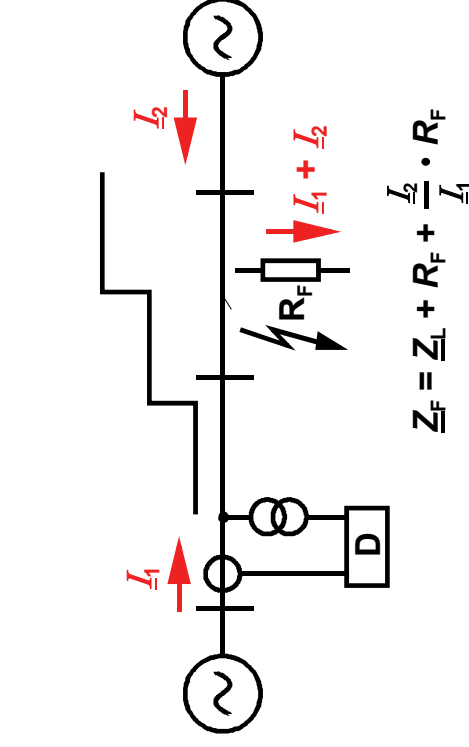


Resultant fault resistance on overhead lines with earth-wire

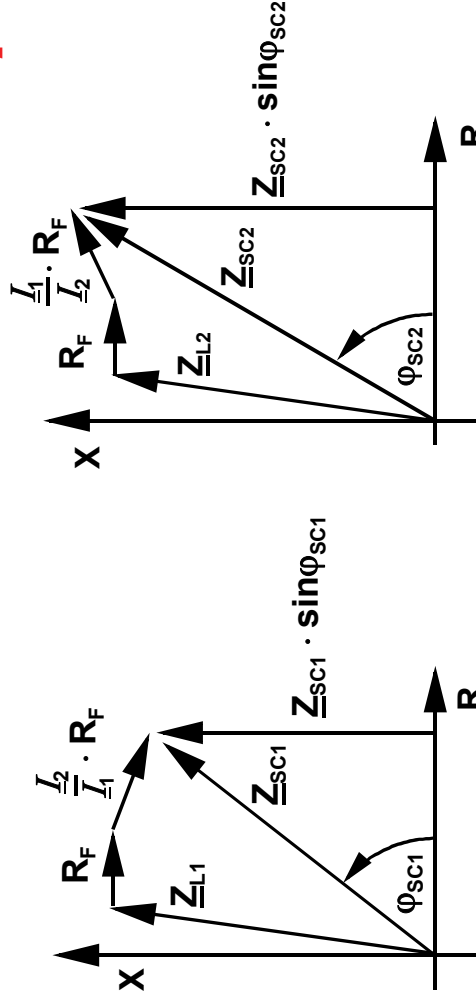
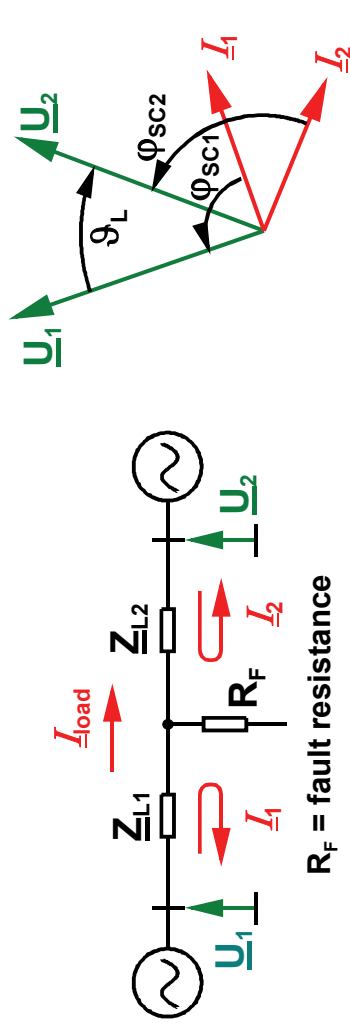


Quadrilateral characteristic with load cut-out for high line loadability

- High reach for remote back-up and adapted arc tolerance (good fault-load discrimination)
- High arc compensation even with short lines



Influence of load flow on the distance measurement for faults with fault resistance

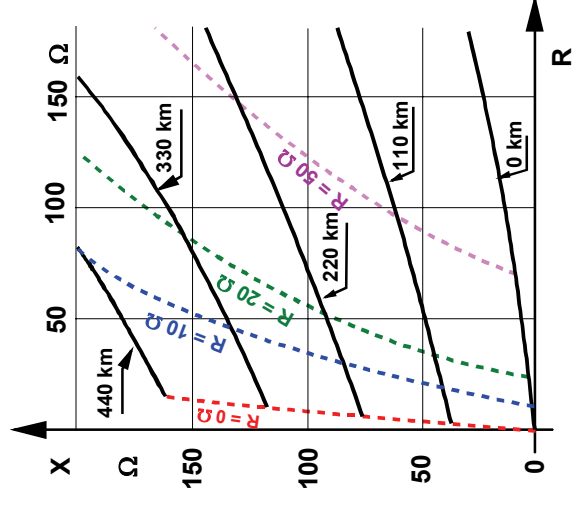
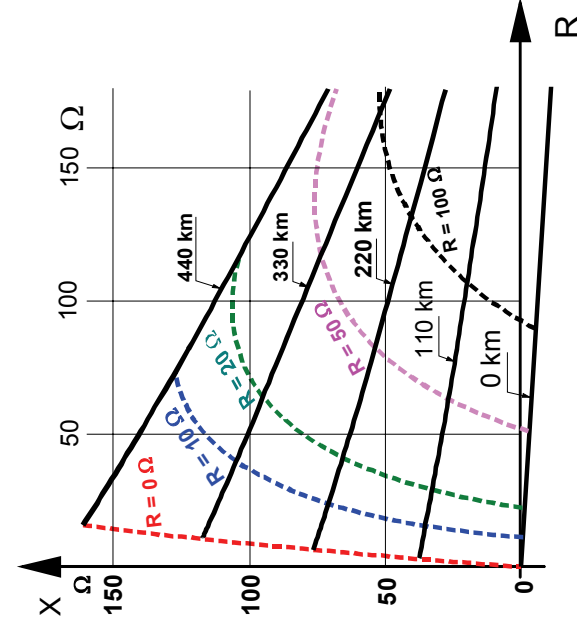
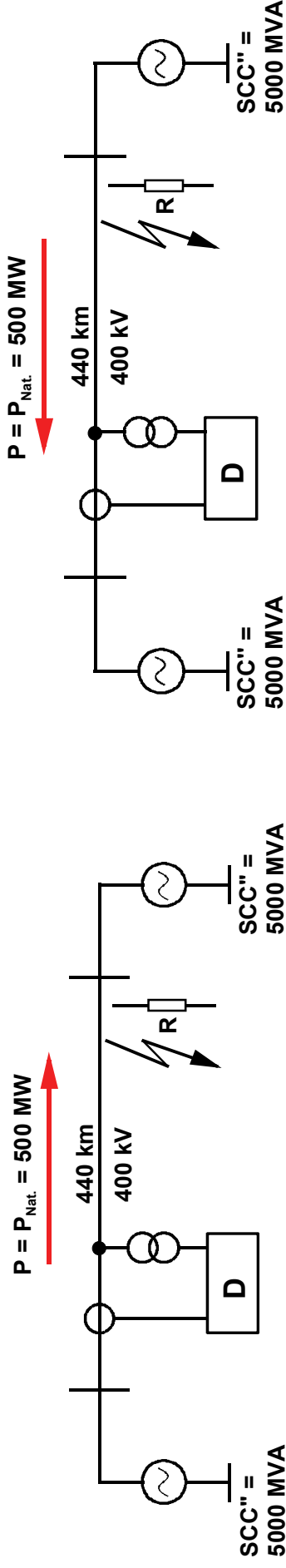


$$\underline{Z}_{K1} = \underline{Z}_{L1} + R_F + \frac{I_2}{I_1} \cdot R_F$$

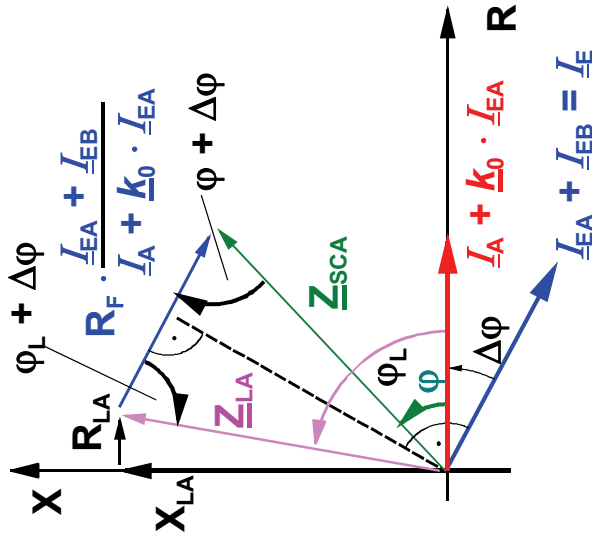
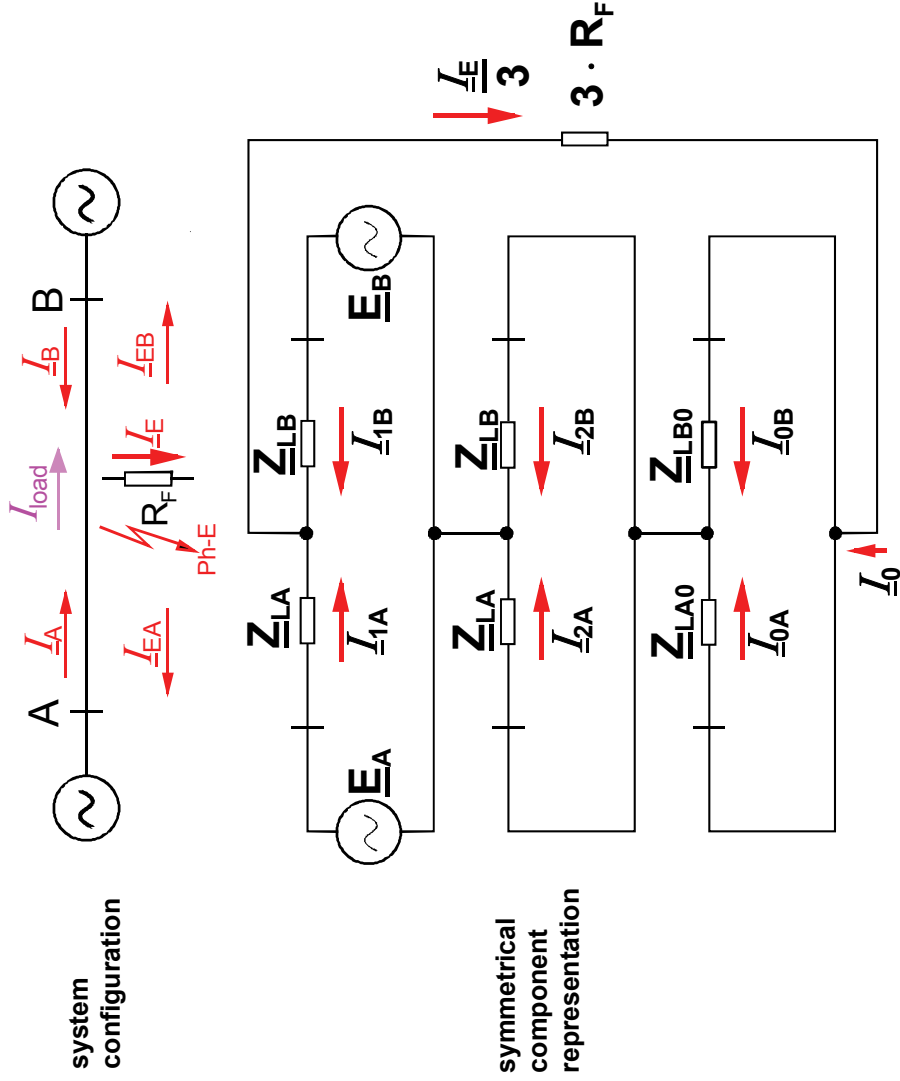
$$\underline{Z}_{K2} = \underline{Z}_{L1} + R_F + \frac{I_1}{I_2} \cdot R_F$$

Distance measuring error for faults with fault resistance in conjunction with load transfer

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Distance measurement during resistance faults, principle of load compensation for 1-Ph-E faults



$$Z_{SCA} = \frac{U_{A(Ph-E)}}{(I_A + k_0 \cdot I_{EA})} \quad K_0 = \frac{1}{3} \cdot \frac{(Z_{LO} - Z_{L1})}{Z_{L1}}$$

$$X_{LA} = |Z_{SC} - A| \frac{\sin(\varphi + \Delta\varphi)}{\sin(\varphi_L + \Delta\varphi)} \sin \varphi_L$$

Adaptation of the polarised MHO-circle to the rotation of the fault resistance in the case of faults with load prior to fault inception

